Knowledge Discovery and Data Mining

Unit#4

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Acknowledgement

- Most of the slides in this presentation are taken from course slides provided by
 - Han and Kimber (Data Mining Concepts and Techniques) and
 - Tan, Steinbach and Kumar (Introduction to Data Mining)

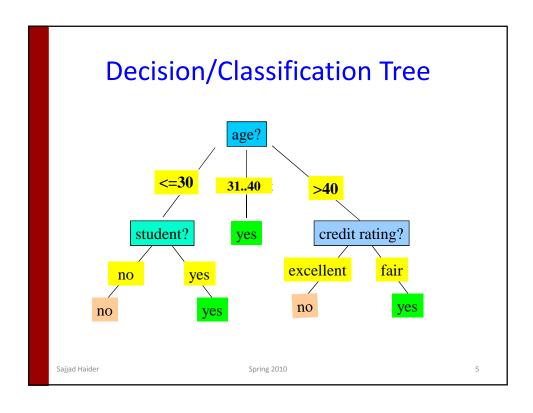
Classification: Definition

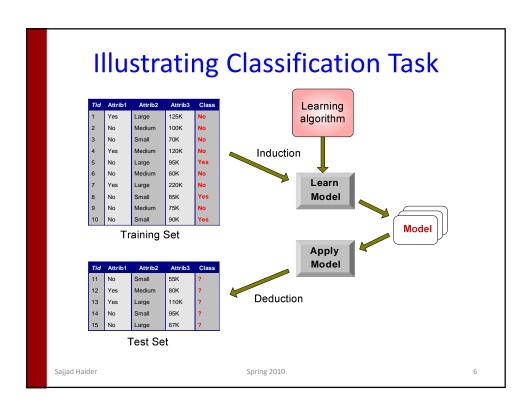
- Given a collection of records (training set)
 - Each record contains a set of attributes, one of the attributes is the class.
- Find a *model* for class attribute as a function of the values of other attributes.
- Goal: <u>previously unseen</u> records should be assigned a class as accurately as possible.
 - A test set is used to determine the accuracy of the model. Usually, the given data set is divided into training and test sets, with training set used to build the model and test set used to validate it.

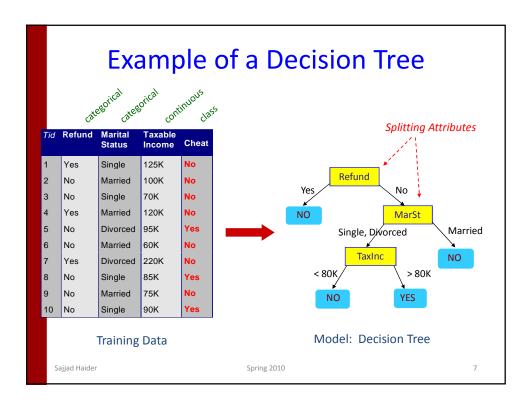
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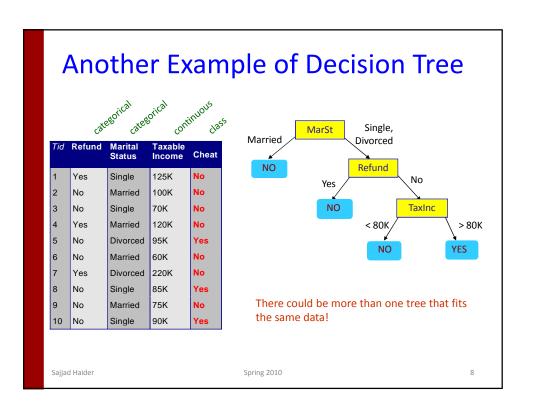
Classification: Motivation

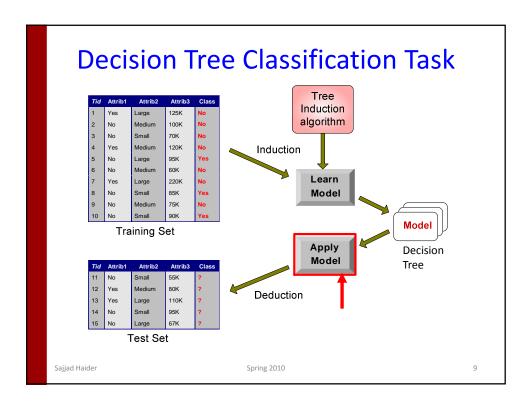
age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

