

Chapters 11

Hash Functions

Dr. Shin-Ming Cheng



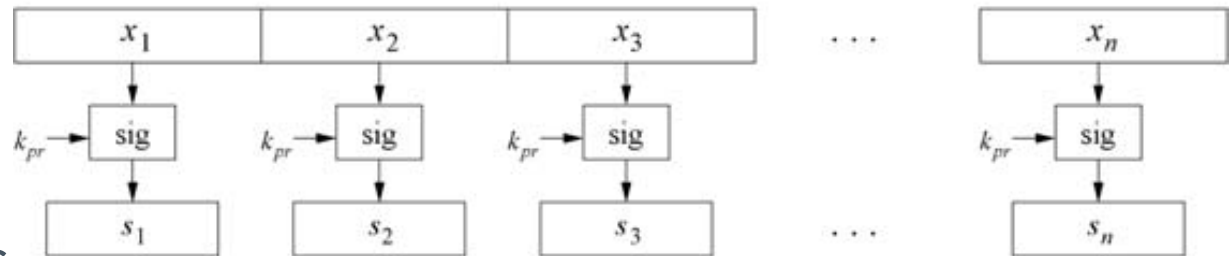
Hash Functions

- › Why we need hash functions
- › How does it work
- › Security properties
- › Algorithms
- › The Secure Hash Algorithm MD4, SHA-1, SHA-512



Motivation

- › Naive signing of long messages generates a signature of same length.



- › Problems
 - Computational overhead
 - Message overhead
 - Security limitations
- › Instead of signing the whole message, sign only a digest (=hash)
 - Also secure, but much faster

Motivation

› Encryption

- Provides **confidentiality**
- Does NOT necessarily provide **integrity of data**
 - › Countermeasure: Use cryptographic function to get a check-value and send it with data

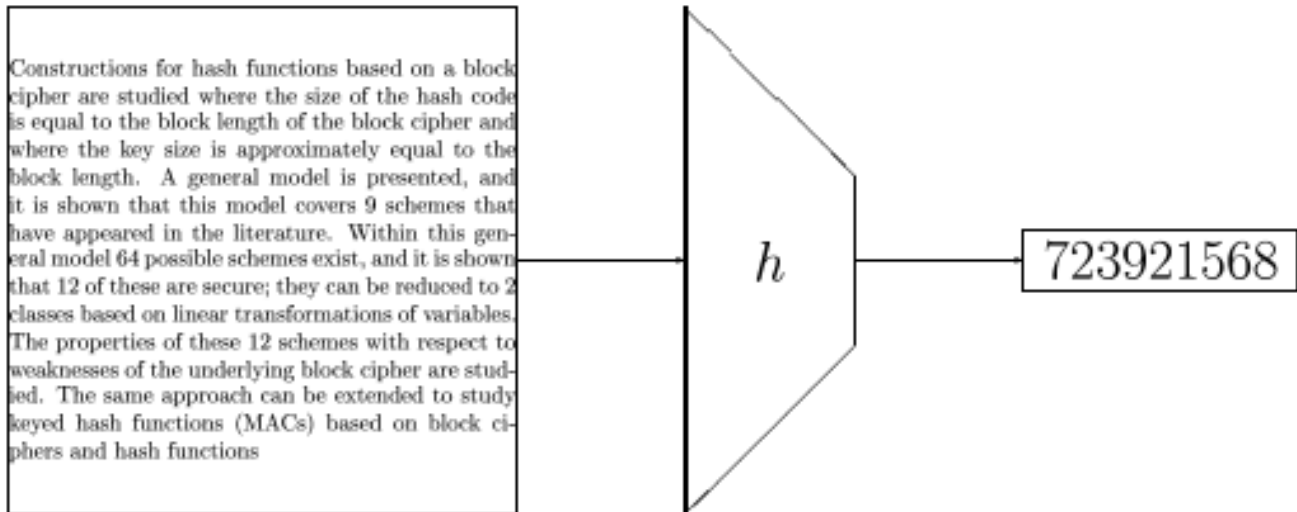
› Two mechanisms for data integrity

- Hash functions
 - › A special type of Manipulation Detection Code (MDC)
- Message Authentication Codes (MAC)
 - › A keyed version of a hash function



Hash Function

- › Efficient function mapping binary strings of **arbitrary length** to binary strings of **fixed length**, called the **hash-value** or **hash-code**



Hash Functions

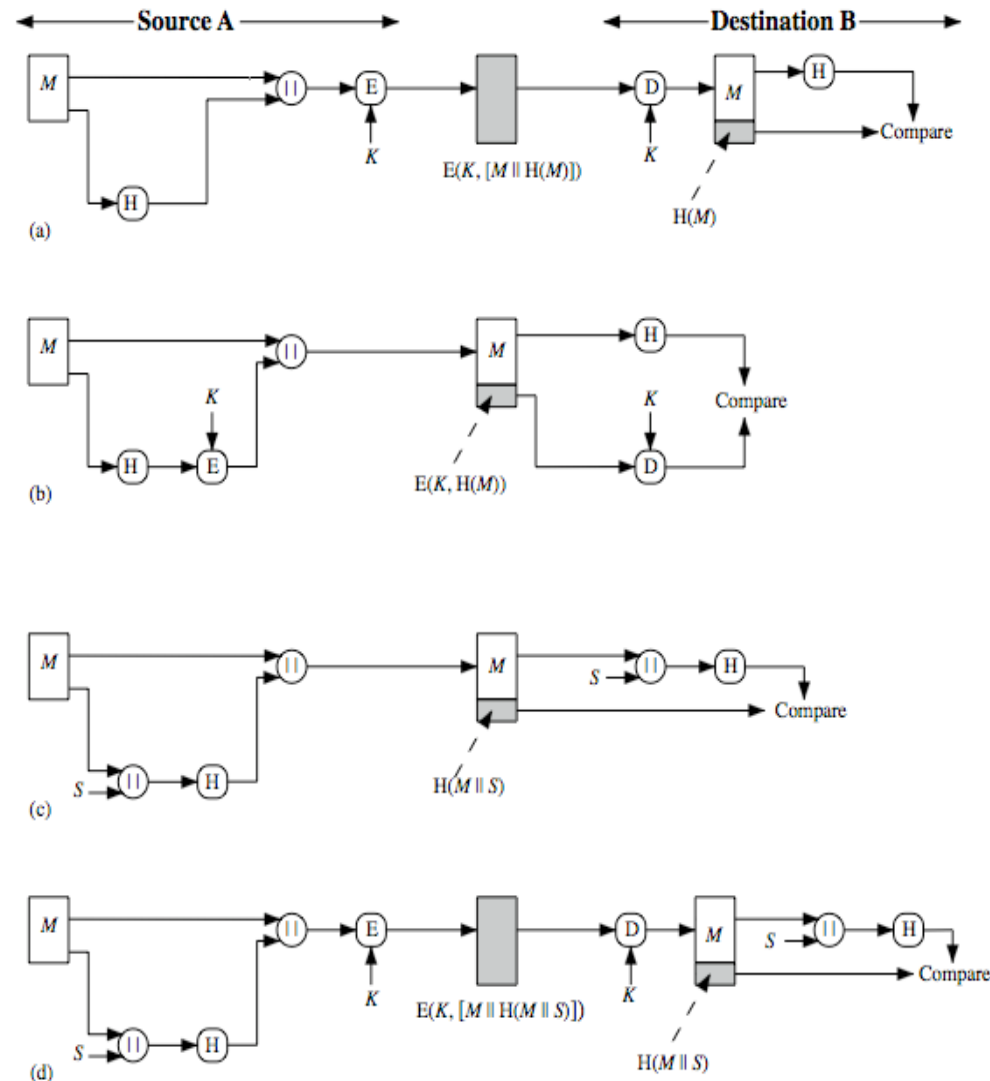
- › Condenses arbitrary message to fixed size

