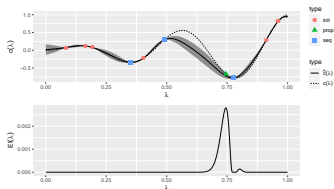


# Introduction to Machine Learning

## Hyperparameter Tuning - Advanced Tuning Techniques

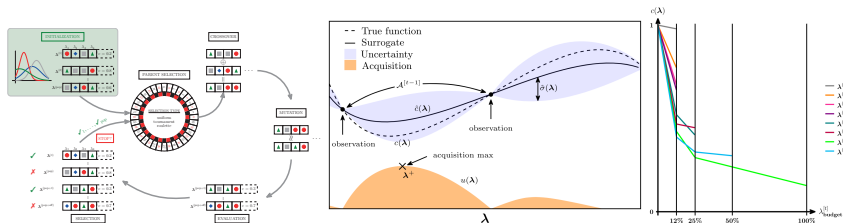


### Learning goals

- Understand the idea of model based optimization
- Be able to explain the terms 'surrogate model' and 'expected improvement'
- Understand the idea of hyperband

# HPO – MANY APPROACHES

- Evolutionary algorithms
- Bayesian / model-based optimization
- Multi-fidelity optimization, e.g. Hyperband

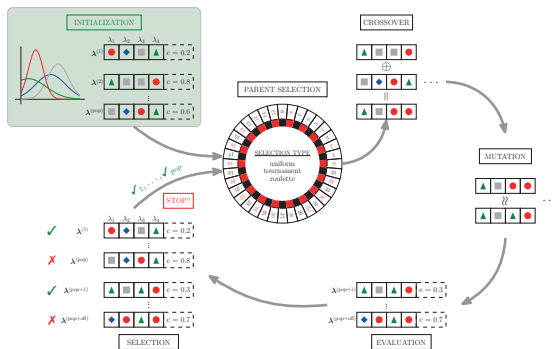


HPO methods can be characterized by:

- how the exploration vs. exploitation trade-off is handled
- how the inference vs. search trade-off is handled

Further aspects: Parallelizability, local vs. global behavior, handling of noisy observations, multifidelity and search space complexity.

# EVOLUTIONARY STRATEGIES



- Are a class of stochastic population-based optimization methods inspired by the concepts of biological evolution
- Are applicable to HPO since they do not require gradients
- Mutation is the (randomized) change of one or a few HP values in a configuration.
- Crossover creates a new HPC by (randomly) mixing the values of two other configurations.

# BAYESIAN OPTIMIZATION

BO sequentially iterates:

❶ **Approximate**  $\lambda \mapsto c(\lambda)$

by (nonlin) regression model  $\hat{c}(\lambda)$ , from evaluated configurations (archive)

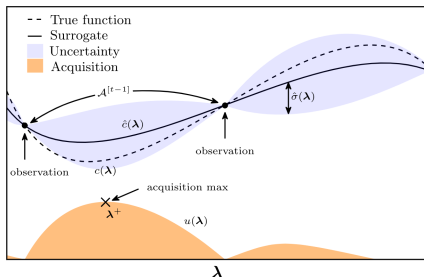
❷ **Propose candidates** via

optimizing an acquisition function that is based on the surrogate  $\hat{c}(\lambda)$

❸ **Evaluate** candidate(s)

proposed in 2, then go to 1

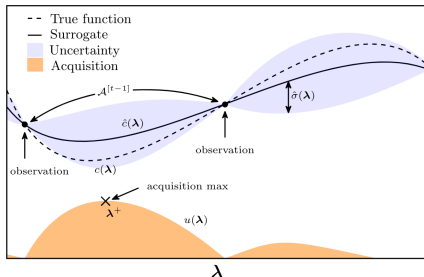
Important trade-off: **Exploration** (evaluate candidates in under-explored areas) vs. **exploitation** (search near promising areas)