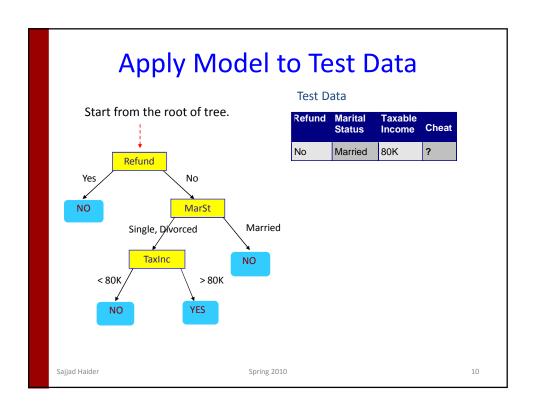


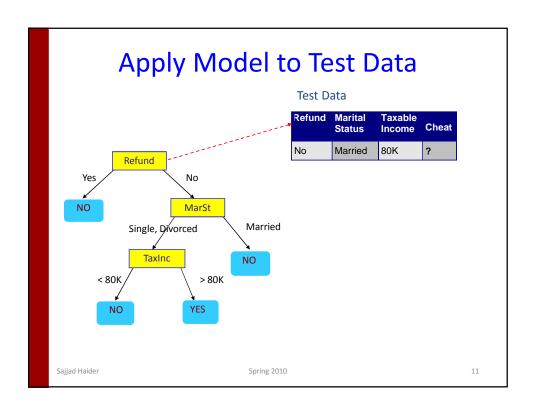


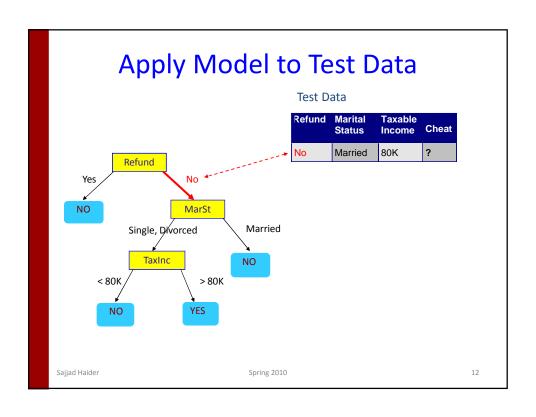


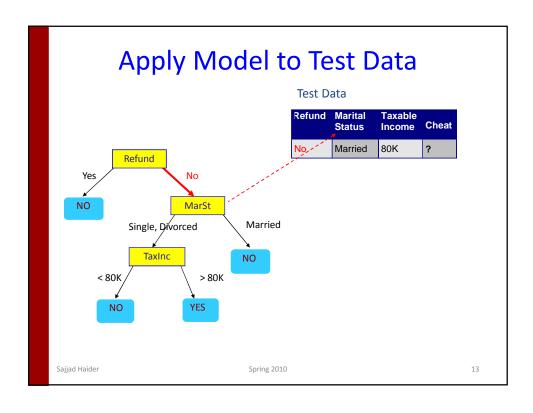


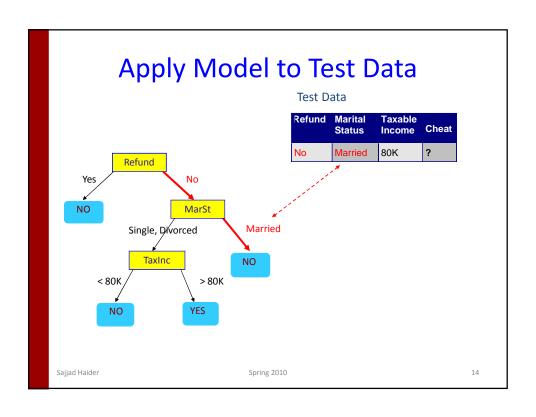


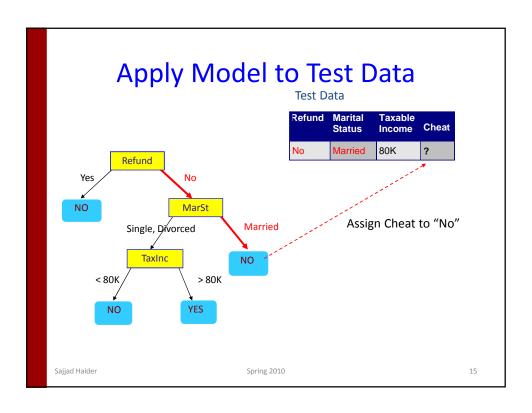


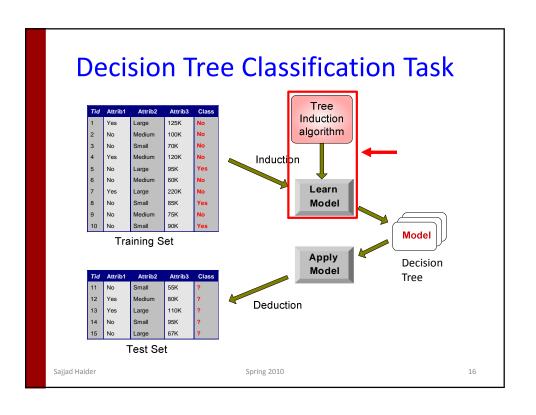












Tree Induction

- Greedy strategy.
 - Split the records based on an attribute test that optimizes certain criterion.
- Issues
 - Determine how to split the records
 - How to specify the attribute test condition?
 - How to determine the best split?
 - Determine when to stop splitting

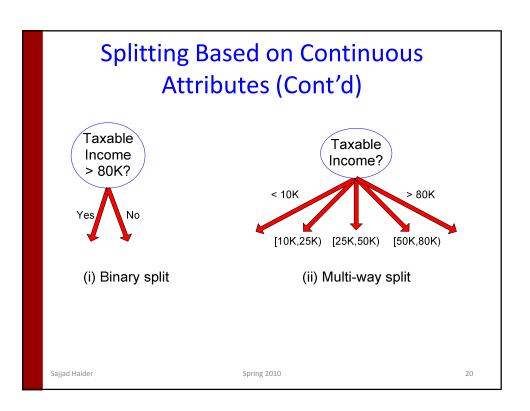
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How to Specify Test Condition?

- Depends on attribute types
 - Nominal
 - Ordinal
 - Continuous
- Depends on number of ways to split
 - 2-way split
 - Multi-way split

Splitting Based on Continuous Attributes

- Different ways of handling
 - Discretization to form an ordinal categorical attribute
 - Static discretize once at the beginning
 - Dynamic ranges can be found by equal interval bucketing, equal frequency bucketing (percentiles), or clustering.
 - Binary Decision: (A < v) or (A \ge v)
 - consider all possible splits and finds the best cut
 - can be more compute intensive



How to determine the Best Split

- Greedy approach:
 - Nodes with homogeneous class distribution are preferred
