

The Hurst exponent can be calculated by rescaled range analysis (R/S analysis). For a time series, $X = X_1, X_2, \dots, X_n$, R/S analysis method is as follows:

- (1) Calculate mean value m .

$$m = \frac{1}{n} \sum_{i=1}^n X_i$$

- (2) Calculate mean adjusted series Y

$$Y_t = X_t - m, \quad t = 1, 2, \dots, n$$

- (3) Calculate cumulative deviate series Z

$$Z_t = \sum_{i=1}^t Y_i, \quad t = 1, 2, \dots, n$$

- (4) Calculate range series R

$$R_t = \max(Z_1, Z_2, \dots, Z_t) - \min(Z_1, Z_2, \dots, Z_t) \\ t = 1, 2, \dots, n$$

- (5) Calculate standard deviation series S

$$S_t = \sqrt{\frac{1}{t} \sum_{i=1}^t (X_i - u)^2} \quad t = 1, 2, \dots, n$$

Here u is the mean value from X_1 to X_t .

- (6) Calculate rescaled range series (R/S)

$$(R/S)_t = R_t/S_t \quad t = 1, 2, \dots, n$$

Note $(R/S)_t$ is averaged over the regions $[X_1, X_t]$, $[X_{t+1}, X_{2t}]$ until $[X_{(m-1)t+1}, X_{mt}]$ where $m = \text{floor}(n/t)$. In practice, to use all data for calculation, a value of t is chosen that is divisible by n .