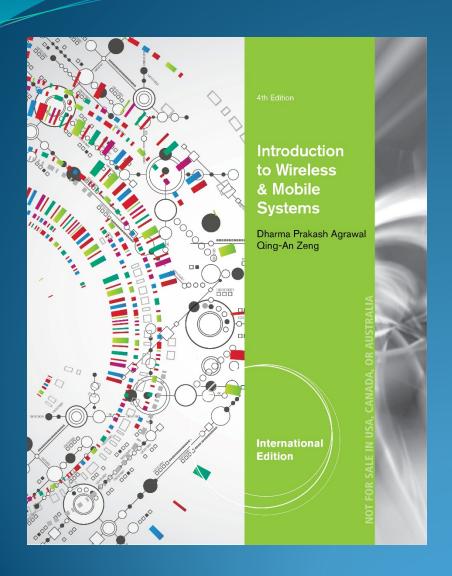
Introduction to Wireless & Mobile Systems



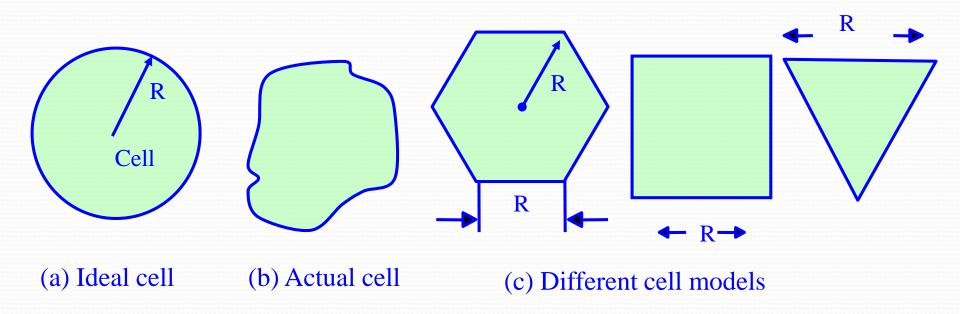
Chapter 5 The Cellular Concept



Outline

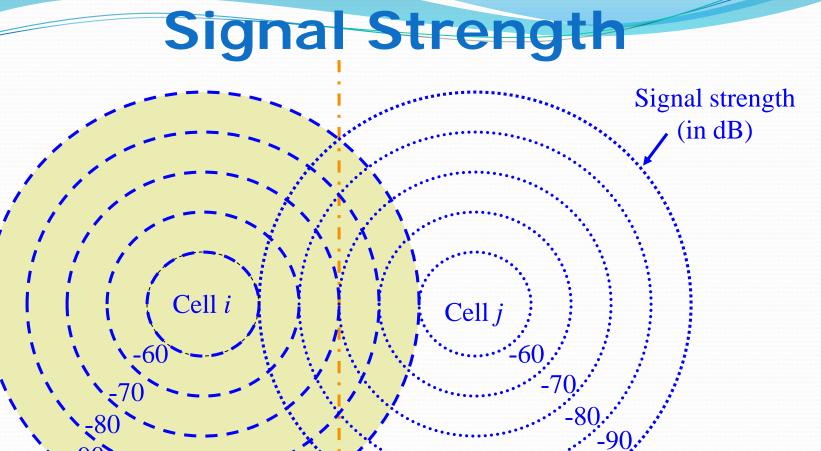
- Cell Area
 - Actual cell/Ideal cell
- Signal Strength
- Handoff Region
- Capacity of a Cell
 - > Traffic theory
 - > Erlang B and Erlang C
- Frequency Reuse
- How to form a Cluster
- Co-channel Interference
- Cell Splitting
- Cell Sectoring

Cell Shape



Impact of Cell Shape and Radius on Service Characteristics

Shape of the Cell	Area	Boundary	Boundary Length/ Unit Area	Channels/ Unit Area with N Channels/ Cell	Channels/Unit Area when Number of Channels Increased by a Factor K	Channels/Unit Area when Size of Cell Reduced by a Factor M	
Square cell (side =R)	R ²	4R	$\frac{4}{R}$	$\frac{N}{R^2}$	$\frac{\mathrm{KN}}{R^2}$	$\frac{\mathbf{M}^{2}\mathbf{N}}{R^{2}}$	
Hexagonal cell (side=R)	$\frac{3\sqrt{3}}{2}R^2$	6R	$\frac{4}{\sqrt{3}R}$	$\frac{N}{1.5\sqrt{3}R^2}$	$\frac{\text{KN}}{1.5\sqrt{3}R^2}$	$\frac{\text{M}^2\text{N}}{1.5\sqrt{3}R^2}$	
Circular cell (radius=R)	π R ²	2πR	2 R	$\frac{N}{\pi R^2}$	$\frac{\mathrm{KN}}{\pi R^2}$	$\frac{\mathrm{M}^{2}\mathrm{N}}{\pi R^{2}}$	
Triangular cell (side=R)	$\frac{\sqrt{3}}{4}R^2$	3R	$\frac{4\sqrt{3}}{R}$	$\frac{4\sqrt{3}\mathrm{N}}{3R^2}$	$\frac{4\sqrt{3}\mathrm{KN}}{3R^2}$	$\frac{4\sqrt{3}M^2N}{3R^2}$	



