

REPORT ON OpenDreamKit DELIVERABLE D6.9

Shared persistent Memoisation Library for PYTHON/SAGE

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- **WP6:** Data/Knowledge/Software-Bases
- **Lead Institution:** University of St Andrews
- **Due:** 2019-02-28 (month 42)
- **Nature:** Other
- **Task:** T6.9 (#131)
- **Proposal:** p. 54
- **Upcoming Report** (sources)

Persistent memoisation is the computational process of storing a program's outputs and retrieving them later, instead of re-running programs that are guaranteed to return the same answer. This approach may be useful in a wide range of fields, but it is particularly relevant to mathematics because of the type of problems mathematicians wish to solve: those with a small input and a small output, but which may still take a long time to complete.

Results can be stored for future calls to a function in the present program session, in later sessions, or even for other users in different parts of the world. Beside the advantages of recalling old results instead of repeating work, a human-readable cache could also be used by researchers to create a reproducible record of computed results that can be used outside the context of the memoisation system itself.

The aim of T6.9 is to establish a persistent memoisation framework to cache results in Python and GAP across sessions, in a way that is easy to deploy and configure, and allows for results to be shared reliably between different researchers. D6.9 requires a "shared persistent memoisation library for Python/Sage", which is fulfilled by `pypersist`, a new Python library written by the current author.

In this report, we present a review of some existing tools for memoisation, describe the new Python library `pypersist`, and give an overview of the future direction of this project.

1. INTRODUCTION

Persistent memoisation refers to the computational practice of storing program results whenever they are computed, and then looking up and retrieving them later, instead of re-running programs that are guaranteed to return the same answer. This approach allows users to avoid unnecessary computation, and makes it possible to create an archive of results that can be used for other purposes later.

A memoised function can be seen as a middle ground between a database and a computer program: a function can have a large (perhaps infinite) domain which makes storing all its outputs in a database impractical; but it may also have a long enough run-time that re-computing an output each time it is called is undesirable. The practice of memoisation – that is, recalling results that happen to have been pre-computed, and computing results that are unknown – bridges the gap between these two extremes.

This approach may be useful in a wide range of fields, but it is particularly relevant to mathematics because of the type of problems mathematicians wish to solve. Mathematics is a rare example of a field with algorithms that require a lot of processing, but have a small input and small output.

Many algorithms in the real world have a large input and a small output – for example, the problem of determining which streamed TV show to recommend to a viewer takes as its input a huge amount of data about past choices consumers have made, and returns a single title as its output. The output of this function can be stored easily, but so much time would be spent processing the large input, and the same input would be repeated so infrequently, that this type of memoisation would have little advantage.

Conversely, many algorithms have a small input and a large output – for example, rendering a plain text file on a screen takes a small amount of data as an input, but creates an image which is likely to be large if stored. In this case, the input can be dealt with quickly, but memoising the output using a disk is likely to be slower than recomputing it from scratch each time.

In mathematics, however, we frequently encounter computational problems with both small input and small output. For instance, we may wish to know whether a given permutation group G is simple; the input may be two or three generators for G , which between them use only a few bytes on a computer, and the output is a single boolean. But despite the small sizes of these data sets, the algorithm may take a long time to complete, and may use a large amount of memory while in progress. Thus, memoising results of this type will use very little disk space, require very little processing, and may avoid a huge amount of work when recalling previously computed results.

It is also worth noting that pure mathematical problems are likely to have discrete inputs and outputs, and are therefore unlikely to suffer from numerical noise. This makes them even more suitable for memoisation, since we do not have a high density of almost-equal inputs that nonetheless would have to be memoised separately.

Furthermore, there is no reason that a memoisation cache should be limited to a single user. A memoisation framework could save results to a shared directory for immediate use by other researchers connected by a network, or could even use an online database for the cache, so long as sufficient precautions were taken to avoid reading and writing clashes.

Besides the obvious advantages of recalling cached results instead of repeating work, a memoisation framework that allows a human-readable cache could be used by researchers to create a reproducible record of computed results that can be included in papers, or shared with collaborators that have no knowledge of the memoisation system.

