### **Machine Learning & Application**

2021-2022

#### Projet Rubik's cube

Le projet porte sur un problème d'apprentissage supervisé. Le problème fait parti des données du challenge des données ENS et s'intitule "Solve 2x2x2 Rubik's cube" et est présenté par la société LumenAI. Une vidéo décrivant le problème se trouve sur le site du collège de France.

Les autres challenges sont aussi très intéressants, mais nécessitent plus de connaissances en machine learning (par exemple de l'apprentissage sur des séries temporelles, sur des images, des sons, du texte, etc...). D'où le choix de ce challenge dont les données sont très proches de problèmes sur lesquels on a travaillé.

La résolution d'un rubik's cube peut être vu comme un problème d'intelligence artificielle (par exemple en utilisant des techniques de recherches avec des heuristiques). On peut même étudier le graphe du jeu du point de vue de la théorie des graphes et découvrir qu'en fait il existe toujours un chemin relativement court à une solution.

#### ex dans la litérature:

- "The Diameter of the Rubik's Cube Group Is Twenty", *T. Rokicki, H. Kociemba, M. Davidson, and J. Dethridge*, SIAM Review, 2014, Vol. 56, No. 4: pp. 645-670.
- "Solving Rubik's Cube Using Graph Theory", Khemani C., Doshi J., Duseja J., Shah K., Udmale S., Sambhe V. (2019) in: Verma N., Ghosh A. (eds) Computational Intelligence: Theories, Applications and Future Directions - Volume I. Advances in Intelligent Systems and Computing, vol 798. Springer, Singapore.

Ici, on a une base de données qui contient la description de rubik's cubes ainsi que le nombre minimal de coups pour les résoudre. On ne sait pas comment les problèmes ont été générés (est-ce que cela entraine un biais dans les problèmes, est-ce que plusieurs problèmes similaires sont présents dans la base? (Ici par similaire, on pourrait peut être avoir deux problèmes qui apparaissent dans la base, mais en permuttant certaines couleurs, on aurait peut-être exactement le même problème!)). Cependant, on vous demande de constuire un modèle pour nous aider à prédire le nombre de coups minimal pour un problème donné. Ensuite, vous pourriez utiliser ce modèle dans un algorithme de recherche étudié en cours d'IA.

On peut le voir comme un problème de regression où il faut deviner le nombre minimal de coups pour résoudre le rubik's cube, ou comme un problème de classification où la classe d'un état du rubik's cube est le nombre minimal de coups pour le résoudre (donc on pourrait avoir au plus 19 classes). Toutes les méthodes que l'on a vu en cours peuvent s'appliquer.

#### Les données et le site du challenge

Le projet s'effectue en binôme. Vous devez ouvrir un compte pour le binôme sur le site du challenge, choisissez de participer seul (le binôme sera un seul participant au challenge), puis inscrivez-vous au challenge du cours *M1 MIAGE Dauphine - PSL - 2021-2022*.

Vous aurez accès à trois ensembles:

- x\_train qui contient la description de 1.837.079 différents rubik's cubes. Chaque rubik's cube est représenté par 25 attributs (lisez la description sur le site du challenge).
- y\_train qui contient le nombre minimal de coups pour résoudre chacun des 1.837.079 différents rubik's cubes. Ces données sont vos données d'entrainement.
- enfin x\_test qui contient la description de 1.837.080 nouveaux rubik's cubes. Vous ne connaissez pas le nombre minimal pour chacun de ces problèmes.

Pour participer aux challenges, il vous faudra uploader sur le site votre prédiction sur les rubik's cubes du fichier x\_test et le site du challenge vous donnera un score. Pour ce score, le site utilise l'erreur moyenne absolue: pour les n=1.837.080 exemples du fichier test, on fait la moyenne entre le vrai nombre minimal de coups  $y_i$  et votre prédiction  $z_i$ :

$$rac{\sum_{i=1}^{n}|y_i-z_i|}{n}$$

Malheureusement (pour vous), le site ne vous donnera pas plus d'information que votre score, vous ne pourrez pas savoir quelles sont vos bonnes prédictions et quelles sont vos erreurs. Pire, le site vous permettra d'uploader une prédiction que deux fois par jour!

#### Soumission et rappot

Un des membres du binôme devra remplir le formulaire Forms de l'équipe Teams du cours (onglet General) pour enregistrer les membres du binôme et le login du binôme qui utilisé sur le site du challenge ENS. Avant le **jeudi 2 décembre à 12h** vous devez 1) avoir créé votre compte pour le binôme et inscrit le binôme sur le challenge du cours, et 2) rempli les informations sur le formulaire Forms.

Vous pouvez faire le projet seul, mais vous serez évalué comme un binôme. Si vous tenez absolument à former un trinôme, contactez moi par email, mais sachez que dès lors, les attentes seront plus élevées.

Le deadline pour le projet sera le **dimanche 20 décembre 23:59** Vous devrez à ce moment là avoir fait trois choses:

- avoir rendu un rapport
- avoir rendu un notebook jupyter ou collab contenant le code pour générer votre solution
- avoir soumis une solution sur le site du challenge ENS.

Le notebook et le rapport seront à soumettre sous myCourse.

Le rapport est un document **pdf** et devra être un document structuré qui explique vos choix, explique votre solution et donne votre résultat. Ne présentez ni le cours, ni le contexte, seul

votre travail est important. Le rapport est de **6** pages maximum au format A4 (sans utiliser une taille de police inférieure strictement à 12). Vous pouvez ajouter une annexe à ce rapport (au format pdf ou sous la forme d'un notebook jupyter), étant entendu que le lecteur n'est pas obligé de lire l'annexe. Votre mission est de proposer un modèle de prédiction pour ce problème, votre rapport doit justifier comment vous avez répondu (complètement ou pas) à cette mission (par exemple, vous pouvez décrire ce que vous avez essayé, ce qui a marché ou non, pourquoi vous avez essayé autre chose...). Une autre façon de décrire ce qu'on attend du rapport est la suivante: votre manageur a donné à plusieurs équipes la même tâche d'apprentissage supervisé. Vous devez lui présenter dans ce rapport des arguments qui justifient la qualité de votre approche et de vos résultats. Votre manageur connait le problème, mais n'est pas forcément un expert du domaine. A vous de le convaincre d'utiliser votre solution! (attention, si vous connaissez aussi les limitations de votre solution, il est bon de les exposer aussi!).

L'évaluation portera sur la qualité de votre analyse, même si vos résultats sont peu concluant. Pour caricaturer, un modèle qui gagnerait la compétition sans pouvoir expliquer ce qu'il a fait n'aura pas une bonne note pour le projet du cours (mais bravo, il a gagné la compétition!). Autre caricature, un projet qui applique un seul algorithme et conclue que ça ne fonctionne pas bien n'aura pas non plus une bonne note.

Une soutenance sera organisée lors de la première semaine de cours (après les examens). Elle permettra de compléter l'évaluation et de vous donner un retour sur votre travail. Cette soutenance ne demande aucune préparation de votre part. Elle durera une douzaine/quinzaine de minutes par groupe. La soutenance consistera en un échange au sujet de vos résultats et votre rapport. Si la soutenance fait apparaître qu'un des membres n'a pas beaucoup contribué, sa note pourra être revue à la baisse. Egalement, on pourra vous demander de montrer le code et de fournir les résultats que vous avez obtenu lors des exercices d'implémentation des TDs.

Ce projet compte pour 40% de la note de l'UE. Il est donc souhaitable que la note corresponde au travail de votre groupe, et non aux conseils d'autres groupes, d'autres étudiants ou d'internet. Si vous utilisez des sources (articles de recherche, posts sur internet, etc...), vous devez mentionnez vos sources dans le rapport (sinon, cela s'appelle du plagiat, et cela peut être puni par un conseil de discipline).

Les quelques lignes de code ci-dessous lisent simplement les fichiers sources et affiche la taille des données.