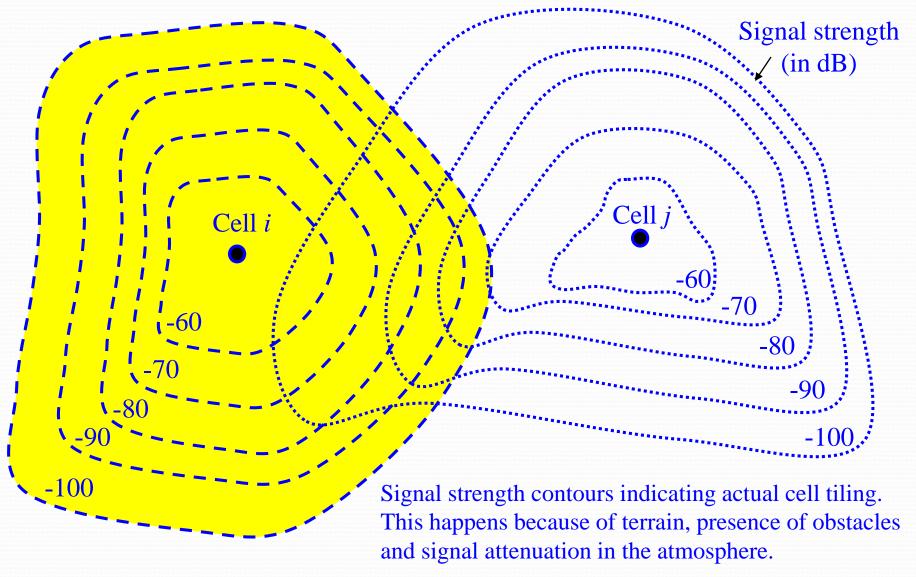
Select cell i on left of boundary

Select cell j on right of boundary

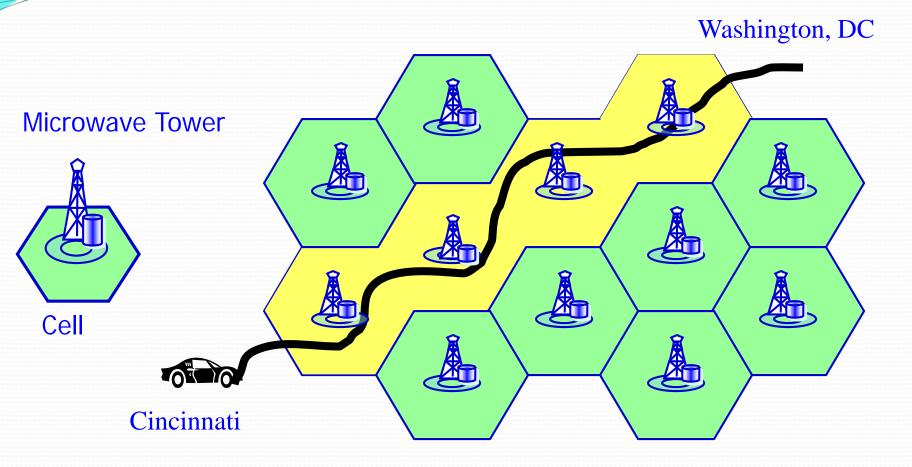
100

Ideal boundary

Actual Signal Strength

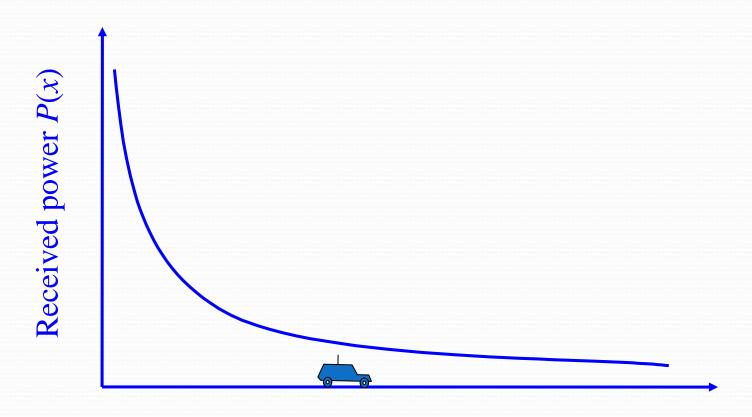


Universal Cell Phone Coverage



Maintaining the telephone number across geographical areas in a wireless and mobile system