The aim of ODK Task 6.9 is to establish a persistent memoisation framework to cache results in Python and GAP across sessions, in a way that is easy to deploy and configure, and allows for results to be shared reliably between different researchers. Deliverable 6.9 requires a “shared persistent memoisation library for Python/Sage”, which is fulfilled by `pypersist`, a new Python library written by the current author. The corresponding software for GAP is in progress, in the form of GAP’s `Memoisation` package, which aims to have the same features as `pypersist`, and to be as compatible as possible with it.

In this report, we will present a review of some existing tools for memoisation (Section 2), describe the new Python library `pypersist` (Section 3), and give an overview of the future direction of this project (Section 4).

2. EXISTING TOOLS

In this section we will consider some tools that already exist for memoisation, with a focus on Python and Sage tools. Some of the tools we discuss are only intended for a subset of the complete memoisation process, while others are more full-featured but lack some important desirable features. A comparison of these tools is shown in Table 1.

	Updated in last year	Python versions	Function decorator	Memory caching	Disk caching	Database caching	Method support	Compiled function support	Custom keys	Custom pickling	Metadata	Sage support	Compiled
GAP operation/attribute	✓	—		✓			✓						
Sage <code>func_persist</code>	✓	Sage	✓	✓	✓							✓	
Sage <code>cached_function</code>	✓	Sage	✓	✓				✓	✓			✓	✓
Sage <code>cached_method</code>	✓	Sage	✓	✓			✓	✓	✓			✓	✓
<code>persist</code>		2/3		✓	✓								
PyMemoize	✓	2/3	✓	✓	✓		✓						
<code>redis-simple-cache</code>		2/3	✓	✓	✓	✓	✓						
<code>dogpile.cache</code>	✓	2/3	✓	✓	✓	✓	✓		✓				
<code>pypersist</code>	✓	2/3	✓	✓	✓	✓	✓		✓	✓	✓	✓	

TABLE 1. Comparison of memoisation tools

2.1. GAP

First, we should consider the existing persistence tools built into GAP and Sage. GAP functions can be installed as methods for an object's *operations* and *attributes*, and if they are, their results are stored for the duration of the current GAP session. However, these results are never saved to disk unless the session itself is stored, and the option is only available for methods of an object.

2.2. Sage

There exists in Sage a simple function decorator, `func_persist`, which can be applied to a function to save its output to disk. This is a working memoisation tool, and even this functionality has great practical use, but the tool has very little configurability: the only option that can be given is to specify the directory in which results are stored. Sage also contains two more configurable tools for memoising functions and methods, respectively named `cached_function` and `cached_method`. These allow a function or method to be memoised with a custom key-generating function, meaning that arguments can be pre-processed in an intelligent way, perhaps to sort arguments, or discard arguments that do not affect the return value of a function. They are also implemented in Cython, meaning that they are compiled rather than interpreted, and perform faster than `func_persist`. They also support compiled functions written in Cython. However, they only support memory caching – that is, they only store results in memory while the current program is running, and do not save results to disk for use in a later session.

These three decorators are useful, but limited. Not only do they lack certain options such as database caching and custom output pickling, but they rely on other parts of the Sage system, and therefore cannot be used more broadly in generic Python programs. Python memoisation tools exist outside Sage that can in principle be applied to Sage.

2.3. Python

Many memoisation tools are available on PyPI, each with a slightly different philosophy and set of features. Table 1 summarises four examples of these, indicating each one's features and status: `persist` and `redis-simple-cache` have not been updated in several years, while `PyMemoize` lacks even the custom key function provided by the Sage tools.

Perhaps the most promising of the existing tools is `dogpile.cache`, an API for caching function and method outputs to a variety of backends; this is a well-established, full-featured system, but it lacks certain features such as custom result pickling – particularly useful to mathematicians who may want to store output using OpenMath, or in some human-readable form for sharing.

There would be an argument for modifying and improving `dogpile.cache` to add these features, rather than creating a new tool. However, given the wide scope of the `dogpile` project, which is largely focused on thread management, it was decided to proceed with a new tool that could be adapted more easily to suit the specific requirements of the project, such as bespoke support for Sage-specific objects, and compatibility with the GAP memoisation package which would be developed in parallel.

To fulfill these requirements, the `pypersist` package was created. It runs in Python version 2 and 3, and it contains all the features mentioned in Table 1, except those features related to Cython. More information about `pypersist` is given in Section 3.

3. PYPERSIST

`pypersist` is a package for Python 2 and 3, created specifically to address the requirements of this deliverable. It has all the features considered in Table 1, having been designed with these features in mind.