- Need a measure of node impurity:

C0: 5 C1: 5 C0: 9 C1: 1

Non-homogeneous,

High degree of impurity

Homogeneous,

Low degree of impurity

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Measures of Node Impurity

- Gini Index
- Entropy
- Misclassification error

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Measure of Impurity: GINI

• Gini Index for a given node t :

$$GINI(t) = 1 - \sum_{j} [p(j|t)]^{2}$$

(NOTE: $p(j \mid t)$ is the relative frequency of class j at node t).

- Maximum $(1 1/n_c)$ when records are equally distributed among all classes, implying least interesting information
- Minimum (0.0) when all records belong to one class, implying most interesting information

C1	0	
C2	6	
Gini=0.000		







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Examples for computing GINI

$$GINI(t) = 1 - \sum_{j} [p(j|t)]^{2}$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Gini =
$$1 - P(C1)^2 - P(C2)^2 = 1 - 0 - 1 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$
 $Gini = 1 - (1/6)^2 - (5/6)^2 = 0.278$

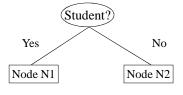
$$P(C1) = 2/6$$
 $P(C2) = 4/6$
 $Gini = 1 - (2/6)^2 - (4/6)^2 = 0.444$

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Binary Attributes: Computing GINI Index

- Splits into two partitions
- Effect of Weighing partitions:
 - Larger and Purer Partitions are sought for.