Variation of Received Power



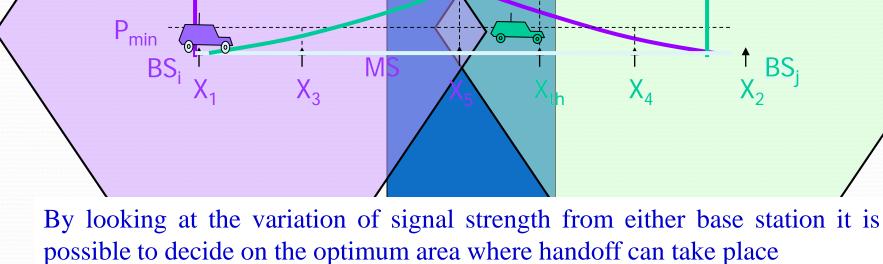
Distance *x* of MS from BS

handoff Region
放手,(原本聽一個基地台的訊號,到後面因為另一個基地台訊號較強,
Signab 出切換到聽後面另一個基地台的訊號)
due to BS_i

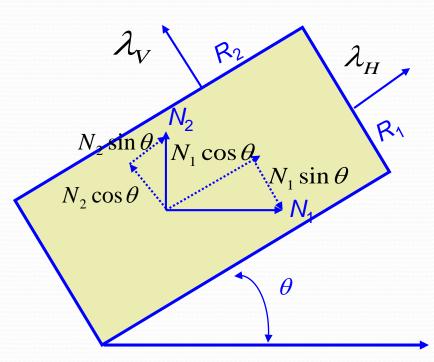
Pi(x),Pj(x)就是兩個BaseStation的訊號強度和距離的關係

P_i(x)

P_j(x)



Handoff Rate in a Rectangular Area



 N_1 is the number of MSs per unit length in horizontal direction

 N_2 is the number of MSs per unit length in vertical direction

Since handoff can occur at sides R_1 and R_2 of a cell

$$\lambda_{H} = R_{1}(N_{1}\cos\theta + N_{2}\sin\theta) + R_{2}(N_{1}\sin\theta + N_{2}\cos\theta)$$

Assuming area $A = R_1 R_2$ is fixed, substitute $R_2 = A/R_1$, differentiating λ_H with respect to R_1 and equating to 0 gives

$$N_1 cosq + N_2 sinq - A/R_1^2 (N_{1s} inq + N_2 cosq) = 0$$

Handoff Rate in a Rectangular Area

Thus, we have:

$$R_1^2 = A \frac{N_1 \sin \theta + N_2 \cos \theta}{N_1 \cos \theta + N_2 \sin \theta}$$
 $R_2^2 = A \frac{N_1 \cos \theta + N_2 \sin \theta}{N_1 \sin \theta + N_2 \cos \theta}$

Simplifying through few steps gives:

$$\lambda_{H} = 2\sqrt{A(N_{1}\cos\theta + N_{2}\sin\theta)(N_{1}\sin\theta + N_{2}\cos\theta)}$$

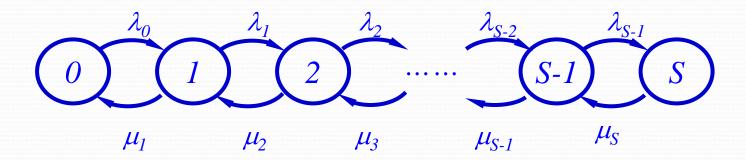
 λ_H is minimized when $\theta = 0$, giving

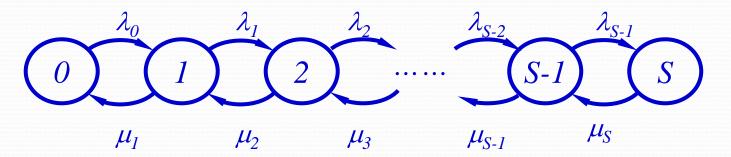
$$\lambda_H = 2\sqrt{AN_1N_2}$$
 and $\frac{R_1}{R_2} = \frac{N_1}{N_2}$

- Average number of MSs requesting service (Average arrival rate): λ
- Average length of time MS requires service (Average holding time): *T*
- Offered load: $a = \lambda T$
- e.g., in a cell with 100 MSs, on an average 30 requests are generated during an hour, with average holding time T=360 seconds
- Then, arrival rate $\lambda=30$ requests/3600 seconds =1/120 requests/sec
- A channel kept busy for one hour is defined as one Erlang (a), i.e.,