# BAYESIAN OPTIMIZATION

## Surrogate Model:

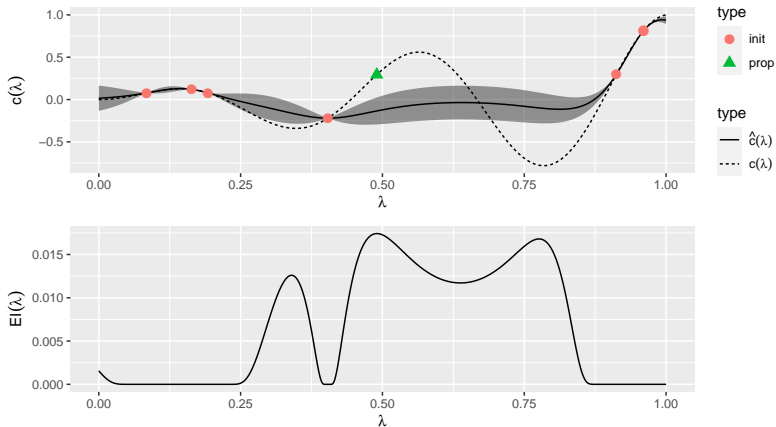
- Probabilistic modeling of  $C(\lambda) \sim (\hat{c}(\lambda), \hat{\sigma}(\lambda))$  with posterior mean  $\hat{c}(\lambda)$  and uncertainty  $\hat{\sigma}(\lambda)$ .
- Typical choices for numeric spaces are Gaussian Processes; random forests for mixed spaces



## Acquisition Function:

- Balance exploration (high  $\hat{\sigma}$ ) vs. exploitation (low  $\hat{c}$ ).
- Lower confidence bound (LCB):  $a(\lambda) = \hat{c}(\lambda) - \kappa \cdot \hat{\sigma}(\lambda)$
- Expected improvement (EI):  $a(\lambda) = \mathbb{E} [\max \{c_{\min} - C(\lambda), 0\}]$   
where  $(c_{\min})$  is best cost value from archive
- Optimizing  $a(\lambda)$  is still difficult, but cheap(er)

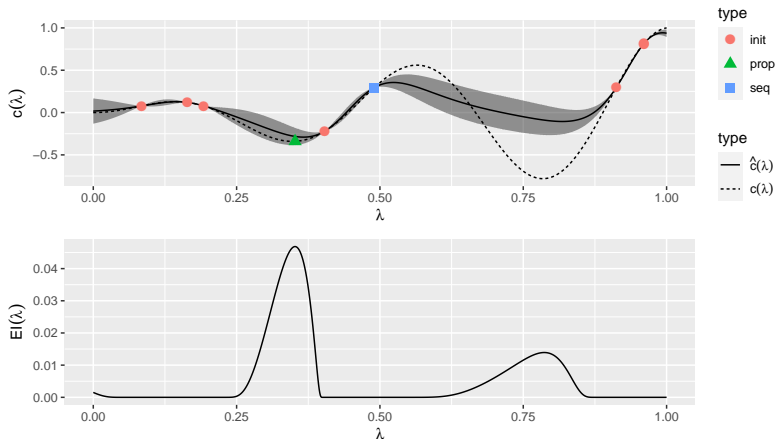
# BAYESIAN OPTIMIZATION



Upper plot: The surrogate model (black, solid) models the *unknown* relationship between input and output (black, dashed) based on the initial design (red points).

Lower plot: Mean and variance of the surrogate model are used to derive the expected improvement (EI) criterion. The point that maximizes the EI is proposed (green point).

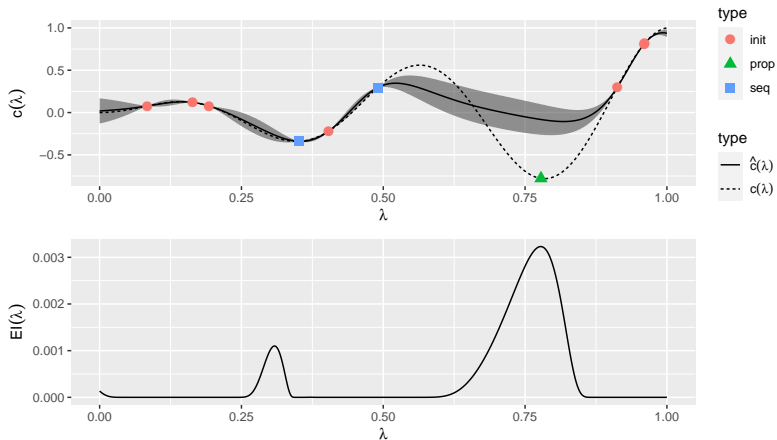
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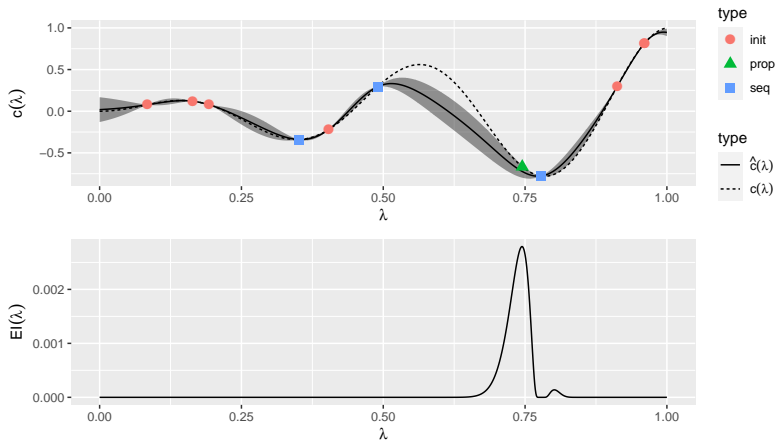