$$h = H(M)$$

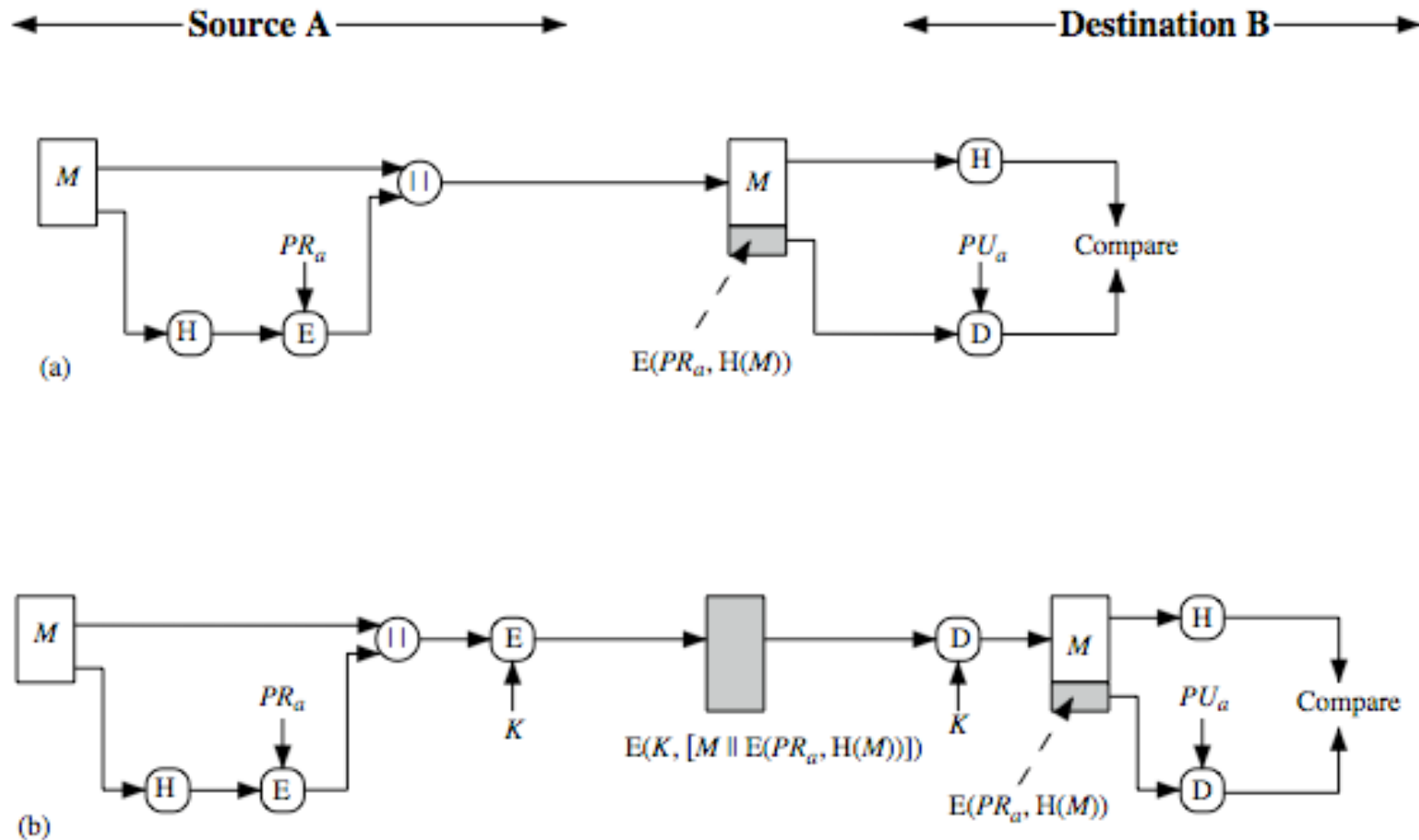
- › Usually assume hash function is public
- › Hash used to detect changes to message
- › A cryptographic hash function
 - computationally infeasible to find data mapping to specific hash (**one-way** property)
 - computationally infeasible to find two data to same hash (**collision-free** property)

Hash Functions & Message Authentication

- › the two parties share a common secret value S .
- › A computes the hash value over the concatenation of M and S and appends the resulting hash value to M .
- › Because B possesses S , it can recompute the hash value to verify.