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt

dfX = pd.read_csv("train_input.csv",index_col=0)
dfY = pd.read_csv("train_output.csv",index_col=0)
X = dfX.to_numpy()
y = dfY['distance'].values
print("taille des données:")
print("X:", X.shape)
print("y:", np.size(y))
```

```
dfT = pd.read_csv("test_input.csv",index_col=0)
           Xtest = dfT.to_numpy()
           print("test:", Xtest.shape)
          /Users/salimzerhouni/opt/anaconda3/lib/python3.9/site-packages/numpy/lib/array
          setops.py:583: FutureWarning: elementwise comparison failed; returning scalar
          instead, but in the future will perform elementwise comparison
            mask \mid = (ar1 == a)
          taille des données:
          X: (1837079, 24)
          y: 1837079
          test: (1837080, 24)
In [264...
           print("Il y a ", X.size, " observations avec ", X[0].size, " attributs")
          Il y a 44089896 observations avec 24 attributs
In [265...
           dfX
Out [265...
                    pos0 pos1 pos2 pos3 pos4 pos5 pos6 pos7 pos8 pos9 ... pos14 pos15
                ID
                 0
                       4
                             1
                                    1
                                          1
                                                6
                                                      2
                                                            6
                                                                         5
                                                                                          4
                                                                                                 4
                 1
                       6
                             5
                                   2
                                          1
                                                2
                                                      2
                                                            6
                                                                  3
                                                                               4
                                                                                          4
                                                                                                 1
                 2
                       5
                             3
                                   3
                                          2
                                                3
                                                      1
                                                            6
                                                                  5
                                                                         1
                                                                               1
                                                                                          4
                                                                                                 6
                 3
                       5
                             5
                                   4
                                          1
                                                2
                                                                         2
                                                                               2
                                                                                                 4
                                                      1
                                                            6
                                                                   1
                                                                                          4
                 4
                             2
                                                1
                                                                        3
                                                                                                 2
                       4
                                   1
                                          5
                                                      3
                                                            6
                                                                  6
                                                                               3
                                                                                          4
           1837074
                       2
                             1
                                   3
                                          3
                                                5
                                                      3
                                                            6
                                                                  6
                                                                         1
                                                                               5
                                                                                          4
                                                                                                 3
           1837075
                       2
                             3
                                   3
                                          5
                                                6
                                                      4
                                                            6
                                                                   1
                                                                        3
                                                                               1
                                                                                          4
                                                                                                 5
           1837076
                       3
                             3
                                   3
                                          2
                                                2
                                                      4
                                                            6
                                                                  6
                                                                               4
                                                                                                 3
                                                                         1
                                                                                          4
           1837077
                       5
                             3
                                   5
                                          1
                                                5
                                                      3
                                                            6
                                                                  3
                                                                        6
                                                                               4
                                                                                          4
                                                                                                 4
           1837078
                                                1
                                                      5
                                                            6
                                                                               2 ...
                                                                                          4
                                                                                                 1
          1837079 rows × 24 columns
In [266...
           dfY
Out [266...
                    distance
                ID
                 0
                          11
                 1
                          11
                 2
                          11
                 3
                          9
                 4
                          12
                          ...
                 ...
```

#### distance

| ID      |    |
|---------|----|
| 1837075 | 9  |
| 1837076 | 12 |
| 1837077 | 11 |
| 1837078 | 11 |

1837079 rows × 1 columns

### Première approche

```
In [276...
          #DecisionTree
          from sklearn.tree import DecisionTreeClassifier
          from math import sqrt
          from sklearn.metrics import precision score
          from sklearn import tree
          from sklearn.model_selection import train_test_split
          from sklearn.metrics import mean_absolute_error
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.10)
          dtree = DecisionTreeClassifier(criterion="gini", max depth=3)
          dtree.fit(X train, y train)
          ydt = dtree.predict(X test)
          mean_absolute_error(y_test,ydt)
         0.857992030831537
Out [276...
In [277...
          np.bincount(ydt)
                              0,
                                                        0,
                                                                0,
                                                                        0,
                                                                                 0,
                      0,
                                       0,
         array([
Out[277...
                                       0, 1837081)
                              0,
In [85]:
          dfY.value_counts()
         distance
Out[85]:
         11
                      675426
         10
                      465294
         12
                      391268
         9
                      180254
         8
                       57074
         13
                       45140
                       16529
         6
                        4485
         5
                        1128
                         267
         14
                         138
                          60
         2
                          13
                           3
         dtype: int64
 In [7]:
          from sklearn.naive bayes import GaussianNB
          X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.10)
          gnb = GaussianNB()
```

```
gnb.fit(X_train,y_train)
ydt2 = gnb.predict(X_test)
mean_absolute_error(y_test,ydt2)
```

1.0050188342369413

#### Des cubes similaires?

Programme de rotation du cube

```
In [9]:
          import itertools
          Xn = []
          for i in range(6):
              for j in range(i+1,6):
                  for k in range(1,4):
                      Xn1 = []
                      Xn1.append(np.roll(X[0,:4*i],4*k).tolist())
                      Xn1.append(np.roll(X[0,4*i:4*(i+1)],1*k).tolist())
                      Xn1.append(np.roll(X[0,4*(i+1):4*j],4*k).tolist())
                      Xn1.append(np.roll(X[0,4*j:4*(j+1)],1*k).tolist())
                      Xn1.append(np.roll(X[0,4*(j+1):],4*k).tolist())
                  flat list = itertools.chain(*Xn1)
                  Xn.append(list(flat list))
          Xn
         [[1, 1, 1, 4, 2, 6, 6, 6, 5, 6, 4, 4, 1, 3, 3, 5, 2, 3, 5, 3, 5, 4, 2, 2],
          [1, 1, 1, 4, 6, 2, 6, 6, 4, 2, 2, 5, 5, 6, 4, 4, 1, 3, 3, 5,
                                                                        2, 3, 5, 31,
          [1, 1, 1, 4, 5, 4, 2, 2, 6, 2, 6, 6, 6, 4, 4, 5, 2, 3, 5, 3, 1, 3, 3, 5],
          [1, 1, 1, 4, 6, 2, 6, 6, 5, 4, 2, 2, 5, 6, 4, 4, 3, 3, 5, 1, 2, 3, 5, 3],
          [1, 1, 1, 4, 5, 4, 2, 2, 5, 6, 4, 4, 1, 3, 3, 5, 6, 2, 6, 6, 3, 5, 3, 2]
          [4, 1, 1, 1, 2, 6, 6, 6, 4, 2, 2, 5, 5, 6, 4,
                                                         4, 1, 3, 3, 5, 2, 3, 5, 31,
          [4, 1, 1, 1, 2, 6, 6, 6, 5, 4, 2, 2, 6, 4, 4,
                                                         5, 2, 3, 5, 3, 1,
                                                                           3, 3, 51,
          [4, 1, 1, 1, 2, 6, 6, 6, 5, 6, 4, 4, 5, 4, 2, 2, 3, 3, 5, 1, 2, 3, 5, 3],
          [4, 1, 1, 1, 2, 6, 6, 6, 5, 4, 2, 2, 5, 6, 4, 4, 1, 3, 3, 5, 3, 5, 3, 2],
          [6, 2, 6, 6, 4, 1, 1, 1, 4, 2, 2, 5, 6, 4, 4, 5, 2, 3, 5, 3, 1, 3, 3, 5],
          [6, 2, 6, 6, 4, 1, 1, 1, 4, 2, 2, 5, 5, 6, 4, 4, 3, 3, 5, 1, 2, 3, 5, 3],
          [6, 2, 6, 6, 4, 1, 1, 1, 4, 2, 2, 5, 1, 3, 3, 5, 5, 6, 4, 4, 3, 5, 3, 2],
          [4, 1, 1, 1, 6, 2, 6, 6, 5, 4, 2, 2, 6, 4, 4, 5, 3, 3, 5, 1, 2, 3, 5, 3],
          [4, 1, 1, 1, 6, 2, 6, 6, 5, 4, 2, 2, 6, 4, 4, 5, 1, 3, 3, 5, 3, 5, 3, 2]
          [6, 2, 6, 6, 5, 4, 2, 2, 5, 6, 4, 4, 4, 1, 1, 1, 1, 3, 3, 5, 1, 3, 5, 3, 2]]
In [10]:
          for i in range(len(Xn)):
              if Xn[i] in X.tolist():
                  print("YES")
```

Pas de "faux" doublons.

#### Réarrangement des combinaisons

print(X[365030],X[411427],X[1266419])

np.split(X[1266419],6)

```
[5 1 6 3 5 1 6 3 2 4 4 2 2 4 4 2 1 3 3 1 6 5 5 6] [1 1 6 6 1 1 6 6 3 5 4 2 3 5 4 2 4 4 3 3 2 2 5 5] [2 2 4 4 1 1 6 6 6 1 1 6 2 4 4 2 3 3 3 3 5 5 5 5]

Out[12]:

Out[12]:

array([2, 2, 4, 4]),
    array([1, 1, 6, 6]),
    array([6, 1, 1, 6]),
    array([2, 4, 4, 2]),
    array([3, 3, 3, 3]),
    array([5, 5, 5, 5])]
```

#### Fonction de réindexation des cubes