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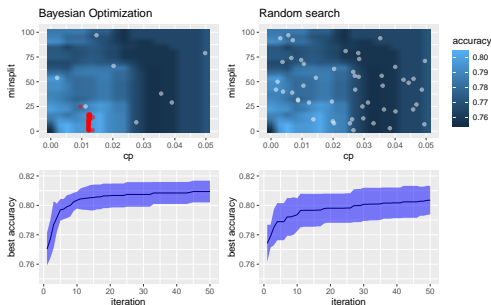


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# BAYESIAN OPTIMIZATION

Since we use the sequentially updated surrogate model predictions of performance to propose new configurations, we are guided to “interesting” regions of  $\Lambda$  and avoid irrelevant evaluations:



**Figure:** Tuning complexity and minimal node size for splits for CART on the titanic data (10-fold CV maximizing accuracy).

Left panel: BO, 50 configurations; right panel: random search, 50 iterations.

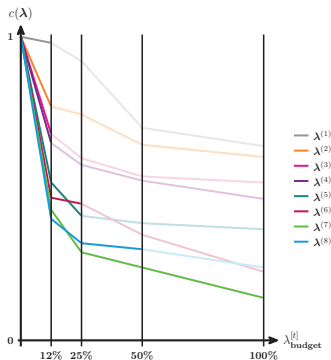
Top panel: one run (initial design of BO is white); bottom panel: mean  $\pm$  std of 10 runs.

# MULTIFIDELITY OPTIMIZATION

- Prerequisite: Fidelity HP  $\lambda_{\text{fid}}$ , i.e., a component of  $\lambda$ , which influences the computational cost of the fitting procedure in a monotonically increasing manner
- Methods of multifidelity optimization in HPO are all tuning approaches that can efficiently handle a  $\mathcal{I}$  with a HP  $\lambda_{\text{fid}}$
- The lower we set  $\lambda_{\text{fid}}$ , the more points we can explore in our search space, albeit with much less reliable information w.r.t. their true performance.
- We assume to know box-constraints of  $\lambda_{\text{fid}}$ , so  $\lambda_{\text{fid}} \in [\lambda_{\text{fid}}^{\text{low}}, \lambda_{\text{fid}}^{\text{upp}}]$ , where the upper limit implies the highest fidelity returning values closest to the true objective value at the highest computational cost.

# SUCCESSIVE HALVING

- Races down set of HPCs to the best
- Idea: Discard bad configurations early
- Train HPCs with fraction of full budget (SGD epochs, training set size); the control param for this is called **multi-fidelity HP**
- Continue with better  $1/\eta$  fraction of HPCs (w.r.t  $\widehat{GE}$ ); with  $\eta$  times budget (usually  $\eta = 2, 3$ )
- Repeat until budget depleted or single HPC remains



# MULTIFIDELITY OPTIMIZATION – HYPERBAND

## Problem with SH

- Good HPCs could be killed off too early, depends on evaluation schedule

## Solution: Hyperband

- Repeat SH with different start budgets  $\lambda_{\text{fid}}^{[0]}$  and initial number of HPCs  $p^{[0]}$
- Each SH run is called bracket
- Each bracket consumes ca. the same budget

For  $\eta = 4$

bracket 3		
$t$	$\lambda_{\text{fid}}^{[t]}$	$p_3^{[t]}$
0	1	82
1	4	20
2	16	5
3	64	1

bracket 2		
$t$	$\lambda_{\text{fid}}^{[t]}$	$p_2^{[t]}$
0	4	27
1	16	6
2	64	1

bracket 1		
$t$	$\lambda_{\text{fid}}^{[t]}$	$p_1^{[t]}$
0	16	10
1	64	2

bracket 0		
$t$	$\lambda_{\text{fid}}^{[t]}$	$p_0^{[t]}$
0	64	5

# MORE TUNING ALGORITHMS:

Other advanced techniques besides model-based optimization and the hyperband algorithm are:

- Stochastic local search, e.g., simulated annealing
- Genetic algorithms / CMAES
- Iterated F-Racing
- Many more . . .

For more information see *Hyperparameter Optimization: Foundations, Algorithms, Best Practices and Open Challenges*, Bischl (2021)