3.1. Features

We now summarise some of the features of `pypersist`. The detailed workings of the package are outside the scope of this report, but full documentation is available at <https://pypersist.readthedocs.io>, and an extensive annotated demonstration of the package's features is given in an interactive notebook hosted on Binder at <https://mybinder.org/v2/gh/mtorpey/pypersist/master?filepath=binder/demo.ipynb>.

Decorator. In order to use all the features of the package, the `persist` decorator is the only thing that needs to be imported. After this, a function can be memoised by simply adding `@persist` above it. This minimal setup produces memoisation with safe defaults, and allows users to exploit the package with no additional knowledge of its features. However, using `@persist(...)` allows further customisation via arguments.

Configurable cache location. By default, results are saved to the `persist/<funcname>` subdirectory of the current working directory. However, by providing a string as the `cache` argument of `@persist`, this location can be changed.

Configurable function name. In order to avoid confusion between two different functions with the same name, a `funcname` argument can be supplied to `@persist`, which should be a string that uniquely identifies the function. This string could include a version number, author name, or anything else required to ensure uniqueness.

MongoDB cache. Support is provided for caching results in a MongoDB database, via the REST interface provided by Python's `Eve` package. If a `cache` argument is provided which starts with `mongodb://`, then it is interpreted as the address of a MongoDB server which can send and receive results for the function, and that server will be used instead of saving results locally. Such a server can be set up using the `mongodb_server/run.py` script distributed with `pypersist`.

Custom key function. Each entry in a function's cache is stored using a unique key based on the arguments supplied to the function; two sets of arguments should have the same key only if they produce the same output. By default, we use a tuple of the arguments, with their names, sorted alphabetically, and with any default arguments removed. This allows for equivalent calls such as `foo(x=3, y=5)` and `foo(y=5, x=3)` to be treated equally. However, the decorator takes an optional `key` argument, which should be a function that takes a list of arguments and produces a key based on them. A developer could thus choose to ignore arguments that control, for example, verbosity, or other options that do not affect the function's return value.

Custom hashing. When a result is stored in the cache, it is stored using a hash of its key. This allows a record to be looked up quickly, and perhaps removes the necessity of storing the keys at all. By default, a key is hashed using its SHA-256 encoding, which makes it extremely unlikely that a hash collision will ever be encountered. However, a custom hash function can be specified using a `hash` argument to the decorator, and in this case it will be used to produce a hash instead of the default method. If an injective hash function is chosen, then its inverse can be specified using the `unhash` argument; this allows hashes to be double-checked, and a list of previously-encountered keys to be produced.

Storing keys. By default, a key is not stored after it has been hashed, and correctness is assumed due to the vanishingly small probability of an SHA-256 hash collision. However, for complete correctness, the decorator takes an argument `storekey` which, if set to true, stores keys along with results, and checks them when looking up results, raising an error if a hash collision is detected. This also allows a user to iterate over the stored keys of a cache, as mentioned below.

Custom pickling. In order to store an object in a cache, it needs to be preserved on disk or in a database. For this purpose, we require sometimes complex objects to be *pickled* and *unpickled* – that is, converted to a string for storing, and converted back when retrieved later. The default methods use Python's `pickle` module (or, if appropriate, Sage's own pickling functions) and a base 64 encoding to produce strings that can be written without invisible or difficult-to-display characters. However, like much of `pypersist`'s functionality, custom `pickle` and `unpickle` functions can be specified that do this a different way. This can allow results to be stored in a human-readable way which can then be used outside Python, or even to be stored using a format such as OpenMath for use in a completely different computer system.

Manual cache interaction. It may be necessary at some time to modify a memoisation cache manually – perhaps to remove an inaccurate result, or to add a result that was found before

the cache was created. This can be done directly in `pypersist` – a memoised function `foo` has an attribute `foo.cache` which can be used much like a dictionary, reading, setting and deleting entries as desired. Furthermore, if `storekey` is set to `true`, or if an `unhash` method is provided, `foo.cache` is an iterable object with attributes `keys`, `values` and `items` that can be used in loops.

3.2. Software engineering

`pypersist` was written using modern open-source software technologies and practices, with an emphasis on clarity of understanding and ease of use. The report on OpenDreamKit D1.5 contains, in Section 4.3.2.1, a checklist of software engineering best practices. The package fulfills all the requirements in that list, as summarised in Table 2.