```
In [3]:
         def faceCube(dfX):
             df = pd.DataFrame()
             df['pos0'] = dfX['pos18']
             df['pos1'] = dfX['pos17']
             df['pos2'] = dfX['pos19']
             df['pos3'] = dfX['pos16']
             df['pos4'] = dfX['pos21']
             df['pos5'] = dfX['pos22']
             df['pos6'] = dfX['pos20']
             df['pos7'] = dfX['pos23']
             df['pos8'] = dfX['pos1']
             df['pos9'] = dfX['pos5']
             df['pos10'] = dfX['pos0']
             df['pos11'] = dfX['pos4']
             df['pos12'] = dfX['pos2']
             df['pos13'] = dfX['pos6']
             df['pos14'] = dfX['pos3']
             df['pos15'] = dfX['pos7']
             df['pos16'] = dfX['pos14']
             df['pos17'] = dfX['pos13']
             df['pos18'] = dfX['pos10']
             df['pos19'] = dfX['pos9']
             df['pos20'] = dfX['pos11']
             df['pos21'] = dfX['pos8']
             df['pos22'] = dfX['pos15']
             df['pos23'] = dfX['pos12']
             return df
```

```
In [569...
    dfX2 = faceCube(dfX2,dfX)
    dfX2
```

| Out[569 |         | pos0 | pos1 | pos2 | pos3 | pos4 | pos5 | pos6 | pos7 | pos8 | pos9 | ••• | pos14 | pos15 |
|---------|---------|------|------|------|------|------|------|------|------|------|------|-----|-------|-------|
|         | ID      |      |      |      |      |      |      |      |      |      |      |     |       |       |
|         | 0       | 3    | 3    | 5    | 1    | 3    | 5    | 2    | 3    | 1    | 2    |     | 1     | 6     |
|         | 1       | 5    | 1    | 3    | 3    | 3    | 5    | 5    | 2    | 5    | 2    | ••• | 1     | 3     |
|         | 2       | 4    | 4    | 3    | 4    | 2    | 5    | 2    | 2    | 3    | 1    | ••• | 2     | 5     |
|         | 3       | 6    | 6    | 3    | 1    | 3    | 5    | 6    | 5    | 5    | 1    |     | 1     | 1     |
|         | 4       | 2    | 6    | 1    | 6    | 1    | 5    | 2    | 5    | 2    | 3    |     | 5     | 6     |
|         | •••     | •••  | •••  | •••  | •••  | •••  | •••  | •••  | •••  | •••  | •••  |     | •••   | •••   |
|         | 1837074 | 2    | 4    | 6    | 5    | 1    | 5    | 6    | 2    | 1    | 3    |     | 3     | 6     |
|         | 1837075 | 6    | 4    | 1    | 1    | 6    | 5    | 2    | 2    | 3    | 4    |     | 5     | 1     |
|         | 1837076 | 1    | 6    | 5    | 2    | 1    | 5    | 1    | 2    | 3    | 4    |     | 2     | 6     |
|         | 1837077 | 4    | 6    | 2    | 2    | 6    | 5    | 2    | 1    | 3    | 3    |     | 1     | 3     |

```
        pos0
        pos1
        pos2
        pos3
        pos4
        pos5
        pos6
        pos7
        pos8
        pos9
        ...
        pos14
        pos15

        1837078
        1
        5
        6
        4
        2
        5
        2
        3
        1
        5
        ...
        2
        4

        1837079 rows × 24 columns
```

```
In [286... x2 = dfx2.to_numpy()
```

Ajout des attributs "nombre de couleur par face"

```
In [90]:
    f=[]
    b=[]
    l=[]
    r=[]
    u=[]
    d=[]

for i in range(len(dfX2['pos0'])):

    f.append(len(np.unique([dfX2['pos0'][i],dfX2['pos1'][i],dfX2['pos2'][i],dfX2['pos6'][i],dfX2['pos6'][i],dfX2['pos6'][i],dfX2['pos6'][i],dfX2['pos6'][i],dfX2['pos8'][i],dfX2['pos8'][i],dfX2['pos1'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX2['pos10'][i],dfX
```

```
In [178... dfx2['f'] = f dfx2['b'] = b dfx2['l'] = l dfx2['r'] = r dfx2['u'] = u dfx2['d'] = d dfx2
```

| Out[178 |         | pos0 | pos1 | pos2 | pos3 | pos4 | pos5 | pos6 | pos7 | pos8 | pos9 | ••• | pos20 | pos21 |
|---------|---------|------|------|------|------|------|------|------|------|------|------|-----|-------|-------|
|         | 0       | 3    | 3    | 5    | 1    | 3    | 5    | 2    | 3    | 1    | 2    |     | 2     | 5     |
|         | 1       | 5    | 1    | 3    | 3    | 3    | 5    | 5    | 2    | 5    | 2    |     | 4     | 4     |
|         | 2       | 4    | 4    | 3    | 4    | 2    | 5    | 2    | 2    | 3    | 1    |     | 1     | 1     |
|         | 3       | 6    | 6    | 3    | 1    | 3    | 5    | 6    | 5    | 5    | 1    |     | 4     | 2     |
|         | 4       | 2    | 6    | 1    | 6    | 1    | 5    | 2    | 5    | 2    | 3    |     | 4     | 3     |
|         | •••     |      | •••  | •••  | •••  | •••  | •••  |      | •••  | •••  |      |     | •••   | •••   |
|         | 1837074 | 2    | 4    | 6    | 5    | 1    | 5    | 6    | 2    | 1    | 3    |     | 4     | 1     |
|         | 1837075 | 6    | 4    | 1    | 1    | 6    | 5    | 2    | 2    | 3    | 4    |     | 4     | 3     |
|         | 1837076 | 1    | 6    | 5    | 2    | 1    | 5    | 1    | 2    | 3    | 4    |     | 6     | 1     |
|         | 1837077 | 4    | 6    | 2    | 2    | 6    | 5    | 2    | 1    | 3    | 3    |     | 3     | 6     |
|         | 1837078 | 1    | 5    | 6    | 4    | 2    | 5    | 2    | 3    | 1    | 5    |     | 3     | 6     |
|         |         |      |      |      |      |      |      |      |      |      |      |     |       |       |

1837079 rows × 30 columns

```
somme = []
for i in range(len(dfX2['pos0'])):
    s = dfX2['f'][i] + dfX2['b'][i] + dfX2['l'][i] + dfX2['r'][i] + dfX2['u']
    somme.append(s)
dfX2['somme'] = somme
dfX2
```

Out[181...

|         | pos0 | pos1 | pos2 | pos3 | pos4 | pos5 | pos6 | pos7 | pos8 | pos9 | ••• | pos21 | pos22 |
|---------|------|------|------|------|------|------|------|------|------|------|-----|-------|-------|
| 0       | 3    | 3    | 5    | 1    | 3    | 5    | 2    | 3    | 1    | 2    |     | 5     | 4     |
| 1       | 5    | 1    | 3    | 3    | 3    | 5    | 5    | 2    | 5    | 2    |     | 4     | 1     |
| 2       | 4    | 4    | 3    | 4    | 2    | 5    | 2    | 2    | 3    | 1    |     | 1     | 6     |
| 3       | 6    | 6    | 3    | 1    | 3    | 5    | 6    | 5    | 5    | 1    |     | 2     | 4     |
| 4       | 2    | 6    | 1    | 6    | 1    | 5    | 2    | 5    | 2    | 3    |     | 3     | 2     |
| •••     | •••  | •••  | •••  |      | •••  | •••  |      | •••  |      | •••  |     |       | •••   |
| 1837074 | 2    | 4    | 6    | 5    | 1    | 5    | 6    | 2    | 1    | 3    |     | 1     | 3     |
| 1837075 | 6    | 4    | 1    | 1    | 6    | 5    | 2    | 2    | 3    | 4    |     | 3     | 5     |
| 1837076 | 1    | 6    | 5    | 2    | 1    | 5    | 1    | 2    | 3    | 4    |     | 1     | 3     |
| 1837077 | 4    | 6    | 2    | 2    | 6    | 5    | 2    | 1    | 3    | 3    |     | 6     | 4     |
| 1837078 | 1    | 5    | 6    | 4    | 2    | 5    | 2    | 3    | 1    | 5    |     | 6     | 1     |

1837079 rows × 31 columns

```
In [128...
```

```
#DecisionTree
from sklearn.tree import DecisionTreeClassifier
from math import sqrt
from sklearn.metrics import precision_score
from sklearn.metrics import tree
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_absolute_error
X2_train, X2_test, y_train, y_test = train_test_split(X2, y, test_size=0.10)
dtree = DecisionTreeClassifier(criterion="gini", max_depth=3)
dtree.fit(X2_train, y_train)
ydt = dtree.predict(X2_test)
mean_absolute_error(y_test,ydt)
```

Out[128...

0.8587323360985912

```
In [28]:
```

```
#RandomForest
from sklearn.ensemble import RandomForestClassifier
X2_train, X2_test, y_train, y_test = train_test_split(X2, y, test_size=0.10)
dtree = RandomForestClassifier(max_depth=10,verbose=3)
dtree.fit(X2_train, y_train)
ydt = dtree.predict(X2_test)
mean_absolute_error(y_test,ydt)
```

