1.9.19

Josyula G S Avaneesh - EE25BTECH11030

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Question

Find the value of x for which the distance between the points $\mathbf{A}(x,2)$ and $\mathbf{B}(9,8)$ is 10 units.

Equation

Distance between 2 vectors **A** and **B** can be represented as:

$$||AB|| = \sqrt{(\mathbf{B} - \mathbf{A})^T (\mathbf{B} - \mathbf{A})}$$
 (1)

Given details:

$$\mathbf{3} = \begin{pmatrix} 9 \\ 8 \end{pmatrix} \tag{2}$$

$$\mathbf{B} = \begin{pmatrix} 9 \\ 8 \end{pmatrix} \tag{2}$$

$$\mathbf{A} = \begin{pmatrix} x \\ 2 \end{pmatrix} \tag{3}$$

$$||AB|| = 10 \tag{4}$$

By substituting values:

$$||AB|| = \sqrt{\left(9 - x \quad 8 - 2\right) \begin{pmatrix} 9 - x \\ 8 - 2 \end{pmatrix}} = \sqrt{\left(9 - x \quad 6\right) \begin{pmatrix} 9 - x \\ 6 \end{pmatrix}}$$
 (5)

$$= \sqrt{(9-x)^2 + (6)^2} = \sqrt{(x^2 - 18x + 81) + 36} = \sqrt{x^2 - 18x + 117}$$
 (6)

Now from equation (3) and (4), we can say that :

$$\sqrt{x^2 - 18x + 117} = 10\tag{7}$$

Square on both sides

$$x^2 - 18x + 117 = 100 (8)$$

$$x^2 - 18x + 17 = 0 (9)$$

On solving this we get,
$$x = 1$$
 or $x = 17$ (10)

Final answer:

The values of x are 1 and 17. Therefore, the points $\mathbf{A}(x,2)$ are (1,2) or (17,2).

C Code (1) - Function to generate a line segment

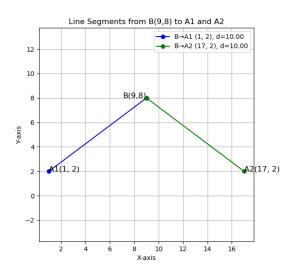
```
import ctypes
import numpy as np
import matplotlib.pyplot as plt
import matplotlib as mp
mp.use("TkAgg")
# Load shared object
lib = ctypes.CDLL("./line.so")
# Define function signature
lib.distance.argtypes = [ctypes.c_double, ctypes.c_double,
                       ctypes.c double, ctypes.c double]
lib.distance.restype = ctypes.c double
```

```
# Fixed point B
 B = (9, 8)
# Two A points
 A1 = (1, 2)
 A2 = (17,2)
 # Distances from B using C function
 d1 = lib.distance(B[0], B[1], A1[0], A1[1])
 d2 = lib.distance(B[0], B[1], A2[0], A2[1])
 # Plot line segments B->A1 and B->A2
 plt.figure(figsize=(6,6))
```

```
# Line B->A1
 |plt.plot([B[0], A1[0]], [B[1], A1[1]], 'b-o', label=f"BA1 {A1}, d
     ={d1:.2f}")
s | plt.text(A1[0], A1[1], f"A1{A1}", fontsize=12, ha='left')
 # Line B->A2
 plt.plot([B[0], A2[0]], [B[1], A2[1]], 'g-o', label=f"BA2 {A2}, d
     ={d2:.2f}")
plt.text(A2[0], A2[1], f"A2{A2}", fontsize=12, ha='left')
 # Mark B
plt.scatter(B[0], B[1], color='red')
 plt.text(B[0], B[1], "B(9,8)", fontsize=12, ha='right')
```

```
# Labels & styling
plt.xlabel("X-axis")
plt.ylabel("Y-axis")
plt.title("Line Segments from B(9,8) to A1 and A2")
plt.legend()
plt.grid(True)
plt.axis("equal")
plt.savefig('/home/avaneesh1/Matrix/ee1030-2025/ee25btech11030/
    matgeo/1.9.19/figs/distance.png')
plt.show(block=True)
```

Plot-Using Both C and Python



Python Code

```
import numpy as np
import matplotlib.pyplot as plt
import matplotlib as mp
mp.use("TkAgg")
# Fixed point B
B = (9, 8)
# Two A points
A1 = (1, 2)
A2 = (17, 2)
# Distances using numpy
d1 = np.sqrt((A1[0]-B[0])**2 + (A1[1]-B[1])**2)
d2 = np.sqrt((A2[0]-B[0])**2 + (A2[1]-B[1])**2)
```

Python Code

```
# Plot line segments B->A1 and B->A2
 plt.figure(figsize=(6,6))
 # Line B->A1
 |plt.plot([B[0], A1[0]], [B[1], A1[1]], 'b-o', label=f"BA1 {A1}, d
     ={d1:.2f}"
plt.text(A1[0], A1[1], f"A1{A1}", fontsize=12, ha='left')
 # Line B->A2
 |plt.plot([B[0], A2[0]], [B[1], A2[1]], 'g-o', label=f"BA2 {A2}, d
     ={d2:.2f}")
plt.text(A2[0], A2[1], f"A2{A2}", fontsize=12, ha='left')
```

Python Code

```
# Mark B
plt.scatter(B[0], B[1], color='red')
plt.text(B[0], B[1], "B(9,8)", fontsize=12, ha='right')
# Labels & styling
plt.xlabel("X-axis")
plt.ylabel("Y-axis")
plt.title("Line Segments from B(9,8) to A1 and A2")
plt.legend()
plt.grid(True)
plt.axis("equal")
plt.savefig('/home/avaneesh1/Matrix/ee1030-2025/ee25btech11030/
    matgeo/1.9.19/figs/distance2.png')
plt.show(block=True)
```

Plot-Using only Python

