Week 11: Solving Maximum Matching Problem

1. Describe the difference between original Ford-Fulkerson algorithm and Edmonds-Karp algorithm in general flow network and in bipartite matching.

Both algorithms can be exactly the same, however Ford-Fulkerson doesn't have a defined way to find the augmented paths, while Edmonds-Karp uses a Breadth first search to find the shortest path with available capacity

2. Brief about blossom algorithm.

Blossom algorithms also uses breadth first found augmented paths which to form pairings. When a new longer augmented path is found then the pairings are updated. The blossom algorithm encounters a "blossom" which is an odd cycle of alternating edges. The blossom is contracted into a single super vertex and the augmented path is found using this blossom.

3. Suppose edges between Vs and Vt are weighted, please design an algorithm for finding maximum matching with minimum cost.

Given Vs has n elements and Vt m elements.

Create n*m matrix

Fill the cells with the weights of the edges

Subtract the minimum weight in a line to all the elements in that line Subtract the minimum weight in a column to all the elements in that column

Count the number X of lines and columns that contain 0

If X<min(n,m)

Take the lowest number from the lines and column that don't contain 0 Subtract it to all the elements not part of a column or line with 0 Add it to all the elements part of a column or line with 0 Repeat until X=min(n,m)

4. Please compare time complexity between original flow algorithm and your modified version in Question 3.

The maximum flow algorithm using Edmonds-Karp has a time complexity of $O(V^2*E)$

The algorithm in Question 3 has complexity O(n^2*m^2) but it returns the minimum cost while the other just the first pairing encountered.