```
[Parallel(n_jobs=1)]: Using backend SequentialBackend with 1 concurrent worker
s.
building tree 1 of 100

[Parallel(n_jobs=1)]: Done 1 out of 1 | elapsed: 1.3s remaining: 0.0
s
building tree 2 of 100

[Parallel(n jobs=1)]: Done 2 out of 2 | elapsed: 2.7s remaining: 0.0
```

building tree 3 of 100 building tree 4 of 100 building tree 5 of 100 building tree 6 of 100 building tree 7 of 100 building tree 8 of 100 building tree 9 of 100 building tree 10 of 100 building tree 11 of 100 building tree 12 of 100 building tree 13 of 100 building tree 14 of 100 building tree 15 of 100 building tree 16 of 100 building tree 17 of 100 building tree 18 of 100 building tree 19 of 100 building tree 20 of 100 building tree 21 of 100 building tree 22 of 100 building tree 23 of 100 building tree 24 of 100 building tree 25 of 100 building tree 26 of 100 building tree 27 of 100 building tree 28 of 100 building tree 29 of 100 building tree 30 of 100 building tree 31 of 100 building tree 32 of 100 building tree 33 of 100 building tree 34 of 100 building tree 35 of 100 building tree 36 of 100 building tree 37 of 100 building tree 38 of 100 building tree 39 of 100 building tree 40 of 100 building tree 41 of 100 building tree 42 of 100 building tree 43 of 100 building tree 44 of 100 building tree 45 of 100 building tree 46 of 100 building tree 47 of 100 building tree 48 of 100 building tree 49 of 100 building tree 50 of 100 building tree 51 of 100 building tree 52 of 100 building tree 53 of 100 building tree 54 of 100 building tree 55 of 100 building tree 56 of 100 building tree 57 of 100 building tree 58 of 100 building tree 59 of 100 building tree 60 of 100 building tree 61 of 100 building tree 62 of 100 building tree 63 of 100 building tree 64 of 100 building tree 65 of 100

```
building tree 66 of 100
         building tree 67 of 100
         building tree 68 of 100
         building tree 69 of 100
         building tree 70 of 100
         building tree 71 of 100
         building tree 72 of 100
         building tree 73 of 100
         building tree 74 of 100
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         building tree 93 of 100
         building tree 94 of 100
         building tree 95 of 100
         building tree 96 of 100
         building tree 97 of 100
         building tree 98 of 100
         building tree 99 of 100
         building tree 100 of 100
         [Parallel(n jobs=1)]: Done 100 out of 100 | elapsed: 2.2min finished
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent worker
                                                  1 | elapsed:
         [Parallel(n jobs=1)]: Done
                                      1 out of
                                                                  0.0s remaining:
                                                                                     0.0
                                      2 out of
                                                  2 | elapsed:
         [Parallel(n jobs=1)]: Done
                                                                  0.0s remaining:
                                                                                     0.0
         [Parallel(n jobs=1)]: Done 100 out of 100 | elapsed:
                                                                  1.8s finished
         0.8584873821499336
Out[28]:
```

### Regroupement des colonnes

```
In [199...] X2 = dfX2.to numpy()
          #RandomForest
          from sklearn.ensemble import RandomForestClassifier
          X2 train, X2 test, z train, z test = train test split(X2, z, test size=0.30)
          dtree = RandomForestClassifier(max depth=10,verbose=3, n jobs=50)
          dtree.fit(X2_train, z_train)
          zdt = dtree.predict(X2 test)
          mean absolute error(z test,zdt)
         [Parallel(n_jobs=50)]: Using backend ThreadingBackend with 50 concurrent worke
         rs.
         building tree 1 of 100
         building tree 2 of 100
         building tree 3 of 100building tree 4 of 100building tree 5 of 100
         building tree 6 of 100
         building tree 7 of 100
         building tree 8 of 100
         building tree 9 of 100
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         building tree 41 of 100building tree 42 of 100
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         building tree 46 of 100building tree 48 of 100
         building tree 49 of 100
         building tree 50 of 100
         building tree 51 of 100
```

building tree 52 of 100

```
building tree 53 of 100
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         building tree 59 of 100building tree 60 of 100
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         building tree 67 of 100building tree 68 of 100building tree 69 of 100
         building tree 70 of 100
         building tree 71 of 100building tree 72 of 100building tree 73 of 100
         building tree 74 of 100
         building tree 75 of 100building tree 76 of 100building tree 77 of 100
         building tree 78 of 100
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         building tree 80 of 100building tree 81 of 100
         building tree 82 of 100
         building tree 83 of 100
         building tree 84 of 100building tree 85 of 100
         building tree 86 of 100
         building tree 87 of 100
         building tree 88 of 100
         building tree 89 of 100
                                                                 13.3s remaining:
         [Parallel(n jobs=50)]: Done 35 out of 100 | elapsed:
                                                                                     24.
         building tree 90 of 100
         building tree 91 of 100
         building tree 92 of 100
         building tree 93 of 100
         building tree 94 of 100
         building tree 95 of 100
         building tree 96 of 100
         building tree 97 of 100
         building tree 98 of 100
         building tree 99 of 100
         building tree 100 of 100
         [Parallel(n jobs=50)]: Done 69 out of 100 | elapsed:
                                                                 22.9s remaining:
                                                                                     10.
         [Parallel(n jobs=50)]: Done 100 out of 100 | elapsed:
                                                                  23.8s finished
         [Parallel(n jobs=50)]: Using backend ThreadingBackend with 50 concurrent worke
         [Parallel(n jobs=50)]: Done 35 out of 100 | elapsed:
                                                                 0.5s remaining:
                                                                                      0.
         95
         [Parallel(n jobs=50)]: Done 69 out of 100 | elapsed: 0.7s remaining:
                                                                                      0.
         [Parallel(n_jobs=50)]: Done 100 out of 100 | elapsed:
                                                                 0.8s finished
         0.6641028153373832
Out[199...
```

#DecisionTree

```
X2_train, X2_test, z_train, z_test = train_test_split(X2, z, test_size=0.30)
          dtree = DecisionTreeClassifier(criterion="gini", max depth=5)
          dtree.fit(X2 train, z train)
          zdt = dtree.predict(X2 test)
          mean absolute error(z test,zdt)
          0.6185431953607536
Out [196...
In [200...
          np.bincount(zdt)
                    607, 441847, 108670])
          array([
Out [200...
In [198...
          from sklearn.metrics import plot confusion matrix
          plot confusion matrix(dtree, X2 test, z test)
          <sklearn.metrics. plot.confusion matrix.ConfusionMatrixDisplay at 0x7f9b419774</pre>
Out [198...
          00>
                                                200000
                 169
                          130319
                                     783
            0
                                                175000
                                                150000
                                                125000
          Frue label
            1
                  79
                          210032
                                     611
                                                - 100000
                                                75000
                                                50000
                 157
                          208005
                                     969
            2
                                                25000
                  0
                                      2
                        Predicted label
In [51]:
          from sklearn.neural network import MLPClassifier
          clf = MLPClassifier(hidden_layer_sizes=50,random_state=1, max_iter=20,solver=
          clf.fit(X train, z train)
          Iteration 1, loss = 0.69631506
          Iteration 2, loss = 0.69392003
          Iteration 3, loss = 0.69373080
          Iteration 4, loss = 0.69365517
          Iteration 5, loss = 0.69357592
          Iteration 6, loss = 0.69353350
          Iteration 7, loss = 0.69345259
          Iteration 8, loss = 0.69339986
          Iteration 9, loss = 0.69336452
          Iteration 10, loss = 0.69331956
          Iteration 11, loss = 0.69331658
          Iteration 12, loss = 0.69328718
          Iteration 13, loss = 0.69325883
          Iteration 14, loss = 0.69325440
          Training loss did not improve more than tol=0.000100 for 10 consecutive epoch
          s. Stopping.
          MLPClassifier(hidden layer sizes=50, max iter=20, random state=1, solver='sg
Out [51]:
```

In [52]:

verbose=10)

```
zdt = clf.predict(X2_test)
mean_absolute_error(z_test,zdt)

Out[52]:

In [53]:
    np.bincount(zdt)

Out[53]:
    array([ 51208, 132500])
```

## Modélisation des données sous la forme de coins

Les 6 cellules qui suivent sont un simple tatonnement pour pouvoir faire la fonction cornerCube() expliquée plus tard.