Version control	✓	Git
Tests	✓	<i>pytest</i> suite with 98% code coverage
Automated tests	✓	
Continuous integration	✓	Travis runs test suite for every commit
Automatic building of releases	✓	PyPI release script

TABLE 2. Software engineering good practice checklist for `pypersist`

The project was developed from the beginning using Git, and the full history is available in the repository. A test suite using *pytest* is included in the repository, and is run by Travis every time a commit or pull request is added on Github. The comprehensiveness of this suite is measured by *codecov*, and covers 98% of the code in the package, with the only untested lines being those that handle difficult-to-produce HTTP errors. The package is built for PyPI using Python’s well-established `setuptools` module, and several such releases have already been made.

3.3. Dissemination

The report on OpenDreamKit D1.5 also contains, in Section 4.3.2.2, a checklist of best practices for dissemination. The package also fulfills all of these requirements, as summarised in Table 3.

Development of `pypersist` was open from the start, available publicly on Github, including its full commit history. The issue tracker on its Github page has been used to track upcoming new features, as well as bugs and other problems. All documentation, tools, and setup are included directly in the Git repository, so that everything is kept in one place and can be tracked as a single unit.

The package’s documentation is mostly generated directly from the docstrings in its source files. This means that code is documented where it is written, making the code easier to understand and avoiding the need to duplicate documentation with extra comments. Numpy-style docstrings are used throughout – this widely used standard was chosen for its minimal syntax, which allows the strings to be easily read and understood in plaintext without any processing or compilation. A readme is included, written in Markdown, with a simple two-sentence introduction, a guide to installation, and a small number of examples showing how to get started. Autodoc and Sphinx are used to convert the docstrings and the readme, with very little additional documentation required, into a legible manual, which is hosted on *ReadTheDocs* and linked from the readme itself. This manual is updated automatically on each push to the repository. In this way, the documentation is accessible, clear, and maintainable.

The minimal examples in the readme are supplemented by a Jupyter notebook which is also included with the project. This notebook imports `pypersist` and demonstrates every feature

Host code publicly	✓	https://github.com/mtorpey/pypersist
Reference Manual (APIs)	✓	https://pypersist.readthedocs.io
Tutorial (for beginning users)	✓	Examples section in readme, and Binder demo with extensive annotations: <code>binder/demo.ipynb</code> (linked from readme and manual)
Examples	✓	
Live interactive online demos	✓	
Support mechanisms	✓	Github issues
How to cite the output?	✓	Explained in readme and manual
Installation mechanism	✓	Installation via <i>pip</i> , explained in readme and manual
High level description accessible to non-experts	✓	In readme, manual and Binder
URLs/Blog/etc to and from OpenDreamKit project	✓	Links to OpenDreamKit in readme, in manual, and on PyPI distribution page
Grant acknowledgements	✓	Acknowledged in readme and manual
Open Source license	✓	GPL v2 or later
Workshop	✓	Demo and discussion at <i>Free Computational Mathematics</i> conference, CIRM, Luminy, France, Feb 2019
Engaging users	✓	

TABLE 3. Dissemination good practice checklist for `pypersist`

available, with annotations explaining each example. The notebook can be loaded locally by anyone with a Jupyter installation, but for better accessibility it is also hosted on Binder, with its address linked at the bottom of the readme, as well as in a badge at the top. This demo loads the most recent version of `pypersist`, and therefore also acts as an additional test suite, since it requires the package to be in a working state in order to demonstrate its features. The outputs of the executable cells are not saved into the notebook – instead it is left to readers to execute the cells themselves, producing an interactive experience which may encourage the reader to experiment, and may lead to a better understanding of how the package works. This notebook was demonstrated at the *Free Computational Mathematics* conference held in CIRM, Luminy, France, in February 2019, prompting a discussion and feedback from users.

In order for `pypersist` to be used, it must be easy to install. The package is hosted on PyPI at <https://pypi.org/project/pypersist>, making installation as simple as typing `pip install pypersist` for any user connected to the internet. This installation method is explained in the project’s readme, and therefore also on the first page of its manual.