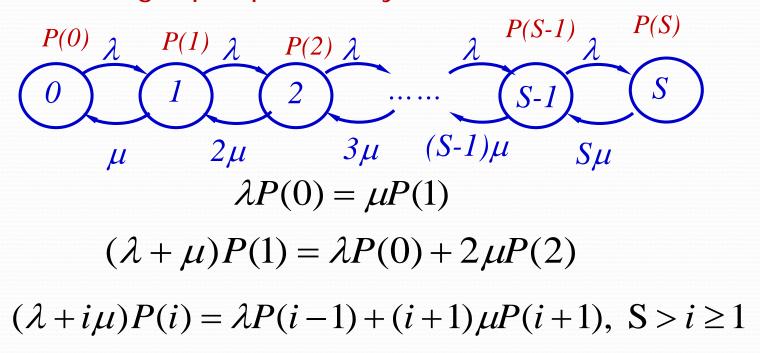
$$a = \# calls * duration = \frac{30 \ Calls}{3600 \ Sec} \cdot \frac{360 \ Sec}{call} = 3 \ Erlangs$$

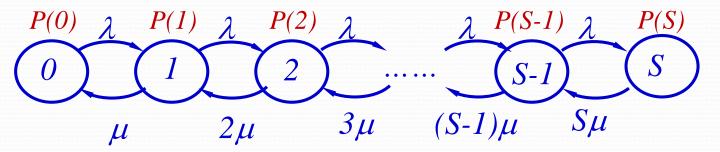
- Average arrival rate λ during a short interval t is given by λ t
- Average service (departure) rate is μ
- The system can be analyzed by a *M/M/S/S* queuing model, where *M* is interarrival time of users, *M* is distribution of service time, *S* is the number of channels, and *S* is the maximum number of users in the system
- The steady state probability P(i) for this system in the form (for i = 0, 1, ..., S)





Assuming equal probability of an event





$$P(i) = (\frac{\lambda}{i\mu})^i P(0), = \frac{a^i}{i!} P(0)$$
 $i \ge 1$ where $a = \frac{\mu}{\lambda}$

This is steady state probability P(i)

As P(0)+P(1)+...P(S)=1; substituting in terms of P(0) gives

$$P(0) + \frac{a}{1!}P(0) + \frac{a^2}{2!}P(0) + \frac{a^3}{3!}P(0) + \dots + \frac{a^S}{S!}P(0) = 1$$

Therefore
$$P(0)\left[\sum_{i=0}^{S} \frac{a^i}{i!}\right] = 1, or P(0) = \left[\sum_{i=0}^{S} \frac{a^i}{i!}\right]^{-1}$$

Capacity of a Cell

• The probability P(S) of an arriving call being blocked is the probability that all S channels are busy

$$P(S) = \frac{a^{S}}{S!} P(0) = \frac{\frac{a^{S}}{S!}}{\sum_{i=0}^{S} \frac{a^{i}}{i!}}$$

- This is Erlang B formula B(S, a)
- In the previous example, if S=2 and a=3, the blocking probability B(2, 3) is

$$B(2,3) = \frac{\frac{3^2}{2!}}{\sum_{k=0}^{2} \frac{3^k}{k!}} = \frac{\frac{9}{2}}{1+3+\frac{9}{2}} = \frac{9}{19} = 0.529$$

• So, the number of calls blocked 30x0.529=15.87

Capacity of a Cell

Efficiency =
$$\frac{\text{Traffic nonblocked}}{\text{Capacity}}$$
=
$$\frac{\text{Erlangs x portions of used channel}}{\text{Number of channels}}$$
=
$$\frac{3(1-0.529)}{2} = \frac{1.413}{2} = 0.7065$$

The probability of a call being delayed:

$$C(S,a) = \frac{\frac{a^{S}}{(S-1)!(S-a)}}{\frac{a^{S}}{(S-1)!(S-a)} + \sum_{i=0}^{S-1} \frac{a^{i}}{i!}}$$
$$= \frac{S.B(S,a)}{S-a[1-B(S-a)]}$$

This is Erlang C Formula

$$as B(S,a) = \frac{\frac{a^S}{S!}}{\sum_{i=0}^{S} \frac{a^i}{i!}}$$

For S=5, a=3, B(5,3)=0.11, gives C(5,3)=0.2360

Erlang B and Erlang C

Probability of an arriving call being blocked is

$$B(S,a) = \frac{a^{S}}{S!} \cdot \frac{1}{\sum_{k=0}^{S} \frac{a^{k}}{k!}}, \qquad \qquad \underline{Erlang \ B \ formula}$$

where S is the number of channels in a group

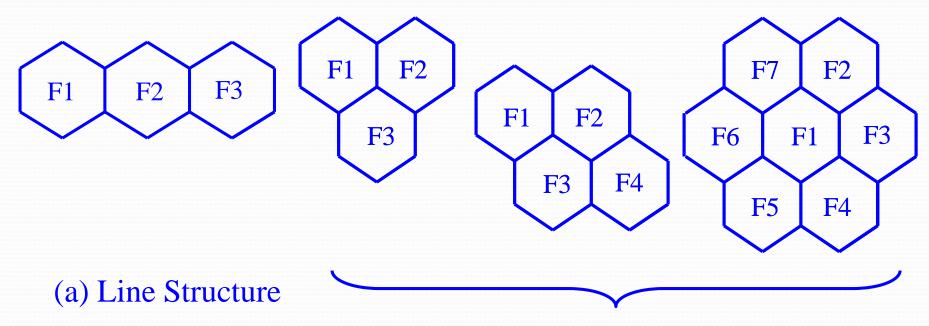
Probability of an arriving call being delayed is

$$C(S,a) = \frac{\frac{a^{S}}{(S-1)!(S-a)}}{\frac{a^{S}}{(S-1)!(S-a)} + \sum_{i=0}^{S-1} \frac{a^{i}}{i!}}, \qquad \underline{Erlang\ C\ formula}$$

where C(S, a) is the probability of an arriving call being delayed with a load and S channels