```
In [283...
          print(X2[365030], X2[411427], X2[1266419])
          np.split(X2[411427],6)
         [3 3 1 1 5 5 6 6 1 1 5 5 6 6 3 3 4 4 4 4 2 2 2 2] [3 4 3 4 2 5 2 5 1 1 1 1 6 6
         6 6 4 5 4 5 2 3 2 3 3 3 3 5 5 5 5 5 2 1 2 1 4 6 4 6 4 4 1 1 6 6 2 2 3
Out[283... [array([3, 4, 3, 4]),
          array([2, 5, 2, 5]),
          array([1, 1, 1, 1]),
          array([6, 6, 6, 6]),
          array([4, 5, 4, 5]),
          array([2, 3, 2, 3])]
 In []:
          #[(5'5',6'13',4'16'),(1'9',2'4',5'17'),(6'12',3'0',4'18'),(4'1',1'8',5'19'),(
In [284...
          np.split(X2[365030],6)
Out[284... [array([3, 3, 1, 1]),
          array([5, 5, 6, 6]),
          array([1, 1, 5, 5]),
          array([6, 6, 3, 3]),
          array([4, 4, 4, 4]),
          array([2, 2, 2, 2])]
 In []:
          #[(5'5',6'13',4'16'),(1'9',5'4',4'17'),(6'12',3'0',4'18'),(3'1',1'8',4'19'),(
In [314...
          np.split(X2[1266419],6)
Out[314... [array([3, 3, 3, 3]),
          array([5, 5, 5, 5]),
          array([2, 1, 2, 1]),
          array([4, 6, 4, 6]),
          array([4, 4, 1, 1]),
          array([6, 6, 2, 2])]
 In [ ]:
          #[(5'5',6'13',4'16'),(1'9',5'4',4'17'),(4'12',3'0',1'18'),(3'1',2'8',1'19'),(
In [52]:
          def cornerCube(dfX):
              df = pd.DataFrame()
              df1 = faceCube(dfX)
```

```
df['corner0'] = df1[['pos5', 'pos13', 'pos16']].apply(tuple, axis=1)
             df['corner1'] = df1[['pos9','pos4','pos17']].apply(tuple, axis=1)
             df['corner2'] = df1[['pos1','pos8','pos19']].apply(tuple, axis=1)
             df['corner3'] = df1[['pos12','pos0','pos18']].apply(tuple, axis=1)
             df['corner4'] = df1[['pos10','pos3','pos21']].apply(tuple, axis=1)
             df['corner5'] = df1[['pos2', 'pos14', 'pos20']].apply(tuple, axis=1)
             df['corner6'] = df1[['pos15','pos7','pos22']].apply(tuple, axis=1)
             df['corner7'] = df1[['pos6','pos11','pos23']].apply(tuple, axis=1)
             return df
In [5]:
         dfX3 = cornerCube(dfX)
```

```
dfX3
```

```
Out[5]:
                       corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7
                  ID
                   0 (5, 6, 4) (2, 3, 6) (3, 1, 4) (1, 3, 2) (4, 1, 5) (5, 1, 2) (6, 3, 4) (2, 6, 5)
                   1 (5, 6, 4) (2, 3, 6)
                                           (1, 5, 4)
                                                      (2, 5, 1)
                                                                (6, 3, 4)
                                                                           (3, 1, 4)
                                                                                     (3, 2, 1) (5, 2, 6)
                      (5, 6, 4)
                                (1, 2, 5)
                                           (4, 3, 1)
                                                      (3, 4, 6)
                                                                (5, 4, 1)
                                                                           (3, 2, 1)
                                                                                     (5, 2, 6) (2, 3, 6)
                       (5, 6, 4) (1, 3, 2)
                                           (6, 5, 2)
                                                      (4, 6, 3)
                                                                (5, 1, 2)
                                                                           (3, 1, 4)
                                                                                     (1, 5, 4) (6, 2, 3)
                      (5, 6, 4)
                                (3, 1, 4)
                                           (6, 2, 3)
                                                      (1, 2, 5)
                                                                (4, 6, 3)
                                                                           (1, 5, 4)
                                                                                     (6, 5, 2) (2, 1, 3)
                            ...
                                                                                           ...
                                      ...
                                                 ...
                                                           ...
                                                                      ...
                                                                                ...
                                                                                                     ...
           1837074
                      (5, 6, 4) (3, 1, 4)
                                           (4, 1, 5)
                                                      (3, 2, 1)
                                                                (2, 5, 1)
                                                                          (6, 3, 4)
                                                                                    (6, 2, 3) (6, 5, 2)
           1837075
                      (5, 6, 4) (4, 6, 3)
                                           (4, 3, 1)
                                                      (3, 6, 2)
                                                                (2, 1, 3)
                                                                          (1, 5, 4)
                                                                                     (1, 2, 5) (2, 6, 5)
           1837076 (5, 6, 4) (4, 1, 5)
                                          (6, 3, 4)
                                                      (3, 1, 4) (3, 2, 1) (5, 2, 6) (6, 2, 3) (1, 2, 5)
           1837077 (5, 6, 4) (3, 6, 2)
                                           (6, 3, 4)
                                                      (5, 4, 1) (5, 2, 6) (2, 1, 3) (3, 1, 4) (2, 5, 1)
           1837078 (5, 6, 4) (5, 2, 6)
                                           (5, 1, 2) (4, 1, 5) (3, 4, 6) (6, 2, 3) (4, 3, 1) (2, 1, 3)
```

1837079 rows × 8 columns

```
In [54]:
          def myNumerize(L):
              if L == [4,5,6]:
                   return 0
               elif L == [1,2,3]:
                   return 1
              elif L == [1,2,5]:
                   return 2
              elif L == [1,3,4]:
                   return 3
              elif L == [1,4,5]:
                   return 4
              elif L == [2,3,6]:
                   return 5
              elif L == [2,5,6]:
                   return 6
               if L == [3,4,6]:
                   return 7
```

```
In [7]:
         for col in dfX3.columns:
             dfX3[col] = dfX3[col].apply(sorted)
             dfX3[col] = dfX3[col].apply(myNumerize)
         dfX3
```

corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7 Out[7]: ID ... ... 

1837079 rows × 8 columns

```
In [77]:
          #RandomForest
          from sklearn.ensemble import RandomForestClassifier
          from sklearn.model selection import train test split
          from sklearn.metrics import mean absolute error
          X_train, X_test, y_train, y_test = train_test_split(dfX3.to_numpy(), y, test_
          dtree = RandomForestClassifier(max depth=80,verbose=3,n jobs=32)
          dtree.fit(X_train, y_train)
          ydr = dtree.predict(X train)
          ydt = dtree.predict(X_test)
          print(mean absolute error(y train,ydr),mean absolute error(y test,ydt))
         [Parallel(n jobs=32)]: Using backend ThreadingBackend with 32 concurrent worke
         building tree 1 of 100
         building tree 2 of 100
         building tree 3 of 100
         building tree 4 of 100building tree 5 of 100
         building tree 6 of 100building tree 7 of 100
         building tree 8 of 100
         building tree 9 of 100building tree 10 of 100
         building tree 11 of 100building tree 12 of 100
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         building tree 20 of 100
         building tree 21 of 100
         building tree 22 of 100
         building tree 23 of 100
         building tree 24 of 100building tree 25 of 100building tree 26 of 100
```

building tree 27 of 100building tree 28 of 100 building tree 29 of 100building tree 30 of 100 building tree 31 of 100 building tree 32 of 100 building tree 33 of 100building tree 34 of 100 building tree 35 of 100 building tree 36 of 100 building tree 37 of 100 building tree 38 of 100 building tree 39 of 100building tree 40 of 100 building tree 41 of 100 building tree 42 of 100 building tree 43 of 100 building tree 44 of 100 building tree 45 of 100 building tree 46 of 100 building tree 47 of 100 building tree 48 of 100 building tree 49 of 100 building tree 50 of 100building tree 51 of 100 building tree 52 of 100 building tree 53 of 100building tree 54 of 100 building tree 55 of 100building tree 56 of 100 building tree 57 of 100 building tree 58 of 100 building tree 59 of 100 building tree 60 of 100 building tree 61 of 100 building tree 62 of 100building tree 63 of 100 building tree 64 of 100 building tree 65 of 100 building tree 66 of 100 building tree 68 of 100 building tree 67 of 100building tree 69 of 100 building tree 70 of 100 building tree 71 of 100 building tree 72 of 100building tree 73 of 100 building tree 74 of 100 building tree 75 of 100 building tree 76 of 100 building tree 77 of 100 building tree 78 of 100 building tree 79 of 100 building tree 80 of 100 building tree 81 of 100 building tree 82 of 100 building tree 83 of 100 building tree 84 of 100 building tree 85 of 100 building tree 86 of 100 building tree 87 of 100 building tree 88 of 100building tree 89 of 100