4. FUTURE DIRECTION

Although `pypersist` now has many features and is well-tested, it is still in development. It is hoped that as more developers begin to use it, they will provide feedback that will inform the development further, whether by revealing bugs, or by requesting new features. There are already several features that are planned, and work will continue on this project as time goes on. In this section we describe some aims for the future direction of Task 6.9, in `pypersist` and beyond.

4.1. Features

CouchDB. Support currently exists in `pypersist` for a MongoDB database backend. This works well, but there are certain features offered by the CouchDB system that might also be useful. CouchDB emphasises ease of setup, and allows information to be added and retrieved from the database via HTTP, with a human-readable web-based front-end that would allow human-readable results to be shared instantly on computation via a website. It is likely that

implementing this would require little deviation from the existing code for MongoDB, and could result in big improvements in ease of use, ease of setup, and interoperability.

Better metadata. `pypersist` has the capacity to store metadata, which may be useful for storing information about a given computation. However, no metadata is stored by default, and metadata is not validated in any way when a result is loaded from the cache. Some decision should be made on what metadata should always be stored, and functionality should be added that allows this metadata to be used where relevant, for example by allowing a cache to be filtered by date or user. Some useful fields could be where and when a result was originally computed, comments from the user or the author of the function, and information about the system that produced the result.

Provenance tracking. One use of metadata would be to record where a given result came from, allowing researchers to evaluate the trust they are willing to place in it. A limited form of this can be achieved by sharing results using a version control system such as Git, in which the timestamp and author of a commit give some useful information. But a more full-featured provenance-tracking system could be added in the future, recording the exact time and place that a computation was performed, as well as the user that called it, and version numbers for both `pypersist` and the function being memoised.

Permissions. In a multi-user memoisation cache, it would be useful to have explicit support for permissions handling. Most of the functionality for this could be delegated to the backend – for example, any database system has support for user permissions, and Git repositories can be set up to accept certain requests from only certain users – but it would be useful if `pypersist` handled this properly instead of simply raising an error when an interaction is unsuccessful.

Verbosity. Results in `pypersist` are stored and retrieved silently, and users are not made aware of its existence in any way except when errors are raised (for example due to a hash collision or HTTP error). It may be useful at times to display messages to the screen showing the progress of memoisation, so that interested users have a record of exactly what is being written and read at what time and in what location. Different levels of verbosity showing different levels of information may be useful.

GAP version. Though Deliverable 6.9 only requires a “shared persistent memoisation library for Python/Sage”, Task 6.9 also discusses a GAP version of this library. GAP would benefit from all the features included in `pypersist`, and a GAP version of this library would also be able to interface with the same cache as the Python version in certain circumstances, allowing results to be shared across different computer algebra systems as well as across different sessions. A prototype of this already exists in the form of GAP’s `Memoisation` package, which was developed in parallel with `pypersist`. However, this prototype is not yet stable or full-featured, and should be developed into a tool comparable to the Python version.

Sage integration. As shown in Table 1, there exist three different tools already in Sage for memoising data. Now that `pypersist` has overtaken `func_persist` in terms of features, it is possible that it could replace this tool entirely; with some additional work (support for compiled functions, optimization), it could replace `cached_function` and `cached_method` as well. With careful integration and testing to ensure that there were no regressions, `pypersist` could be imported and used instead of those tools, possibly with the addition of some Sage-specific

options that would allow it to be used as effectively as possible. However, `pypersist` should remain a generic Python package that can be used outside as well as inside Sage.

Search by property. The core behaviour of a memoisation system is to look up a single input and return a single output if one exists. However, once a cache with a number of results has been built up, a user may wish to search through it to find all input–output pairs that satisfy a particular property. For instance, if a boolean function called `is_prime` is memoised, and has been used to test the primality of several integers, a researcher who desires prime numbers might search through the cache for all inputs that returned `true`. This can be achieved using the current system, but some kind of indexing might be helpful, to allow answers to be returned more quickly.

4.2. Reporting

It is planned that `pypersist` version 1.0 will be released by the end of the OpenDreamKit project. The work done in preparation for that release, including the features mentioned above, may be summarised in a later report that would act as an addendum to this document.

Disclaimer: this report, together with its annexes and the reports for the earlier deliverables, is self contained for auditing and reviewing purposes. Hyperlinks to external resources are meant as a convenience for casual readers wishing to follow our progress; such links have been checked for correctness at the time of submission of the deliverable, but there is no guarantee implied that they will remain valid.