

Exercise 1:

Having mastered the intricacies of random forests, our medical research team has set eyes on yet another (and indeed very central) topic in machine learning: **tuning**. Researcher Laetitia, who has vigorously studied the I2ML lecture materials, is asked to explain tuning in simple terms to her colleagues: *"Hyperparameter tuning, often abbreviated as tuning, can be broken down to one simple formula:*

$$\min_{\boldsymbol{\lambda} \in \tilde{\Lambda}} \widehat{\text{GE}}(\mathcal{I}, \mathcal{J}, \rho, \boldsymbol{\lambda}). \quad (1)$$

Researchers Son and Holger seem to have not studied the materials as engaged as Laetitia, since they cannot make sense of the expression above.

- 1) Explain hyperparameter tuning in your own words, using the formula above. What do data scientists mean when they call it a bi-level optimization problem?

A tuning problem consists of several elements:

- A data set \mathcal{D} ,
- A learner \mathcal{I} ,
- d hyperparameters of the learner and their configuration space $\tilde{\Lambda} = \tilde{\Lambda}_1 \times \tilde{\Lambda}_2 \times \dots \times \tilde{\Lambda}_d$,
- A performance measure ρ to estimate the generalization error, as determined by the application
- A (resampling) procedure \mathcal{J} for estimating the predictive performance

Son finds himself wondering how this would translate to their specific research problem. As before, they try to predict whether a patient admitted to the hospital will require intensive care, a binary classification task with target space $\mathcal{Y} = \{0, 1\}$. The feature space is the same as before: $\mathcal{X} = (\mathbb{R}_0^+)^3$, with $\mathbf{x}^{(i)} = (x_{age}, x_{blood\ pressure}, x_{weight})^{(i)} \in \mathcal{X}$ for $i = 1, 2, \dots, n$ observations.

- 2) Given a data set \mathcal{D} , a random forest learner \mathcal{I} , and our research group's problem, write down an example for a specific tuning problem using the list above.

The research group wants to apply the tuning procedure and get as best an estimate of the generalization error as they can. Holger tunes a learner with a simple 5-fold cross-validation (CV), training 5 models for each of the 100 hyperparameter configurations $\boldsymbol{\lambda}_i$, $i = 1, \dots, 100$ generated by random search. The unseen CV splits are used to estimate the performance, and the best-performing hyperparameter configuration $\boldsymbol{\lambda}^*$, which yielded an average accuracy of $\rho_{ACC} = 0.92$, is chosen to train the final model on the entire data set.

- 3) Does the final model result in an expected accuracy ρ_{ACC} wrt new, unseen observations equal to, lower or higher than 0.92?