```
building tree 90 of 100
         building tree 91 of 100
         building tree 92 of 100
         building tree 93 of 100building tree 94 of 100
         building tree 95 of 100
         building tree 96 of 100
         building tree 97 of 100
         building tree 98 of 100
         building tree 99 of 100building tree 100 of 100
         [Parallel(n jobs=32)]: Done 71 out of 100 | elapsed:
                                                                  33.5s remaining:
                                                                                     13.
         [Parallel(n jobs=32)]: Done 100 out of 100 | elapsed:
                                                                  35.5s finished
         [Parallel(n jobs=32)]: Using backend ThreadingBackend with 32 concurrent worke
         [Parallel(n jobs=32)]: Done 71 out of 100 | elapsed:
                                                                  20.4s remaining:
                                                                                      8.
         [Parallel(n jobs=32)]: Done 100 out of 100 | elapsed:
                                                                  22.0s finished
         [Parallel(n jobs=32)]: Using backend ThreadingBackend with 32 concurrent worke
         0.7807164877090502 0.7894266988917195
         [Parallel(n jobs=32)]: Done 71 out of 100 | elapsed:
                                                                  0.6s remaining:
                                                                                       0.
         [Parallel(n jobs=32)]: Done 100 out of 100 | elapsed:
                                                                  0.7s finished
In [13]:
          dfX4 = dfX3.copy()
          dfX4['distance'] = dfY
          dfX4 = dfX4.drop duplicates()
          dfY2 = dfX4['distance']
In [14]:
          dfX44 = dfX3.copy()
          dfX44['distance'] = dfY
          X4 = dfX4.to numpy()
          X4 = X4.tolist()
          X44 = dfX44.to numpy()
          X44 = X44.tolist()
          weight = []
          for i in range(len(X4)):
              weight.append(X44.count(X4[i]))
              if i%1000 == 0:
                  print(i)
         0
         1000
         2000
         3000
         4000
         5000
         6000
         7000
         8000
         9000
         10000
         11000
         12000
         13000
         14000
         15000
         16000
```

```
17000

18000

19000

20000

In [30]: dfx4['weight'] = np.array(weight)
```

```
In [30]:
    dfX4['weight'] = np.array(weight)
    dfX5 = dfX4.sort_values(by=['weight'])
```

```
In [31]:
    dfx5 = dfx5.drop_duplicates(subset=['corner0','corner1','corner2','corner3','
    y2 = dfx5['distance'].values
    dfx5 = dfx5.drop('distance',axis=1)
    dfx5 = dfx5.drop('weight',axis=1)
    dfx5
```

Out [31]: corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7

| ID    |   |   |   |   |   |   |     |   |
|-------|---|---|---|---|---|---|-----|---|
| 6472  | 0 | 6 | 2 | 4 | 1 | 3 | 7   | 5 |
| 16613 | 0 | 5 | 4 | 7 | 6 | 1 | 3   | 2 |
| 12583 | 0 | 7 | 5 | 6 | 1 | 2 | 4   | 3 |
| 6774  | 0 | 1 | 6 | 7 | 4 | 3 | 2   | 5 |
| 24108 | 0 | 7 | 5 | 1 | 4 | 6 | 3   | 2 |
| •••   |   |   |   |   |   |   | ••• |   |
| 1756  | 0 | 3 | 5 | 6 | 7 | 2 | 1   | 4 |
| 3467  | 0 | 6 | 7 | 5 | 1 | 3 | 4   | 2 |
| 140   | 0 | 3 | 7 | 1 | 4 | 2 | 5   | 6 |
| 150   | 0 | 5 | 7 | 4 | 1 | 2 | 3   | 6 |
| 6617  | 0 | 6 | 2 | 5 | 3 | 4 | 7   | 1 |

5040 rows × 8 columns

```
from sklearn.ensemble import RandomForestClassifier
from sklearn.model_selection import train_test_split
from sklearn.metrics import mean_absolute_error
X_train, X_test, y_train, y_test = train_test_split(dfX5.to_numpy(), y2, test_dtree = RandomForestClassifier(max_depth=5)
dtree.fit(X_train, y_train)
ydr = dtree.predict(X_train)
ydt = dtree.predict(X_test)
print(mean_absolute_error(y_train,ydr),mean_absolute_error(y_test,ydt))
```

0.4928571428571429 0.5087301587301587

```
from sklearn.neural_network import MLPClassifier
   X_train, X_test, y_train, y_test = train_test_split(dfX5.to_numpy(), y2, test
   mlp = MLPClassifier(hidden_layer_sizes=800,random_state=1, max_iter=500,solve:
   mlp.fit(X_train, y_train)
   ydr = mlp.predict(X_train)
   ydt = mlp.predict(X_test)
   print(mean_absolute_error(y_train,ydr),mean_absolute_error(y_test,ydt))
```

0.49603174603174605 0.5154761904761904

# Ajout des orientations de couleur (n'es pas implémenté sur les données finales)

```
In [44]:
          dfX6 = coinCube(dfX)
In [47]:
          def compressTuple(L):
              if L == (5,6,4):
                   return (0,0)
              elif L == (1,3,2):
                   return (1,0)
              elif L == (3,2,1):
                   return (1,1)
              elif L == (2,1,3):
                   return (1,2)
              elif L == (1,2,5):
                   return (2,0)
              elif L == (2,5,1):
                   return (2,1)
              elif L == (5,1,2):
                   return (2,2)
              elif L == (1,4,3):
                   return (3,0)
              elif L == (4,3,1):
                   return (3,1)
              elif L == (3,1,4):
                   return (3,2)
              elif L == (1,5,4):
                   return (4,0)
              elif L == (5,4,1):
                   return (4,1)
              elif L == (4,1,5):
                   return (4,2)
              elif L == (2,3,6):
                   return (5,0)
              elif L == (3,6,2):
                   return (5,1)
              elif L == (6,2,3):
                   return (5,2)
              elif L == (2,6,5):
                   return (6,0)
              elif L == (6,5,2):
                   return (6,1)
              elif L == (5,2,6):
                   return (6,2)
              elif L == (3,4,6):
                   return (7,0)
              elif L == (4,6,3):
                   return (7,1)
```

```
elif L == (6,3,4):
    return (7,2)
else:
    L == None
```

```
corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7
Out[48]:
                   ID
                    0
                           (0, 0)
                                     (5, 0)
                                               (3, 2)
                                                         (1, 0)
                                                                    (4, 2)
                                                                              (2, 2)
                                                                                        (7, 2)
                                                                                                  (6, 0)
                    1
                           (0, 0)
                                     (5, 0)
                                               (4, 0)
                                                          (2, 1)
                                                                   (7, 2)
                                                                             (3, 2)
                                                                                        (1, 1)
                                                                                                  (6, 2)
                    2
                           (0, 0)
                                     (2, 0)
                                                          (7, 0)
                                               (3, 1)
                                                                   (4, 1)
                                                                             (1, 1)
                                                                                        (6, 2)
                                                                                                  (5, 0)
                    3
                           (0, 0)
                                     (1, 0)
                                               (6, 1)
                                                                                                  (5, 2)
                                                          (7, 1)
                                                                    (2, 2)
                                                                              (3, 2)
                                                                                        (4, 0)
                    4
                           (0, 0)
                                     (3, 2)
                                               (5, 2)
                                                         (2, 0)
                                                                   (7, 1)
                                                                              (4, 0)
                                                                                        (6, 1)
                                                                                                   (1, 2)
                            ...
             1837074
                           (0, 0)
                                     (3, 2)
                                               (4, 2)
                                                          (1, 1)
                                                                    (2, 1)
                                                                             (7, 2)
                                                                                        (5, 2)
                                                                                                   (6, 1)
             1837075
                           (0, 0)
                                     (7, 1)
                                                                             (4, 0)
                                                                                                  (6, 0)
                                               (3, 1)
                                                         (5, 1)
                                                                   (1, 2)
                                                                                        (2, 0)
             1837076
                           (0, 0)
                                     (4, 2)
                                               (7, 2)
                                                         (3, 2)
                                                                   (1, 1)
                                                                             (6, 2)
                                                                                        (5, 2)
                                                                                                  (2, 0)
             1837077
                                               (7, 2)
                                                                                                  (2, 1)
                           (0, 0)
                                     (5, 1)
                                                        (4, 1)
                                                                    (6, 2)
                                                                             (1, 2)
                                                                                        (3, 2)
             1837078
                                               (2, 2)
                                                                   (7, 0)
                                                                             (5, 2)
                                                                                                  (1, 2)
                           (0, 0)
                                     (6, 2)
                                                        (4, 2)
                                                                                        (3, 1)
```

1837079 rows × 8 columns