Yes 9
No 5
Gini = 0.46

Gini(N1) = 1 - (6/7)² - (1/7)²

= 0.24

Gini(N2) = $1 - (3/7)^2 - (4/7)^2$

= 0.49

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 N1
 N2

 Yes
 6
 3

 No
 1
 4

 Gini=0.365

Gini(Student) = 7/14 * 0.24 + 7/14 * 0.49 = ??

Categorical Attributes: Computing GINI Index

- For each distinct value, gather counts for each class in the dataset
- · Use the count matrix to make decisions

Multi-way split

	CarType		
	Family	Sports	Luxury
C1	1	2	1
C2	4	1	1
Gini	0.393		

Two-way split (find best partition of values)

	CarType	
	{Sports, Luxury}	{Family}
C1	3	1
C2	2	4
Gini	0.400	

	CarType		
	{Sports}	{Family, Luxury}	
C1	2	2	
C2	1	5	
Gini	0.419		

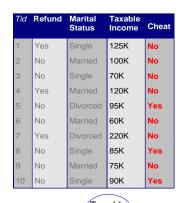
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Continuous Attributes: Computing GINI

Index

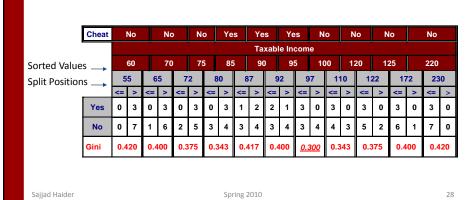
- Use Binary Decisions based on one value
- Several Choices for the splitting value
 - Number of possible splitting valuesNumber of distinct values
- Each splitting value has a count matrix associated with it
 - Class counts in each of the partitions, A
 < v and A ≥ v
- Simple method to choose best v
 - For each v, scan the database to gather count matrix and compute its Gini index
 - Computationally Inefficient! Repetition of work.





Continuous Attributes: Computing GINI Index (Cont'd)

- For efficient computation: for each attribute,
 - Sort the attribute on values
 - Linearly scan these values, each time updating the count matrix and computing gini index
 - Choose the split position that has the least gini index



GINI Index for Buy Computer Example

- Gini (Income):
- Gini (Credit_Rating):
- Gini (Age):

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Alternative Splitting Criteria based on Entropy

Entropy at a given node t:

$$Entropy(t) = -\sum_{j} p(j|t) \log p(j|t)$$

(NOTE: $p(j \mid t)$ is the relative frequency of class j at node t).

- Measures homogeneity of a node.
 - Maximum (log n_c) when records are equally distributed among all classes implying least information
 - Minimum (0.0) when all records belong to one class, implying most information
- Entropy based computations are similar to the GINI index computations

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Entropy in a nut-shell





Low Entropy

High Entropy

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Examples for computing Entropy

 $Entropy(t) = -\sum_{j} p(j|t) \log_{2} p(j|t)$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Entropy =
$$-0 \log 0 - 1 \log 1 = -0 - 0 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

Entropy =
$$-(1/6) \log_2 (1/6) - (5/6) \log_2 (1/6) = 0.65$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Entropy =
$$-(2/6) \log_2 (2/6) - (4/6) \log_2 (4/6) = 0.92$$

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Splitting Criteria based on Classification Error

• Classification error at a node t :

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

- Measures misclassification error made by a node.
 - Maximum (1 1/n_c) when records are equally distributed among all classes, implying least interesting information
 - Minimum (0.0) when all records belong to one class, implying most interesting information

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Examples for Computing Error

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

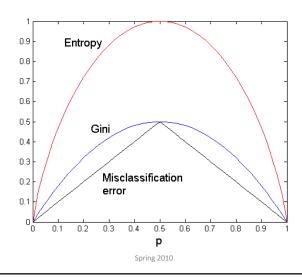
C1 P(C1) =
$$0/6 = 0$$
 P(C2) = $6/6 = 1$
C2 **6** Error = $1 - \max(0, 1) = 1 - 1 = 0$

C1	1	P(C1) = 1/6	P(C2) = 5/6
C2	5	Error = 1 – ma	ax (1/6, 5/6) = 1 – 5/6 = 1/6

Comparison among Splitting Criteria

For a 2-class problem:

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Inducing a decision tree

- There are many possible trees
- How to find the most compact one
 - that is consistent with the data?
- The *key* to building a decision tree which attribute to choose in order to branch.
- The *heuristic* is to choose the attribute with the minimum GINI/Entropy.