Hash Functions & Digital Signatures

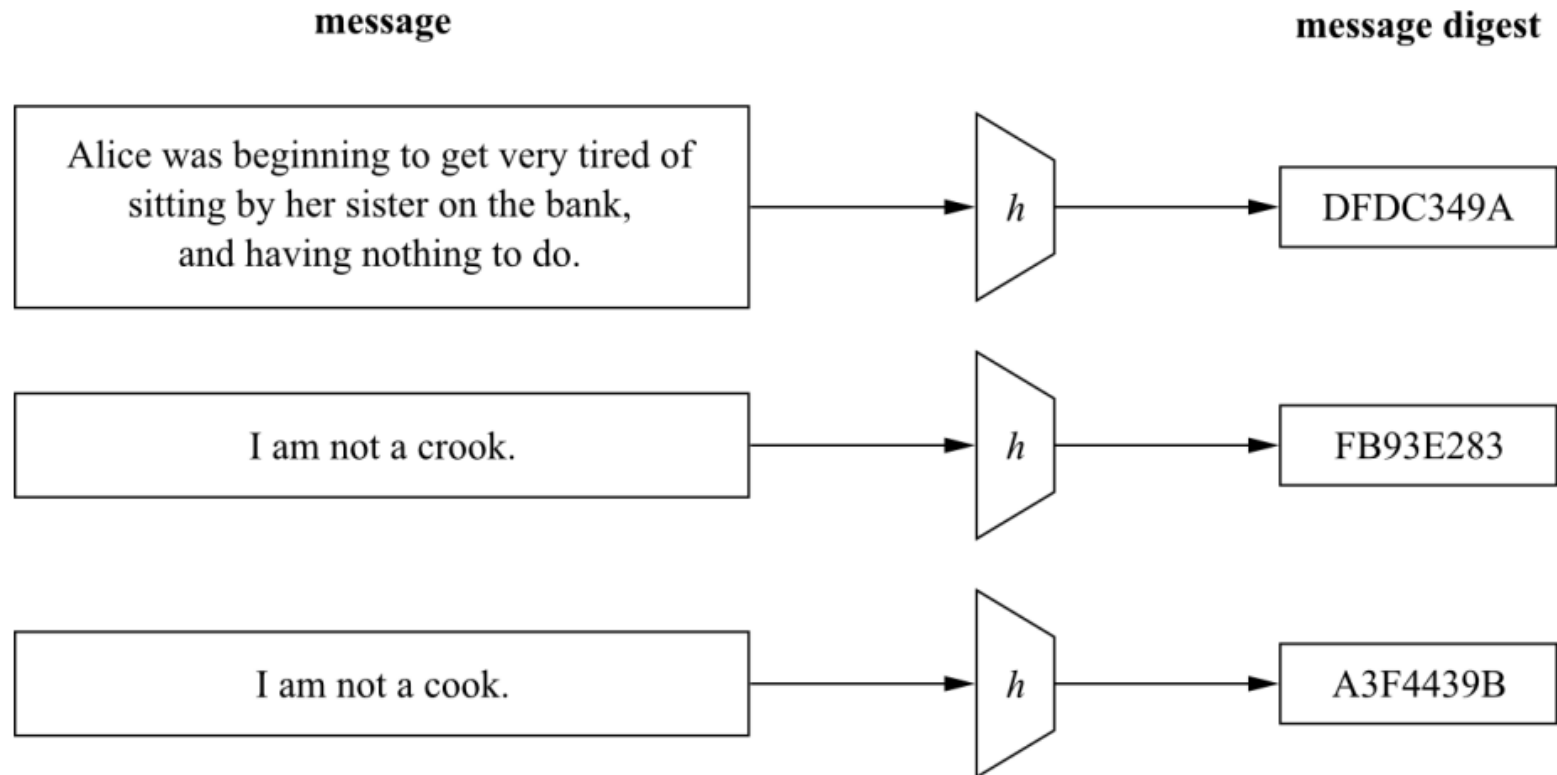


Other Hash Function Uses

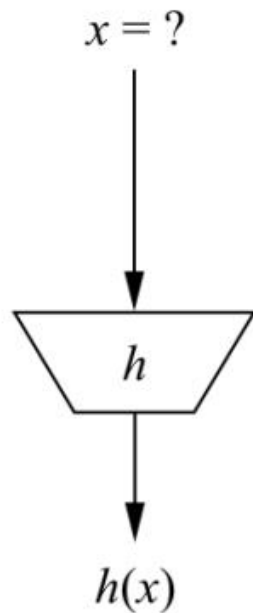
- › to create a one-way password file
 - store hash of password not actual password
- › for intrusion detection and virus detection
 - keep & check hash of files on system
- › pseudorandom function (PRF) or pseudorandom number generator (PRNG)



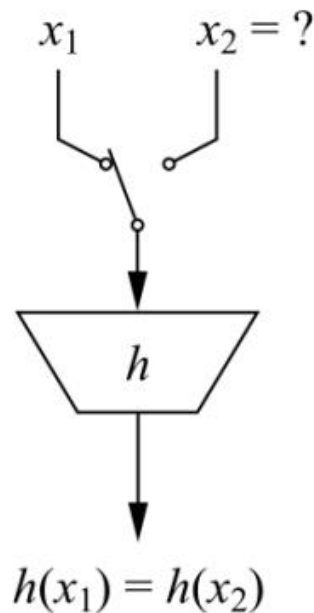
Principal input-output behavior of hash functions