Cell Structure

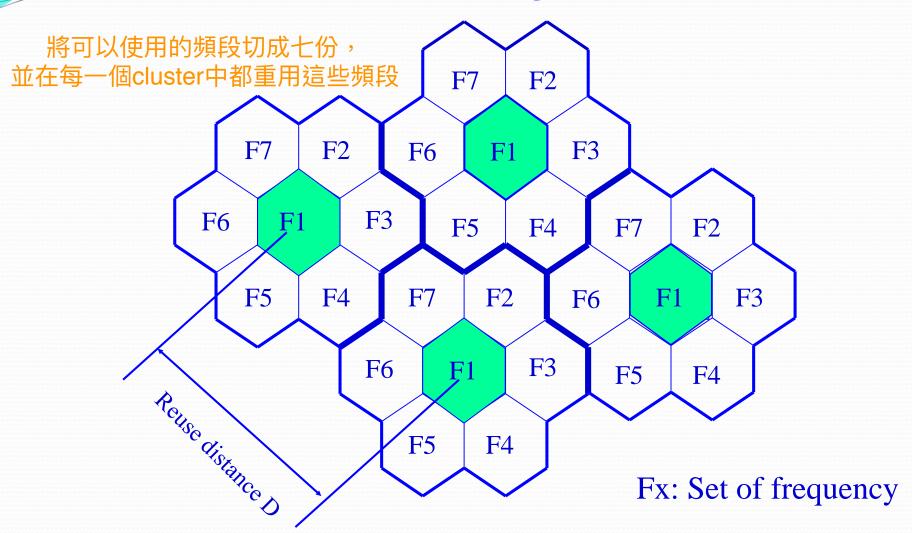
這些cell排列的結果稱作cluster



(b) Plan Structure

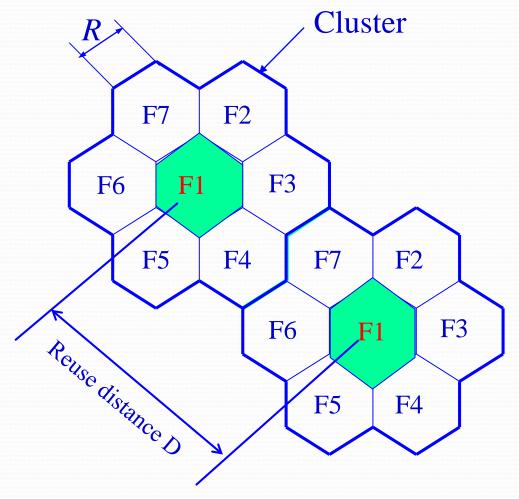
Note: Fx is set of frequency, i.e., frequency group

Frequency Reuse



7-cell reuse cluster

Reuse Distance



• For hexagonal cells, the reuse distance is given by

$$D = \sqrt{3N}R$$

N: cell的個數 R:半徑 where *R* is cell radius and *N* is the reuse pattern (the cluster size or the number of cells per cluster).

Reuse factor is

$$q \equiv \frac{D}{R} = \sqrt{3N}$$

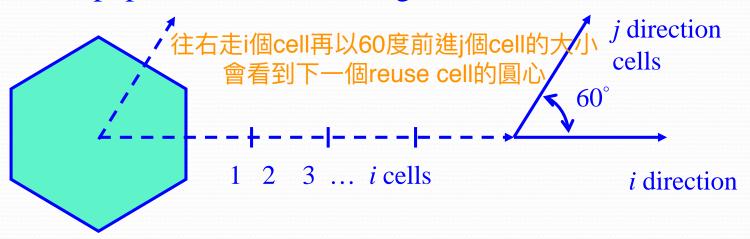
Reuse Distance (Cont'd)