```
i=0
for col in dfX6.columns:
    nom = 'orient' + str(i)
    dfX6[[col,nom]] = pd.DataFrame(dfX6[col].tolist(),index=dfX6.index)
    i+=1
    dfX6
```

| Out[51]: |         | corner0 | corner1 | corner2 | corner3 | corner4 | corner5 | corner6 | corner7 | orient0 | 0 |
|----------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---|
|          | ID      |         |         |         |         |         |         |         |         |         |   |
|          | 0       | 0       | 5       | 3       | 1       | 4       | 2       | 7       | 6       | 0       |   |
|          | 1       | 0       | 5       | 4       | 2       | 7       | 3       | 1       | 6       | 0       |   |
|          | 2       | 0       | 2       | 3       | 7       | 4       | 1       | 6       | 5       | 0       |   |
|          | 3       | 0       | 1       | 6       | 7       | 2       | 3       | 4       | 5       | 0       |   |
|          | 4       | 0       | 3       | 5       | 2       | 7       | 4       | 6       | 1       | 0       |   |
|          | •••     |         |         |         |         |         |         |         |         |         |   |
|          | 1837074 | 0       | 3       | 4       | 1       | 2       | 7       | 5       | 6       | 0       |   |
|          | 1837075 | 0       | 7       | 3       | 5       | 1       | 4       | 2       | 6       | 0       |   |
|          | 1837076 | 0       | 4       | 7       | 3       | 1       | 6       | 5       | 2       | 0       |   |
|          | 1837077 | 0       | 5       | 7       | 4       | 6       | 1       | 3       | 2       | 0       |   |

ID

```
1837078
                       0
                               6
                                       2
                                              4
                                                      7
                                                              5
                                                                      3
                                                                              1
                                                                                     0
         1837079 rows x 16 columns
In [60]:
          dfX6 = dfX6.drop('corner0',axis=1)
          dfX6 = dfX6.drop('orient0',axis=1)
In [61]:
          #RandomForest
          from sklearn.ensemble import RandomForestClassifier
          X train, X test, y train, y test = train test split(dfX6.to numpy(), y, test
          dtree = RandomForestClassifier(max depth = 20 ,verbose=3, n jobs=50)
          dtree.fit(X train, y train)
          ydtr = dtree.predict(X train)
          ydt = dtree.predict(X test)
          print(mean absolute error(y train,ydtr),mean absolute error(y test,ydt))
         [Parallel(n jobs=50)]: Using backend ThreadingBackend with 50 concurrent worke
         building tree 1 of 100building tree 2 of 100
         building tree 3 of 100
         building tree 4 of 100
         building tree 5 of 100
         building tree 6 of 100
         building tree 7 of 100building tree 8 of 100
         building tree 9 of 100building tree 10 of 100
         building tree 11 of 100
         building tree 12 of 100
         building tree 13 of 100building tree 14 of 100
         building tree 15 of 100building tree 16 of 100
         building tree 17 of 100
         building tree 18 of 100
         building tree 19 of 100
         building tree 20 of 100
         building tree 21 of 100building tree 22 of 100
         building tree 23 of 100building tree 24 of 100
         building tree 25 of 100
         building tree 26 of 100building tree 27 of 100
         building tree 28 of 100
         building tree 29 of 100
         building tree 30 of 100building tree 31 of 100
         building tree 32 of 100
         building tree 33 of 100
         building tree 34 of 100
         building tree 35 of 100
         building tree 36 of 100building tree 37 of 100
         building tree 38 of 100
         building tree 39 of 100
         building tree 40 of 100building tree 41 of 100
```

corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7 orient0 o

```
building tree 42 of 100building tree 43 of 100
building tree 44 of 100
building tree 45 of 100
building tree 46 of 100
building tree 47 of 100
building tree 48 of 100
building tree 49 of 100
building tree 50 of 100
building tree 51 of 100
building tree 52 of 100building tree 53 of 100
building tree 54 of 100building tree 55 of 100building tree 56 of 100
building tree 57 of 100
building tree 58 of 100building tree 59 of 100
building tree 60 of 100
building tree 61 of 100building tree 62 of 100
building tree 63 of 100
building tree 64 of 100
building tree 65 of 100building tree 66 of 100building tree 67 of 100
building tree 68 of 100building tree 69 of 100
building tree 70 of 100
building tree 71 of 100
building tree 72 of 100
building tree 73 of 100building tree 74 of 100building tree 75 of 100
building tree 76 of 100
building tree 77 of 100
building tree 78 of 100building tree 79 of 100building tree 80 of 100
building tree 81 of 100
building tree 82 of 100building tree 83 of 100building tree 84 of 100
building tree 85 of 100building tree 86 of 100building tree 87 of 100building
tree 88 of 100
building tree 89 of 100
building tree 90 of 100
building tree 91 of 100
building tree 92 of 100
[Parallel(n jobs=50)]: Done 35 out of 100 | elapsed: 14.2s remaining:
                                                                           26.
building tree 93 of 100
building tree 94 of 100
building tree 95 of 100building tree 96 of 100
building tree 97 of 100
building tree 98 of 100building tree 99 of 100
```

```
[Parallel(n jobs=50)]: Done 69 out of 100 | elapsed:
                                                       27.4s remaining:
                                                                          12.
[Parallel(n jobs=50)]: Done 100 out of 100 | elapsed:
                                                       28.0s finished
[Parallel(n jobs=50)]: Using backend ThreadingBackend with 50 concurrent worke
[Parallel(n jobs=50)]: Done 35 out of 100 | elapsed:
                                                       25.5s remaining:
                                                                           47.
[Parallel(n jobs=50)]: Done 69 out of 100 | elapsed:
                                                       30.5s remaining:
                                                                          13.
[Parallel(n jobs=50)]: Done 100 out of 100 | elapsed:
                                                       32.1s finished
[Parallel(n jobs=50)]: Using backend ThreadingBackend with 50 concurrent worke
[Parallel(n jobs=50)]: Done 35 out of 100 | elapsed:
                                                       28.0s remaining:
[Parallel(n jobs=50)]: Done 69 out of 100 | elapsed:
                                                       32.7s remaining:
                                                                          14.
0.07402734124517305 0.9035240708080214
[Parallel(n jobs=50)]: Done 100 out of 100 | elapsed:
                                                       34.4s finished
```

## Premier résultat envoyé : colonne constante de 11

```
In []:
    dfY2 = dfY.copy()
    dfY2['distance'] = 11
    dfY2.loc[3674158] = 11
    dfY2 = pd.concat([dfY,dfY2], ignore_index = True)
    dfY2 = dfY2.iloc[1837079:]
    dfY2.to_csv("y_test.csv")
    dfY2
```

## Deuxième résultat envoyé : utilisation des coins

|         | corner0 | corner1 | corner2 | corner3 | corner4 | corner5 | corner6 | corner7 |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| ID      |         |         |         |         |         |         |         |         |
| 1837079 | 0       | 7       | 3       | 6       | 5       | 2       | 4       | 1       |
| 1837080 | 0       | 6       | 3       | 1       | 5       | 4       | 7       | 2       |
| 1837081 | 0       | 1       | 7       | 6       | 2       | 3       | 4       | 5       |
| 1837082 | 0       | 2       | 7       | 5       | 3       | 1       | 6       | 4       |
| 1837083 | 0       | 1       | 4       | 2       | 6       | 7       | 3       | 5       |
| •••     |         |         |         |         |         |         |         |         |
| 3674154 | 0       | 5       | 4       | 1       | 6       | 2       | 7       | 3       |

Out [143...

corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7 ID 3674155 0 6 2 1 5 4 7 3 7 6 5 3 3674156 0 4 1 2 4 5 7 2 3674157 0 1 3 6 2 3 7 3674158 5 4 1 6

1837080 rows × 8 columns

```
In [144... | T3 = dfT3.to_numpy()
In [468...
          dtree = RandomForestClassifier(max depth=100,verbose=3, n jobs=32)
          dtree.fit(X3, y)
          ydt = dtree.predict(T3)
         [Parallel(n jobs=32)]: Using backend ThreadingBackend with 32 concurrent worke
         rs.
         building tree 1 of 100building tree 2 of 100
         building tree 3 of 100
         building tree 4 of 100
         building tree 5 of 100
         building tree 6 of 100building tree 7 of 100building tree 8 of 100
         building tree 9 of 100building tree 10 of 100building tree 11 of 100
         building tree 12 of 100
         building tree 13 of 100building tree 14 of 100
         building tree 15 of 100
         building tree 16 of 100
         building tree 17 of 100
         building tree 18 of 100building tree 19 of 100building tree 20 of 100
         building tree 21 of 100
         building tree 22 of 100building tree 23 of 100building tree 24 of 100
         building tree 25 of 100building tree 26 of 100
         building tree 28 of 100building tree 27 of 100
         building tree 29 of 100
         building tree 30 of 100
         building tree 31 of 100building tree 32 of 100
         building tree 33 of 100
         building tree 34 of 100
         building tree 35 of 100
         building tree 36 of 100
         building tree 37 of 100
         building tree 38 of 100
         building tree 39 of 100
         building tree 40 of 100
```