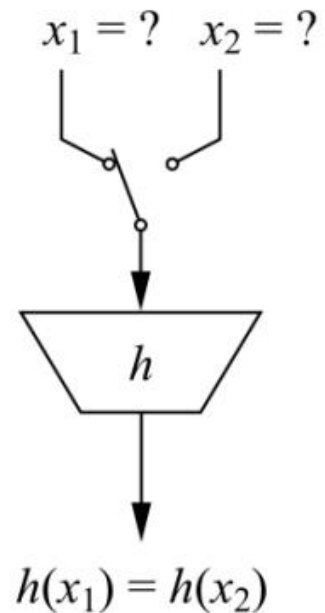
Security Properties



preimage resistance



second preimage
resistance



collision resistance

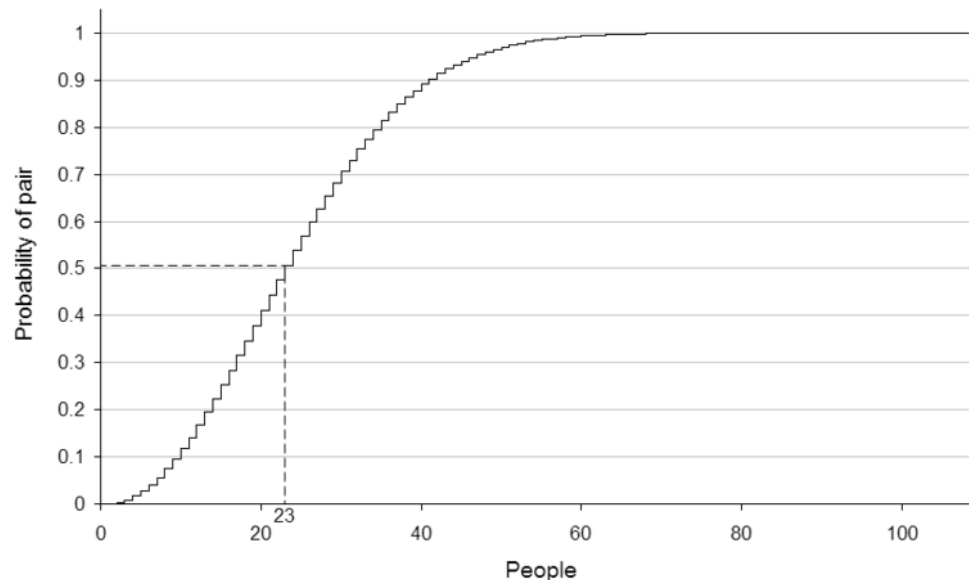
Security Properties

- › Preimage resistance:
 - For a given output z , it is impossible to find any input x such that $h(x) = z$,
 - $h(x)$ is one-way
- › Second preimage resistance:
 - Given x_1 , and thus $h(x_1)$, it is computationally infeasible to find any x_2 such that $h(x_1) = h(x_2)$
- › Collision resistance:
 - It is computationally infeasible to find any pairs $x_1 \neq x_2$ such that $h(x_1) = h(x_2)$



Security Properties

- › Collision resistance causes most problems
 - How hard is it to find a collision with a probability of 0.5?
 - Birthday Problem: How many people are needed such that two of them have the same birthday with a probability of 0.5?
 - › A counter-intuitive result



Security Properties

Birthday Paradox

- › It is harder to construct collision free hash functions than one-way hash functions due to the birthday paradox
- › If the function has output size of n bits, then we expect to find a collision after $2^{n/2}$ iterations
 - Whilst breaking the one-way property would require 2^n iterations on average
- › Hence to achieve a security level of 80 bits we need 160 bits of output

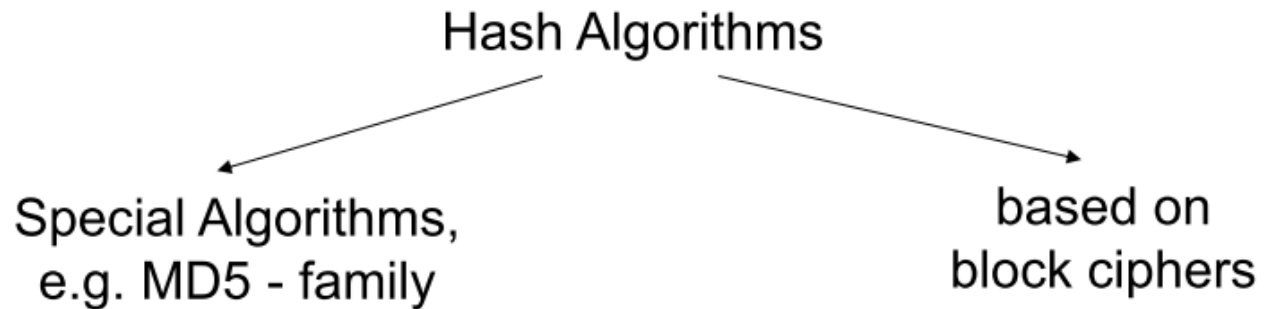


Security Properties

Birthday Attack

- › Given user prepared to sign a valid message x
- › opponent generates
 - $2^{m/2}$ variations x' of x , all with essentially the same meaning, and saves them
 - $2^{m/2}$ variations y' of a desired fraudulent message y
- › two sets of messages are compared to find pair with same hash
 - probability > 0.5 by birthday paradox
- › have user sign the valid message, then substitute the forgery which will have a valid signature

Algorithms



- › MD5 - family
- › SHA-1: output – 160-bit; input – 512-bit chunks of message x ; operations - bitwise AND, OR, XOR, complement and cyclic shifts
- › RIPE-MD 160: output – 160-bit; input – 512-bit chunks of message x ; operations – like in SHA-1, but two in parallel and combinations of them after each round

Hash from Block Ciphers

- › A hash function can be constructed from a block cipher E
- › There are a number of ways of doing this
 - All methods make use of a constant initial value IV
 - Some use a function g mapping n -bit inputs to keys
 - Pad the message into blocks x_0, x_1, \dots, x_t
 - Similar to CBC but without a key
 - The hash value is the final H_i in the iteration
 - › $H_0 = IV$
 - › $H_i = f(x_i, H_{i-1})$
- › Resulting hash is too small (64-bit)
 - Vulnerable to attack

MD4 (Message-Digest algorithm 4)

- › MD4 is a message digest algorithm (the fourth in a series) designed by Professor Ronald Rivest of MIT in 1990
- › It implements a cryptographic hash function for use in message integrity checks
- › The digest length is 128 bits
- › The algorithm has influenced later designs, such as the MD5, SHA-1, RIPEMD, and SHA-2 algorithms

MD4 Family

- › MD4: 3 rounds of 16 steps, output 128 bits
- › MD5: 4 rounds of 16 steps, output 128 bits
- › SHA-1: 4 rounds of 20 steps, output 160 bits
- › RIPEMD-160: 5 rounds of 16 steps, output 160 bits
- › SHA-2:
 - SHA-224: Truncated SHA-256, output 224 bits
 - SHA-256: 64 rounds of single steps, output 256 bits
 - SHA-384: Truncated SHA-512, output 384 bits
 - SHA-512: 80 rounds of single steps, output 512 bits

MD4

- › There are three functions of three variables
 - $f(u, v, w)$
 - $g(u, v, w)$
 - $h(u, v, w)$

which are just logical bitwise operations

- › A current hash state (H_1, H_2, H_3, H_4) of 32-bit values initialized with a fixed IV
- › There are various fixed constants (y_j, z_i, s_i)

MD4

- › The data stream is loaded 16 words at a time into $X[j]$, $0 \leq j < 16$
- › Execute the following steps
 - $(A, B, C, D) = (H_1, H_2, H_3, H_4)$
 - Execute Round 1
 - Execute Round 2
 - Execute Round 3
 - $(H_1, H_2, H_3, H_4) = (H_1 + A, H_2 + B, H_3 + C, H_4 + D)$
- › After all data has been read in, the output is the concatenation of the final value of H_1, H_2, H_3, H_4

