

Notes:

- If u know basics → easy time passing
- Then more complex exercises
- Same points for easy and difficult exercises
- For each assignment → Specification of points, and if documentation is required
- Based on pivots → there is a B ... → find minimal value for m and n, what is the smallest the matrix can be and the facts are still true
- 3 statements TRUE/FALSE,

*be alarmed → if you see a big matrix in the first part, there is sth you can do so that you can avoid rrefing or ... LOOK for

- based on graph → figure out the eig.vals. and their multiplicities:

-local/global max/min → that means the alg.multiplicity of the eig.val. is more than 1

- dim ColA, dim NullA, dim NullA.T, ..., → dimensions of fundamental subspaces

-differential equation (less complex, with 2 equations, NO mixing problem, just with equation stated)

- you get $\det(A)$ and you need to calculate ... (something with K) combination of $\det(A)$ and $\det(B)$
 $\det(AB) = \det(A) \cdot \det(B)$

- you get a system → put it to the matrix → in the next part you get echelon form and you have to deduce rank, nullspace(=solution), Assume that find x-s that solves the system, if there are free vars you need to set them to sth too (the easiest is to set them to 0) → give PVF.

(there isn't the b/result vector in Nullspace!) → so it is 0-vector

- True/Fals – if it always has a solution, ...

- Cofactor expansion (3 unknowns in 3x3 matrix)

- 3. Vector is dep. On the first 2 → you need to find its lin.comb (it is first part so you should not use rrf but find sth else to figure it out / look for multiples)

- Dep./Indep.: It is dep. if it contains 0-vector, if one vector is multiple of the other, ...
- You get a vector a , check if it is orthogonal? \Rightarrow matrix multiplication?
- You get a basis for a subspace of \mathbb{R}^4 \Rightarrow find its orthogonal complement (= it is the nullspace of the transposed vectors)

PART2:

- *some surprise with the mixing problem

1.

- o U get xyz such that the expression=0 (plain equation, plane spanned by 2 vectors)
- o Find its nullspace and you will get its vectors ... ?

Projection

- a. Project v onto x ... (you can use the "classic" projection or the "least square")
 - b. Calculate a Distance $||\text{projection} - \dots||$
 - c. You get 2 vectors in a null space (you cannot know if they are orthogonal \Rightarrow GramSchmidt)
2. Mixing problem:
- a. Same solution as we have already seen but there are different questions (4):
 - i. How much will be in tank-x at time t
 - ii. At what time it will be quarter of the original
 - iii. In the long run (limit) !!! \Rightarrow to 0 or to ∞ !!!
 - iv. + surprise
3. One set of 2 vectors and one with 3 \Rightarrow when you put them together they are not necessarily lind.indep.
4. Regression
5. SVD (similar to one we had)