■ The cluster size or the number of cells per cluster is given by

$$N = i^2 + ij + j^2$$

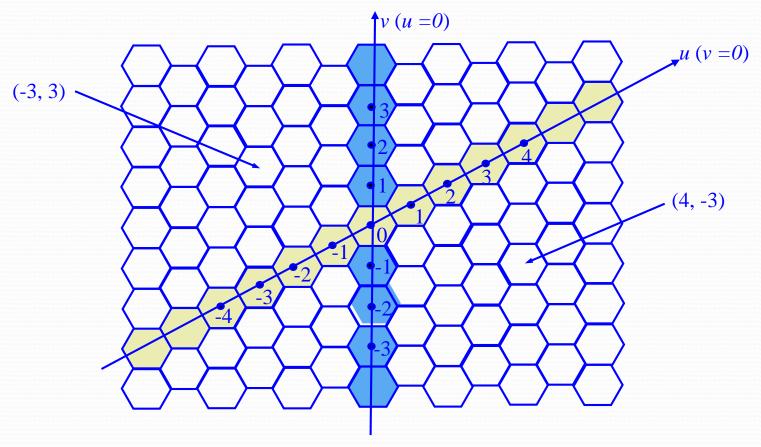
where i and j are positive integers, i.e. $0 \ge i, j < \infty$

N = 1, 3, 4, 7, 9, 12, 13, 16, 19, 21, 28,The popular value of *N* being 4 and 7



Reuse Distance (Cont'd)

$$N = i^2 + ij + j^2$$
 with *i* and *j* as integers



u and v coordinate representation of cells with (0,0) center

Reuse Distance and Channel set to use

■ For j=1, the cluster size is given by $N = i^2 + i + 1$

Then defining $L = [(i+1)u + v] \mod N$

We can obtain label L for the cell whose center is at (u,v).

For N=7, with i=2, j=1:

$$L = (3u + v) \bmod 7$$

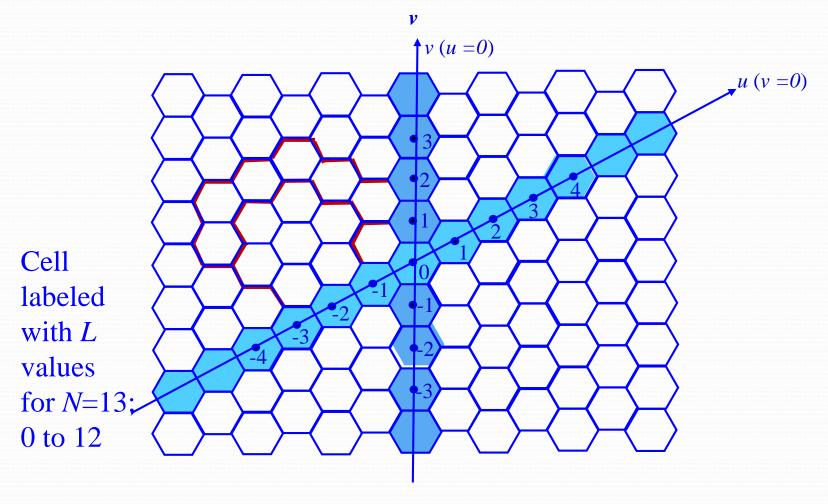
u	0	1	-1	0	0	1	-1
V	0	0	0	1	-1	-1	1
L	0	3	4	1	6	2	5