MD4

› Round 1

– For $j = 0$ to 15 do

$$\triangleright t = A + f(B, C, D) + X[j] + y_j$$

$$\triangleright (A, B, C, D) = (D, t \ll s_j, B, C)$$

› Round 2

– For $j = 16$ to 31 do

$$\triangleright t = A + g(B, C, D) + X[j] + y_j$$

$$\triangleright (A, B, C, D) = (D, t \ll s_j, B, C)$$

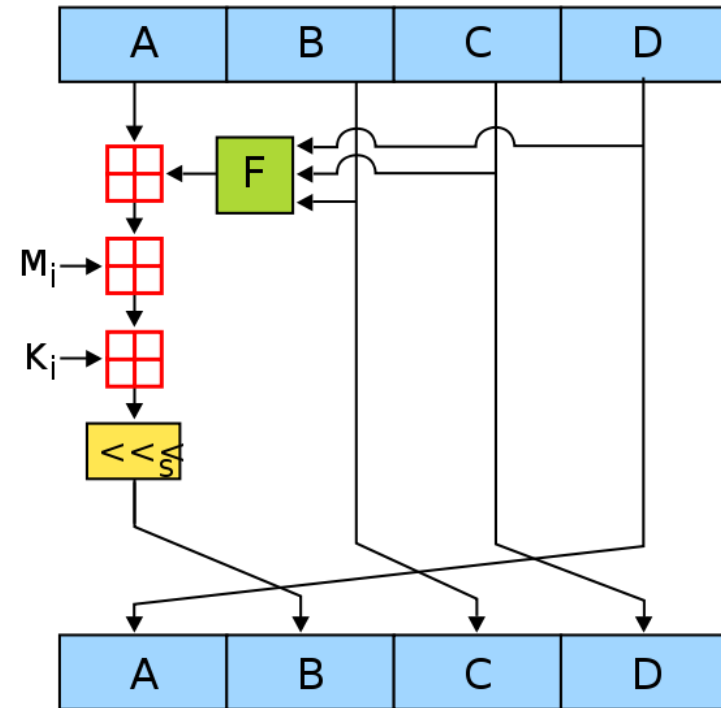
› Round 3

– For $j = 32$ to 47 do

$$\triangleright t = A + h(B, C, D) + X[j] + y_j$$

$$\triangleright (A, B, C, D) = (D, t \ll s_j, B, C)$$

› The symbol \ll denotes a bit-wise rotate to the left



Avalanche Effect

- › A small change in the input produces a large unpredictable change in the output
 - A basic design principle when designing hash functions
- › This design principle is typified in the MD4 family
- › Several hash functions in MD4 family are widely used
 - They are all iterative in nature
 - MD5 has been popular but is not as popular now as SHA-1
 - SHA-1 (Secure Hash Algorithm) is a US and ISO standard



Avalanche Effect

› Examples

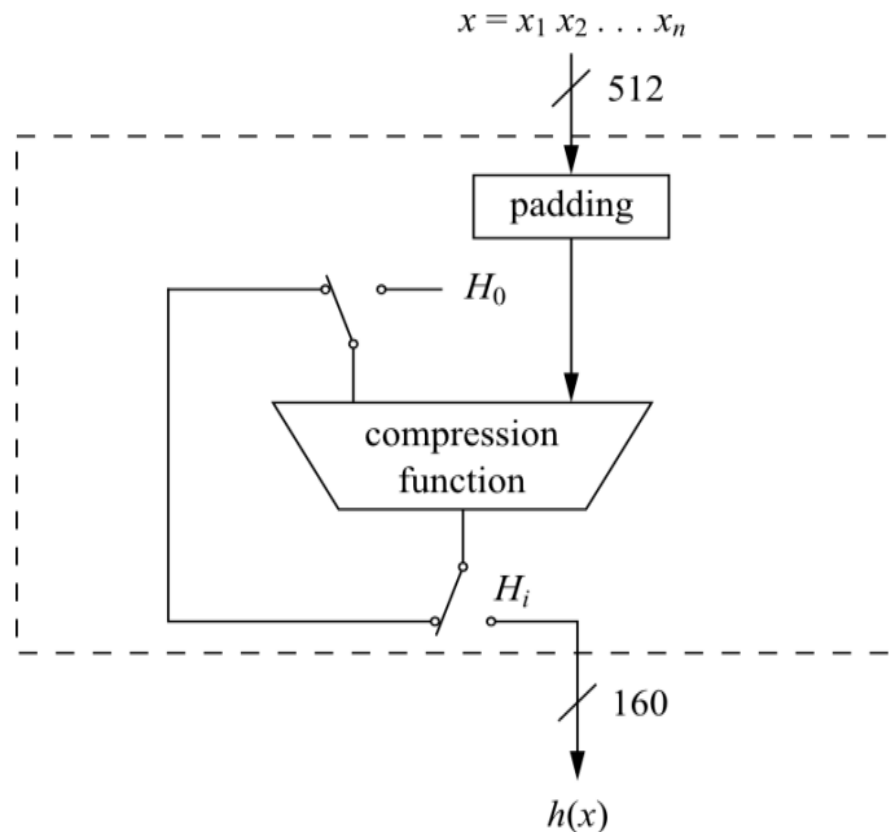
- MD5("The quick brown fox jumps over the lazy dog") = 9e107d9d372bb6826bd81d3542a419d6
- MD5("The quick brown fox jumps over the lazy cog") = 1055d3e698d289f2af8663725127bd4b
- SHA1("The quick brown fox jumps over the lazy dog") =
2fd4e1c67a2d28fced849ee1bb76e7391b93eb12
- SHA1("The quick brown fox jumps over the lazy cog") =
de9f2c7fd25e1b3afad3e85a0bd17d9b100db4b3

Secure Hash Algorithm

- › SHA originally designed by NIST & NSA in 1993
- › was revised in 1995 as SHA-1
- › US standard for use with DSA signature scheme
 - standard is FIPS 180-1 1995, also Internet RFC3174
 - the algorithm is SHA, the standard is SHS
- › based on design of MD4 with key differences
- › produces 160-bit hash values
- › SHA-2 is strongly recommended by NIST today
 - Four variants with output length 224, 256, 384, and 512 bits
 - › <http://csrc.nist.gov/CryptoToolkit/tkhash.html>