```
building tree 41 of 100
building tree 42 of 100
building tree 43 of 100
building tree 44 of 100
building tree 45 of 100
building tree 46 of 100
building tree 47 of 100
building tree 48 of 100
building tree 49 of 100
building tree 50 of 100
building tree 51 of 100
building tree 52 of 100
building tree 53 of 100
building tree 54 of 100
building tree 55 of 100
building tree 56 of 100building tree 57 of 100
building tree 58 of 100building tree 59 of 100
building tree 60 of 100
building tree 61 of 100
building tree 62 of 100building tree 63 of 100
building tree 64 of 100
building tree 65 of 100
building tree 66 of 100
building tree 67 of 100
building tree 68 of 100
building tree 69 of 100
building tree 70 of 100
building tree 71 of 100
building tree 72 of 100
building tree 73 of 100building tree 74 of 100
building tree 75 of 100
building tree 76 of 100
building tree 77 of 100
building tree 78 of 100
building tree 79 of 100
building tree 80 of 100
building tree 81 of 100building tree 82 of 100
building tree 83 of 100
building tree 84 of 100
building tree 85 of 100building tree 86 of 100
building tree 87 of 100
building tree 88 of 100
building tree 89 of 100
building tree 90 of 100
building tree 91 of 100
building tree 92 of 100
building tree 93 of 100
building tree 94 of 100building tree 95 of 100
building tree 96 of 100
building tree 97 of 100
building tree 98 of 100
building tree 99 of 100
building tree 100 of 100
                                                        48.7s remaining:
[Parallel(n jobs=32)]: Done 71 out of 100 | elapsed:
                                                                            19.
[Parallel(n jobs=32)]: Done 100 out of 100 | elapsed:
                                                         51.3s finished
[Parallel(n jobs=32)]: Using backend ThreadingBackend with 32 concurrent worke
```

```
rs.
          [Parallel(n jobs=32)]: Done 71 out of 100 | elapsed:
                                                                       24.8s remaining:
                                                                                            10.
          [Parallel(n jobs=32)]: Done 100 out of 100 | elapsed:
                                                                       26.6s finished
In [470...
           np.bincount(ydt)
                       0,
                                0, 0,
                                             0,
                                                          0,
                                                                   0,
                                                                           0,
                                                                                    0,
          array([
Out [470...
                                0, 665173, 918540, 2533671)
In [154...
           dfYt = pd.DataFrame(ydt)
           ids = pd.DataFrame(np.arange(1837079,3674159))
           ids['ID'] = ids
           dfYt.index = ids['ID']
           dfYt
                    0
Out [154...
                ID
          1837079 10
          1837080 12
           1837081 12
          1837082 10
          1837083
                  11
                ...
          3674154
          3674155 11
          3674156 10
           3674157 12
          3674158 11
         1837080 rows × 1 columns
In [153...
           dfYt.to csv("y test.csv")
In [145...
           X5 = dfX5.to_numpy()
           dfT3
Out [145...
                   corner0 corner1 corner2 corner3 corner4 corner5 corner6 corner7
                ID
          1837079
                                 7
                         0
                                         3
                                                  6
                                                          5
                                                                   2
                                                                           4
                                                                                   1
                                                          5
          1837080
                         0
                                 6
                                          3
                                                  1
                                                                   4
                                                                           7
                                                                                   2
                                          7
                                                          2
          1837081
                         0
                                 1
                                                  6
                                                                   3
                                                                           4
                                                                                   5
          1837082
                                 2
                                          7
                                                  5
                                                          3
                                                                   1
                                                                                   4
          1837083
                                          4
                                                  2
                                                          6
                                                                   7
                         0
                                 1
                                                                           3
                                                                                   5
                         • • •
                                 • • •
                                         • • •
```

|         | corner0 | corner1 | corner2 | corner3 | corner4 | corner5 | corner6 | corner7 |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| ID      |         |         |         |         |         |         |         |         |
| 3674154 | 0       | 5       | 4       | 1       | 6       | 2       | 7       | 3       |
| 3674155 | 0       | 6       | 2       | 1       | 5       | 4       | 7       | 3       |
| 3674156 | 0       | 7       | 6       | 5       | 3       | 4       | 1       | 2       |
| 3674157 | 0       | 4       | 5       | 7       | 2       | 1       | 3       | 6       |
| 3674158 | 0       | 5       | 4       | 2       | 3       | 1       | 7       | 6       |

1837080 rows × 8 columns

```
In [147...
          dtree = RandomForestClassifier(max depth = 100, verbose = 3)
          dtree.fit(X5, y2)
          ydt = dtree.predict(T3)
          np.bincount(ydt)
         [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent worker
                                                  1 | elapsed:
         [Parallel(n jobs=1)]: Done
                                      1 out of
                                                                  0.0s remaining:
                                                                                     0.0
                                      2 out of
                                                  2 | elapsed:
                                                                  0.0s remaining:
         [Parallel(n jobs=1)]: Done
                                                                                     0.0
         building tree 1 of 100
         building tree 2 of 100
         building tree 3 of 100
         building tree 4 of 100
         building tree 5 of 100
         building tree 6 of 100
         building tree 7 of 100
         building tree 8 of 100
         building tree 9 of 100
         building tree 10 of 100
         building tree 11 of 100
         building tree 12 of 100
         building tree 13 of 100
         building tree 14 of 100
         building tree 15 of 100
         building tree 16 of 100
         building tree 17 of 100
         building tree 18 of 100
         building tree 19 of 100
         building tree 20 of 100
         building tree 21 of 100
         building tree 22 of 100
         building tree 23 of 100
         building tree 24 of 100
         building tree 25 of 100
         building tree 26 of 100
         building tree 27 of 100
         building tree 28 of 100
         building tree 29 of 100
         building tree 30 of 100
         building tree 31 of 100
         building tree 32 of 100
         building tree 33 of 100
         building tree 34 of 100
         building tree 35 of 100
```

building tree 36 of 100

building tree 37 of 100 building tree 38 of 100 building tree 39 of 100 building tree 40 of 100 building tree 41 of 100 building tree 42 of 100 building tree 43 of 100 building tree 44 of 100 building tree 45 of 100 building tree 46 of 100 building tree 47 of 100 building tree 48 of 100 building tree 49 of 100 building tree 50 of 100 building tree 51 of 100 building tree 52 of 100 building tree 53 of 100 building tree 54 of 100 building tree 55 of 100 building tree 56 of 100 building tree 57 of 100 building tree 58 of 100 building tree 59 of 100 building tree 60 of 100 building tree 61 of 100 building tree 62 of 100 building tree 63 of 100 building tree 64 of 100 building tree 65 of 100 building tree 66 of 100 building tree 67 of 100 building tree 68 of 100 building tree 69 of 100 building tree 70 of 100 building tree 71 of 100 building tree 72 of 100 building tree 73 of 100 building tree 74 of 100 building tree 75 of 100 building tree 76 of 100 building tree 77 of 100 building tree 78 of 100 building tree 79 of 100 building tree 80 of 100 building tree 81 of 100 building tree 82 of 100 building tree 83 of 100 building tree 84 of 100 building tree 85 of 100 building tree 86 of 100 building tree 87 of 100 building tree 88 of 100 building tree 89 of 100 building tree 90 of 100 building tree 91 of 100 building tree 92 of 100 building tree 93 of 100 building tree 94 of 100 building tree 95 of 100 building tree 96 of 100 building tree 97 of 100 building tree 98 of 100 building tree 99 of 100 building tree 100 of 100

```
[Parallel(n jobs=1)]: Done 100 out of 100 | elapsed:
                                                                     0.4s finished
          [Parallel(n jobs=1)]: Using backend SequentialBackend with 1 concurrent worker
                                        1 out of
                                                    1 | elapsed:
          [Parallel(n jobs=1)]: Done
                                                                     0.2s remaining:
                                                                                         0.0
          [Parallel(n jobs=1)]: Done
                                                    2 | elapsed:
                                                                     0.4s remaining:
                                        2 out of
                                                                                         0.0
          [Parallel(n jobs=1)]: Done 100 out of 100 | elapsed:
                                                                    22.0s finished
                               0,
                      0,
                                                        0,
                                                                0,
                                                                         0,
          array([
                                       0,
                                                0,
Out[147...
                               0, 663711, 918540, 254829])
                      0,
In [148...
          #Correction de doublons dans le test
          X51 = X5.tolist()
          T31 = T3.tolist()
          for i in range(len(T31)):
               if T31[i] in X51:
                   j = X51.index(T31[i])
                   ydt[i] = y2[j]
                   if i%100000==0:
                       print(i)
          0
          100000
          200000
          300000
          400000
          500000
          600000
          700000
          800000
          900000
          1000000
          1100000
          1200000
          1300000
          1400000
          1500000
          1600000
          1700000
          1800000
In [149...
          np.bincount(ydt)
                                                                 0,
                                                                         0,
          array([
                      0,
                               0,
                                       0,
                                                0,
                                                        0,
                                                                                  0,
Out [149...
                      0,
                               0, 663711, 918540, 254829])
```