Gives assignment of Labeling channels to use in different cells values for N=7

v v (u=0)An alternative

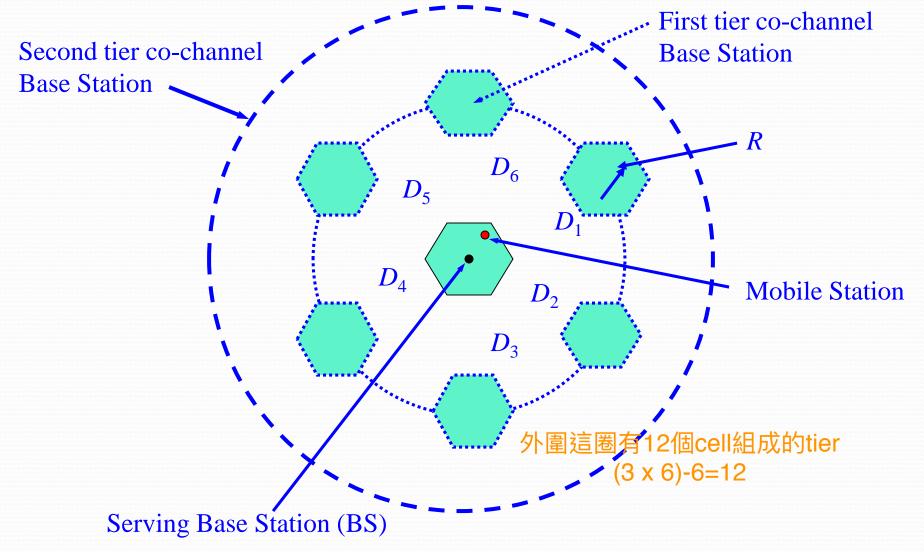
Reuse Distance and Channel set to use

For
$$N=13$$
, $i=3$, $j=1$; $L = (4u + v) \mod 13$

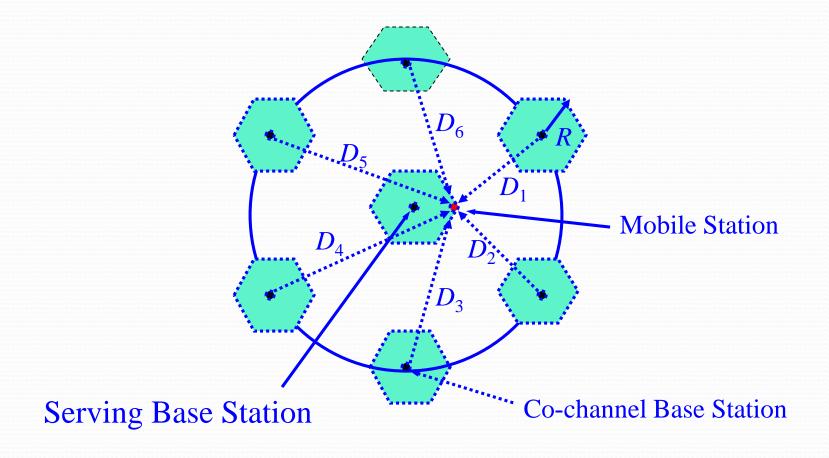


Cochannel Interference

自己所在cell以外的cluster中其他cell的訊號對其造成的干擾



Worst Case of Cochannel Interference



Cochannel Interference

Cochannel interference ratio is given by

$$\frac{C}{I} = \frac{Carrier}{Interference} = \frac{C}{\sum_{k=1}^{M} I_k}$$

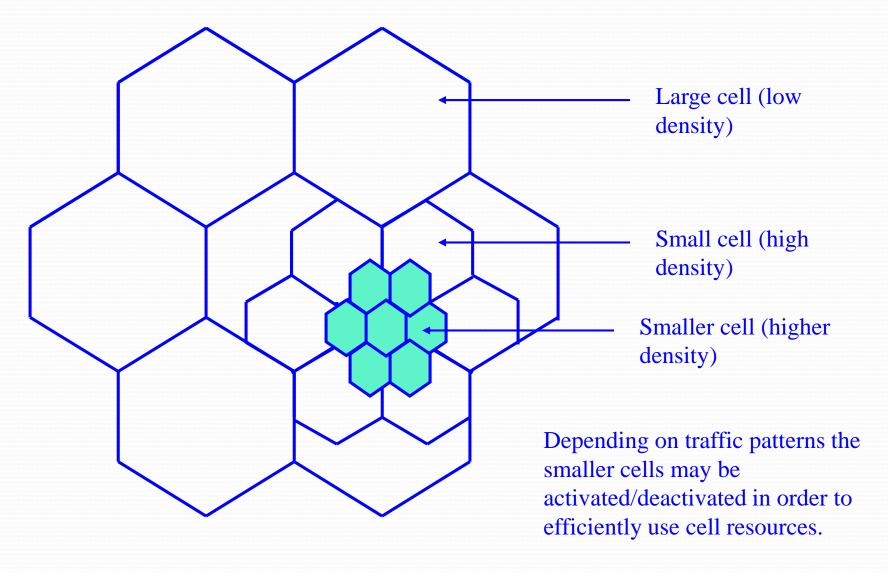
where *I* is co-channel interference and *M* is the maximum number of co-channel interfering cells

For M = 6, C/I is given by:

$$\frac{C}{I} = \frac{C}{\sum_{k=1}^{M} \left(\frac{D_k}{R}\right)^{-\gamma}}$$

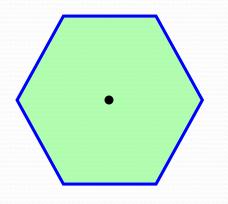
where γ is the propagation path loss slope and $\gamma = 2 \sim 5$

Cell Splitting

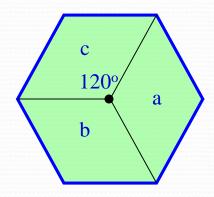


Cell Sectoring by Antenna Design 在cell中切出多個區域,每個區域都只在特定方向傳送特定頻率的訊號,

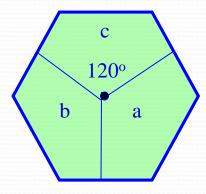
讓其他區域較不會收到干擾



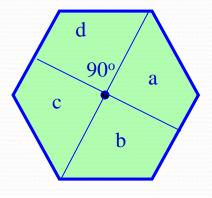
(a). Omni



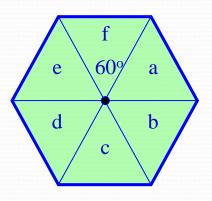
(b). 120° sector



(c). 120° sector (alternate)