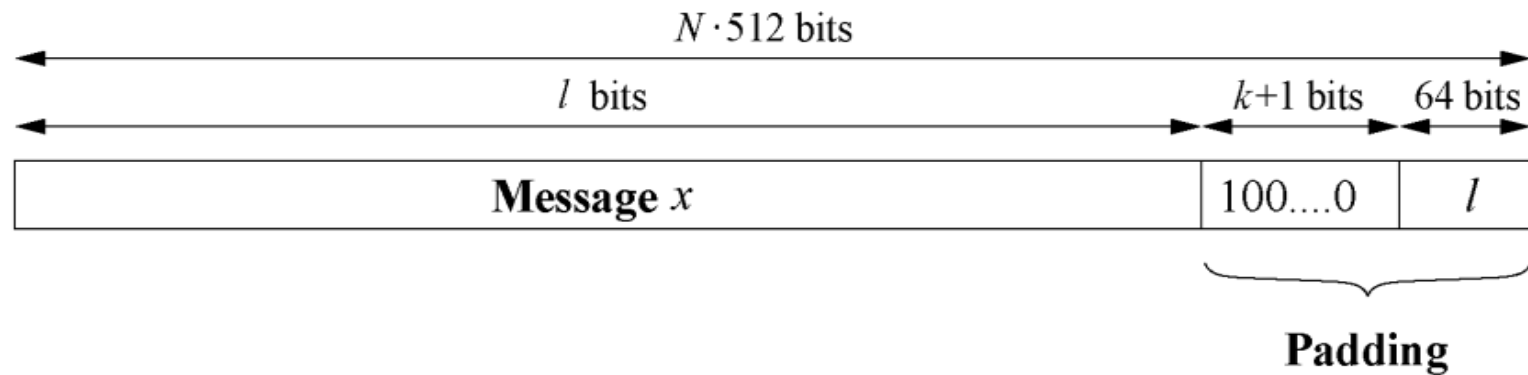
SHA-1 High Level Diagramm

- › Compression Function consists of 80 rounds which are divided into four stages of 20 rounds each



SHA-1: Padding

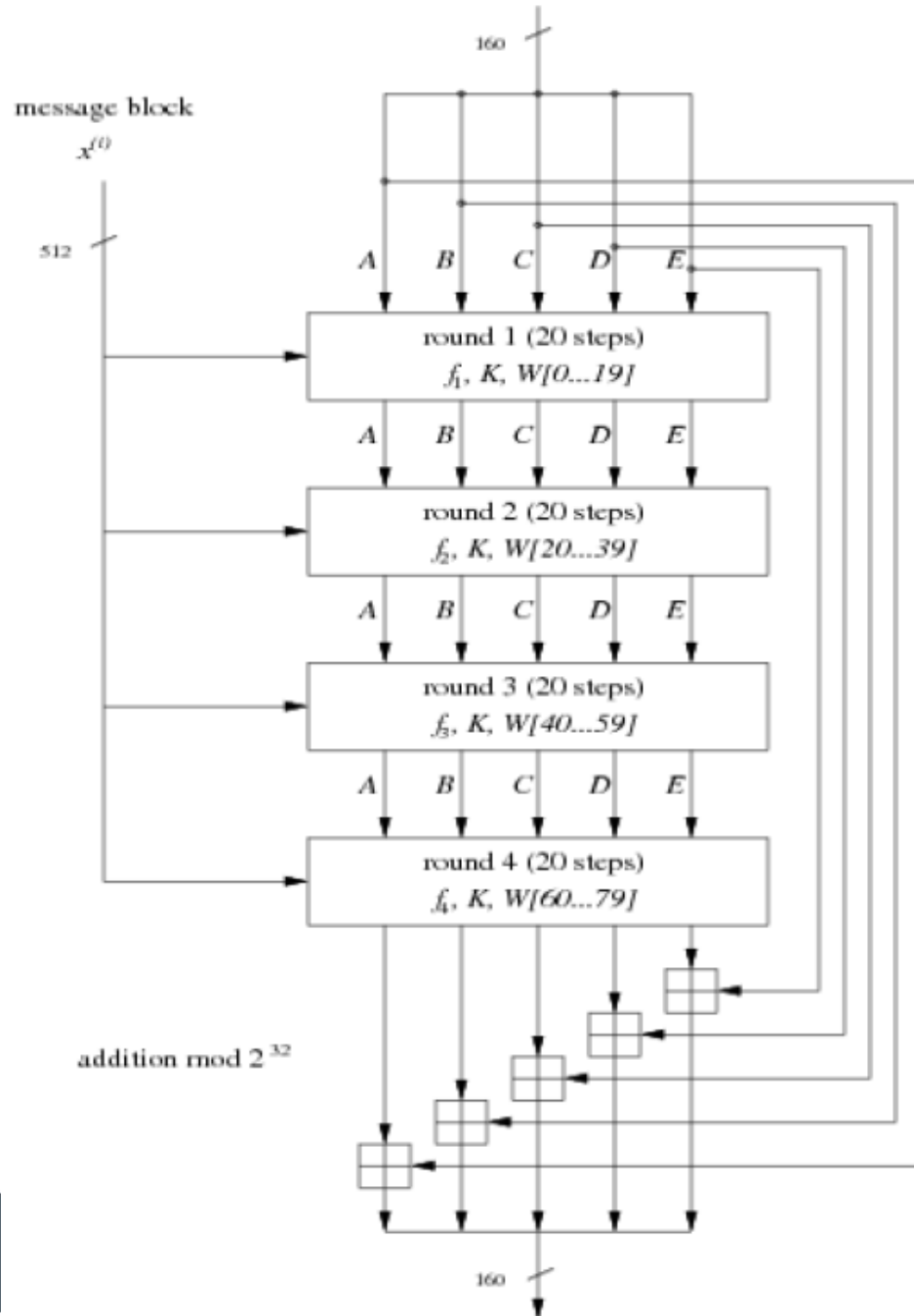
- › Message x has to be padded to fit a size of a multiple of 512 bit
- › $k \equiv 512 - 64 - 1 - l = 448 - (l + 1) \bmod 512$



