

The question is a parameter estimation problem. The objective is to determine the values of unknown variables within a specific parametric equation of a curve.

The two models/equations are:

$$x = (t \cdot \cos \theta - e^{M \cdot |t|} * \sin(0.3 * t) * \sin \theta + X)$$

$$y = (42 + t \cdot \sin \theta + e^{M \cdot |t|} * \sin(0.3 * t) * \cos \theta)$$

with the parameters  $\theta$ ,  $M$ ,  $X$ .

The data (x,y) for 1500 points are given in a file. As  $t$  lies between 6 and 60, it is uniformly sampled to get 1500 points, corresponding to (x,y).

As  $x$  and  $y$  share **two parameters**( $M$ ,  $\theta$ ) , optimizing parameters separately for  $x$  or  $y$  would yield inconsistent results that cannot describe a single coherent 2D curve.

Therefore, the loss for  $x$  and  $y$  are computed separately and their **sum is minimized jointly** using the ADAM optimizer, which finds a single parameter set  $\{\theta, M, X\}$  that simultaneously minimizes errors in both dimensions.