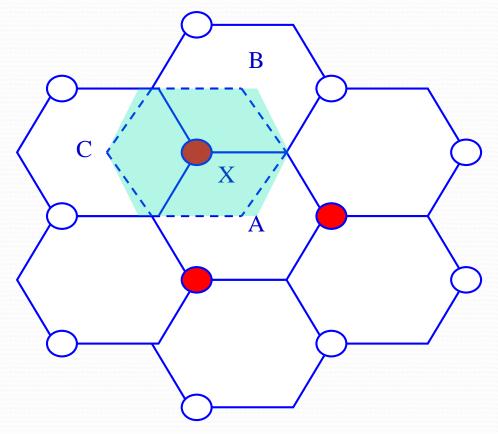
(d). 90° sector



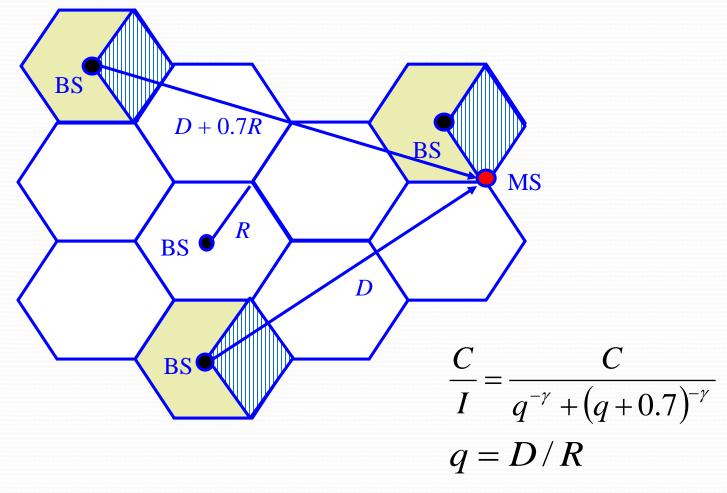
(e). 60° sector

Cell Sectoring by Antenna Design

 Placing directional transmitters at corners where three adjacent cells meet

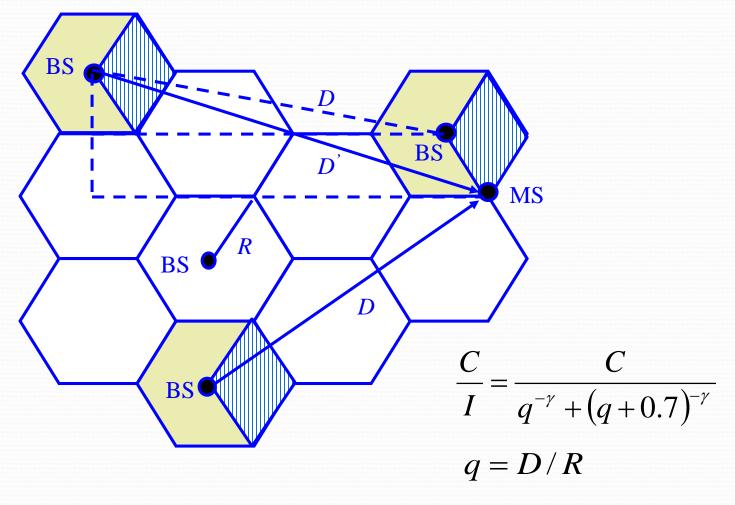


Worst Case for Forward Channel Interference in Three-sectors



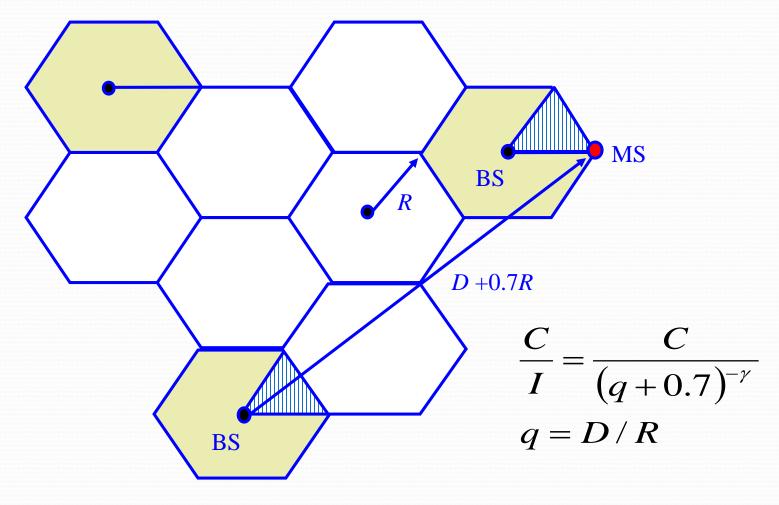
where γ is the propagation path loss slope and $\gamma = 2 \sim 5$

Worst Case for Forward Channel Interference in Three-sectors



where γ is the propagation path loss slope and $\gamma = 2 \sim 5$

Worst Case for Forward Channel Interference in Six-sectors



where γ is the propagation path loss slope and $\gamma = 2 \sim 5$