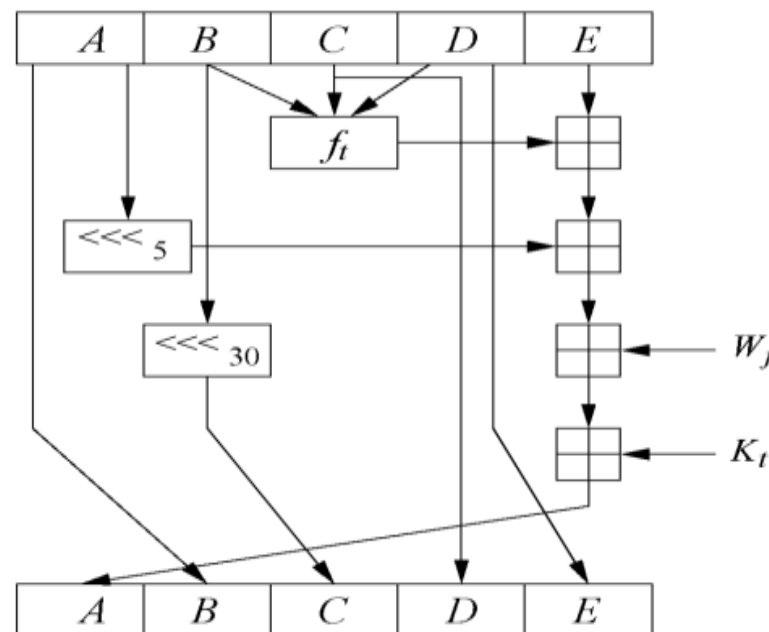
SHA-1: Hash Computation

- › Each message block x_i is processed in four stages with 20 rounds each
- › SHA-1 uses:
 - A message schedule which computes a 32-bit word W_0, W_1, \dots, W_{79} for each of the 80 rounds
 - Five working registers of size of 32 bits A, B, C, D, E
 - A hash value H_i consisting of five 32-bit words $H_i^{(0)}, H_i^{(1)}, H_i^{(2)}, H_i^{(3)}, H_i^{(4)}$
 - In the beginning, the hash value holds the initial value H_0 , which is replaced by a new hash value after the processing of each single message block
 - The final hash value H_n is equal to the output $h(x)$ of SHA-1

SHA-1: All four stages



SHA-1: Internals of a Round



Stage t	Round j	Constant K_t	Function f_t
1	00...19	$K=5A827999$	$f(B, C, D) = (B \wedge C) \vee (\neg B \wedge D)$
2	20...39	$K=6ED9DBA1$	$f(B, C, D) = B \oplus C \oplus D$
3	40...59	$K=8F1BBCDC$	$f(B, C, D) = (B \oplus C) \vee (B \oplus D) \vee (C \oplus D)$
4	60...70	$K=CA62C1D6$	$f(B, C, D) = B \oplus C \oplus D$

Collisions on SHA-1



› Collisions on SHA-1

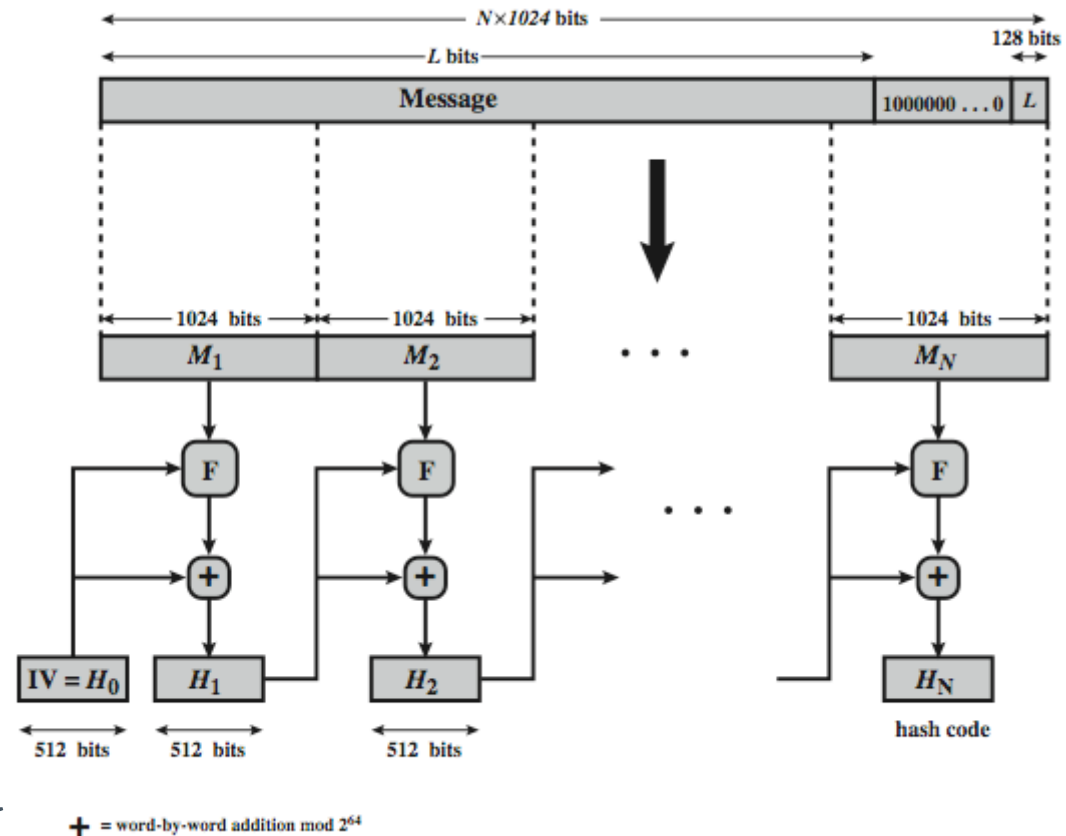
- 王小雲 - 山東大學 數學系
- Rump session of CRYPTO 2004
- Security: $2^{80} \rightarrow 2^{63}$ computations
- “Finding Collisions in the Full SHA-1”, CRYPTO 2005, Lecture Notes in Computer Science vol. 3621, pp. 17-36

› Complexity of 2^{52} ?

- McDonald, Hawkes, and Pieprzyk presented a hash collision attack with claimed complexity 2^{52} at the Rump session of Eurocrypt 2009
- However, the accompanying paper has been withdrawn due to the authors' discovery that their estimate was incorrect

SHA-512 Overview

- › Append padding bits
- › Process the message in 1024-bit blocks
 - Each round takes as input the 512-bit buffer value H_i and updates the contents of that buffer
- › Output the final state value