Algorithm for Decision Tree Induction

- Basic algorithm (a greedy algorithm)
 - Tree is constructed in a top-down recursive manner
 - At start, all the training examples are at the root
 - Attributes are categorical
 - Examples are partitioned recursively based on selected attributes
 - Test attributes are selected on the basis of a heuristic or statistical measure (e.g., GINI/Entropy)
- Conditions for stopping partitioning
 - All examples for a given node belong to the same class
 - There are no remaining attributes for further partitioning majority voting is employed for classifying the leaf
 - There are no examples left

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Extracting Classification Rules from Trees

- Represent the knowledge in the form of IF-THEN rules
- One rule is created for each path from the root to a leaf
- Each attribute-value pair along a path forms a conjunction.
 The leaf node holds the class prediction
- Rules are easier for humans to understand
- Example

```
IF age = "<=30" AND student = "no" THEN buys\_computer = "no"
IF age = "<=30" AND student = "yes" THEN buys\_computer = "yes"
IF age = "31...40" THEN buys\_computer = "yes"
IF age = ">40" AND credit\_rating = "excellent" THEN buys\_computer = "yes"
IF age = "<=30" AND credit\_rating = "fair" THEN buys\_computer = "no"
```

Questions?

- Why the method to generate a classification tree is a heuristic and not a guaranteed method?
 - Hint: Think of a situation where a is the best attribute, but the combination of "b and c" would actually be better than any of "a and b", or "a and c".
 - That is, knowing b and c you can classify, but knowing only a and b (or only a and c) you cannot.
- This shows that the attributes may not be independent. How could we deal with this?
 - Hint: Consider also combination of attributes, not only a, b, c, but also ab, bc, ca
- What is a problem with this approach?

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Example

Attribute 1	Attribute 2	Attribute 3	Class
Α	70	Т	C1
Α	90	Т	C2
А	85	F	C2
Α	95	F	C2
А	70	F	C1
В	90	Т	C1
В	78	F	C1
В	65	Т	C1
В	75	F	C1
С	80	Т	C2
С	70	Т	C2
С	80	F	C1
С	80	F	C1
С	96	F	C1
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Example II

Height	Hair	Eyes	Class
Short	Blond	Blue	+
Tall	Blond	Brown	-
Tall	Red	Blue	+
Short	Dark	Blue	-
Tall	Dark	Blue	-
Tall	Blond	Blue	+
Tall	Dark	Brown	-
Short	Blond	Brown	-

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Tree Induction

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 - Split the records based on an attribute test that optimizes certain criterion.
- Issues
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Stopping Criteria for Tree Induction

- Stop expanding a node when all the records belong to the same class
- Stop expanding a node when all the records have similar attribute values
- Early termination (to be discussed later)

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Characteristics of Decision Tree Induction

- Decision tree induction is a non-parametric approach for building classification models. In other words, it doesn't require any prior assumptions regarding the type of probability distributions satisfied by the class and other attributes.
- Finding an optimal decision tree is an NP-complete problem. Many decision tree algorithms emply a heuristic-based approach to guide their search in the vast hypothesis space. For example, the algorithm discussed in this unit uses a greedy, top-down, recursive partitioning startegy for growing a decision tree.

Characteristics of Decision Tree Induction (Cont'd)

- Techniques developed for constructing decision trees are computationally inexpensive, making it possible to quickly construct models even when the training set size is very large. Furthermore, once a decision tree has been built, classifying a test record is extremely fast, with a worst-case complexity of O(w), where w is the maximum depth of the tree.
- Decision tree, specially smaller-sized trees, are relatively easy to interpret.
- Decision tree algorithms are quite robust to the presence of noise.

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Characteristics of Decision Tree Induction (Cont'd)

- The presence of redundant attributes does not adversely affect the accuracy of decision trees. An attribute is redundant if it is strongly correlated with another attribute in the data. One of the two redundant attributes will not be used for splitting once the other attribute has been chosen.
- Studies have shown that the choice of impurity measures has little effect on the performance of decision tree induction algorithms.

Advantages of Decision Tree Based Classification

- Inexpensive to construct
- Extremely fast at classifying unknown records
- Easy to interpret for small-sized trees
- Accuracy is comparable to other classification techniques for many simple data sets

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