

# Week 3 Forecast

## 1. Write pseudo code of binary search algorithm

Steps

1. Input array  $a$  size  $n$  and  $x$  to be found
2. Initialize  $low = 0$   $high = n - 1$
3. Do until  $low \geq high$   
     $mid = (low + high) / 2$   
    if  $a[mid] == x$  print  $mid$ , go to end  
    else  
        if  $a[mid] < x$   $low = mid + 1$   
        else  $high = mid - 1$
4. Print " $x$  not found"
5. End

## 2 Analysis pseudo code of step 1.

### 2.1 Space complexity

### 2.2 Time complexity in base case

### 2.3 Time complexity in worst case

#### 2.1 Space complexity

array is given  
variables created: mid, low, high  
 $A = 3H$

#### 2.2 Base case

x at  $N/2$  1 comparison

x at  $N/4, 3N/4$  2 comparisons

x at  $N/8, 3N/8, 5N/8, 7N/8$  3 comparisons

$\left. \begin{array}{l} i \text{ 1 comparison} = 1 \\ i \text{ 2 comparison} = 2 \\ i \text{ 3 comparisons} = 4 \end{array} \right\} 2^{i-1}$

$$A = O(\lg n)$$

#### 2.3 Worst case

x is at  $a[0]$  or  $a[n-1]$

comparisons required  $\lg(n)$

$$A = O(\lg n)$$