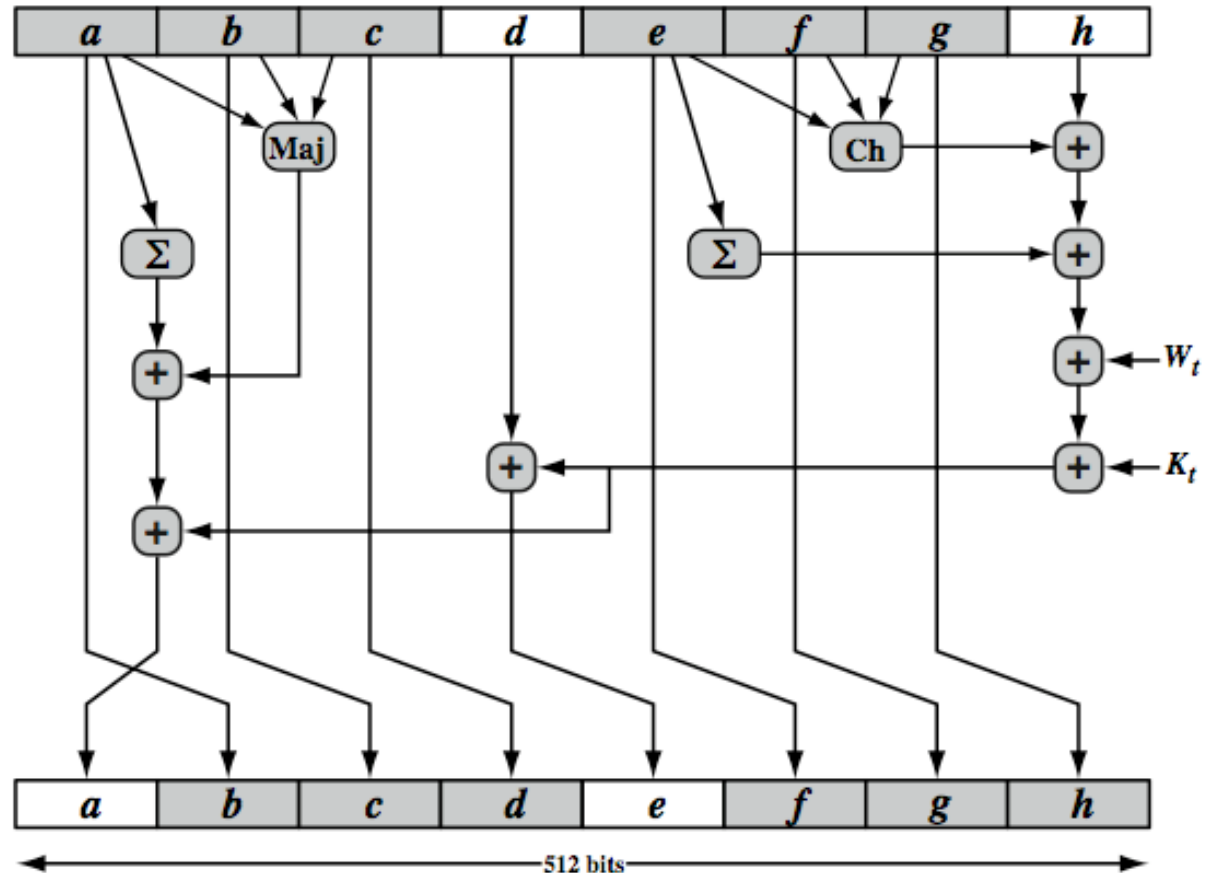


SHA-512 Compression Function

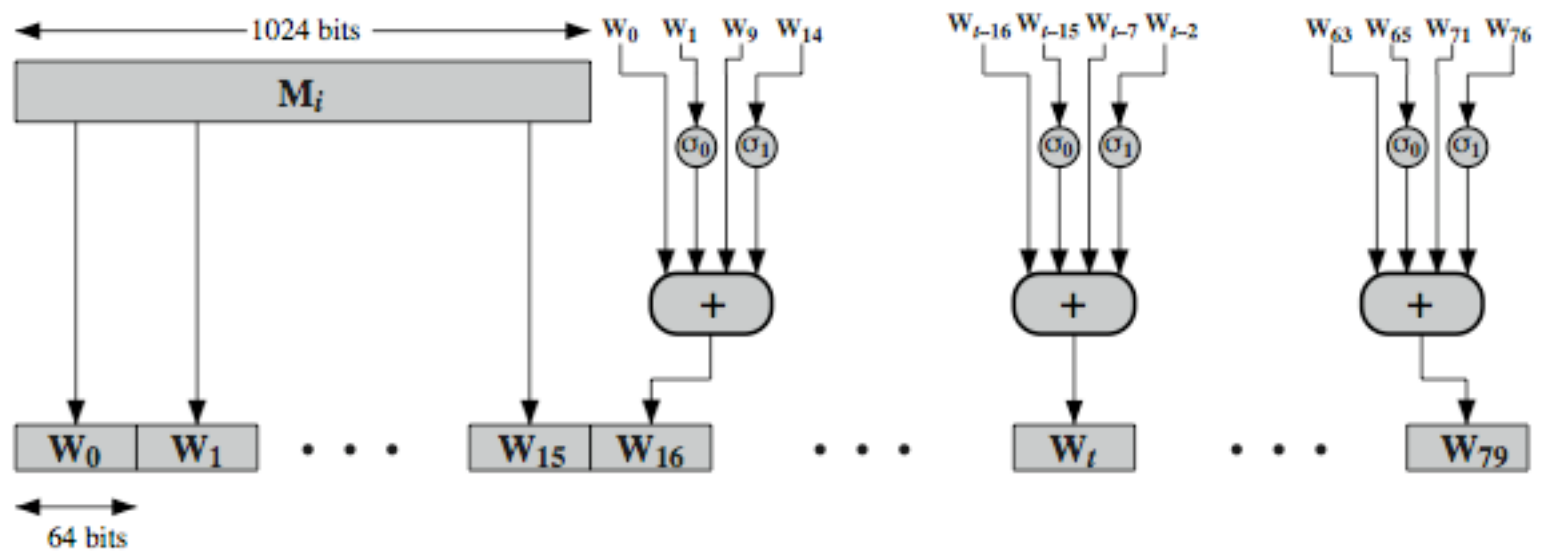
- › heart of the algorithm
- › processing message in 1024-bit blocks
- › consists of 80 rounds
 - updating a 512-bit buffer
 - using a 64-bit value W_t derived from the current message block
 - and a round constant based on cube root of first 80 prime numbers



SHA-512 Round Function



SHA-512 Round Function



SHA-3

- › The **NIST hash function competition** is an open competition held by the US NIST for a new **SHA-3** function to replace the older SHA-1 and SHA-2
 - Submissions were due Oct. 2008, with a list of candidates accepted for the first round published Dec. 2008
 - The list of 14 candidates accepted to Round 2 was published on July 24, 2009
 - Five SHA-3 finalists - BLAKE, Grøstl, JH, Keccak, and Skein advanced to the third (and final) round on December 9, 2010
 - October 2, 2012, [Keccak](#) was selected as the winner

Lessons Learned

- › Hash functions are keyless. The two most important applications of hash functions are their use in digital signatures and in message authentication codes such as HMAC
- › The three security requirements for hash functions are one-wayness, second preimage resistance and collision resistance
- › Hash functions should have at least 160-bit output length in order to withstand collision attacks; 256 bit or more is desirable for long-term security
- › MD5, which was widely used, is insecure. Serious security weaknesses have been found in SHA-1, and the hash functions should be phased out. The SHA-2 algorithms all appear to be secure
- › The ongoing SHA-3 competition will result in new standardized hash functions in a few years