

# TURBO

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## Motion in a Straight Line

Class 11 Physics • Complete Formula Sheet

Sr.	Concept	Formulas	Other Information
1	Position vector ( $\vec{r}$ )	$\vec{r}_A = x_1\hat{i} + y_1\hat{j} + z_1\hat{k}$ $\vec{r}_B = x_2\hat{i} + y_2\hat{j} + z_2\hat{k}$	Here, $\vec{r}_A(x_1, y_1)$ and $\vec{r}_B(x_2, y_2)$ are the position vectors.
2	Displacement vector ( $\Delta\vec{r}$ )	$\Delta\vec{r} = (x_2 - x_1)\hat{i} + (y_2 - y_1)\hat{j} + (z_2 - z_1)\hat{k}$ Displacement vector $\Delta\vec{r} = \vec{r}_2 - \vec{r}_1$	Vector quantity representing change in position.
3	Average speed ( $v_{\text{avg}}$ )	$v_{\text{avg}} = \frac{\text{Total distance travelled}}{\text{Total time taken}} = \frac{\Delta s}{\Delta t}$	$\Delta s$ = distance travelled $\Delta t$ = time taken
4	Instantaneous speed ( $v_{\text{inst}}$ )	$v_{\text{inst}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta s}{\Delta t} = \frac{ds}{dt}$	$ds$ = short displacement $dt$ = short time interval
5	Average speed (different uniform speeds in different time intervals)	$v_{\text{avg}} = \frac{s_1 + s_2 + s_3 + \dots + s_n}{t_1 + t_2 + t_3 + \dots + t_n}$ $= \frac{v_1 t_1 + v_2 t_2 + v_3 t_3 + \dots}{t_1 + t_2 + t_3 + \dots}$ If $t_1 = t_2 = t_3 = \dots = t_n$ , then $v_{\text{avg}} = \frac{v_1 + v_2 + \dots + v_n}{n}$	Different uniform speeds $v_1, v_2, v_3, \dots, v_n$ in different time intervals $t_1, t_2, \dots, t_n$ respectively.
6	Average speed (equal distances with different speeds)	$v_{\text{avg}} = \frac{d}{\frac{d}{nv_1} + \frac{d}{nv_2} + \dots + \frac{d}{nv_n}}$ For 2 equal distances: $v_{\text{avg}} = \frac{2v_1 v_2}{v_1 + v_2}$	Particle moves distance $d$ in $n$ equal parts with different speeds $v_1, v_2, \dots, v_n$ .
7	Average velocity	$\vec{v}_{\text{avg}} = \frac{\text{Net Displacement}}{\text{Time taken}} = \frac{\vec{r}_f - \vec{r}_i}{t_f - t_i} = \frac{\Delta\vec{r}}{\Delta t}$	$\vec{r}_f$ = final position $\vec{r}_i$ = initial position $\Delta t = t_f - t_i$ = time interval
8	Velocity in vector form	$\vec{v} = \frac{d\vec{r}}{dt} = \frac{d(x\hat{i} + y\hat{j} + z\hat{k})}{dt}$ $= \frac{dx}{dt}\hat{i} + \frac{dy}{dt}\hat{j} + \frac{dz}{dt}\hat{k}$ $\vec{v} = v_x\hat{i} + v_y\hat{j} + v_z\hat{k}$	Velocity can be positive, negative or zero.
9	Average acceleration	$\vec{a}_{\text{avg}} = \frac{\text{Total change in velocity}}{\text{Total time taken}} = \frac{\Delta\vec{v}}{\Delta t}$	$\Delta\vec{v}$ = change in velocity $\Delta t$ = time interval
10	Acceleration in vector form	$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d(v_x\hat{i} + v_y\hat{j} + v_z\hat{k})}{dt}$ $= \frac{dv_x}{dt}\hat{i} + \frac{dv_y}{dt}\hat{j} + \frac{dv_z}{dt}\hat{k}$ $\vec{a} = a_x\hat{i} + a_y\hat{j} + a_z\hat{k}$	$d\vec{v}$ = change in velocity $dt$ = time interval
11	Instantaneous acceleration	$a_{\text{inst}} = \frac{dv}{dt} = \frac{d^2x}{dt^2} = \frac{d^2x}{dt^2}$ When $v$ is function of position ( $x$ ): $a_{\text{inst}} = \frac{dv}{dx} \cdot \frac{dx}{dt} = v \frac{dv}{dx}$	$a_{\text{inst}}$ = instantaneous acceleration $dx/dt$ = instantaneous velocity
12	Equations of motion	<b>Scalar Form:</b> $v = u + at$ $s = ut + \frac{1}{2}at^2$ $v^2 = u^2 + 2as$ <b>Vector Form:</b> $\vec{v} = \vec{u} + \vec{a}t$ $\vec{s} = \vec{u}t + \frac{1}{2}\vec{a}t^2$ $\vec{v} \cdot \vec{v} = \vec{u} \cdot \vec{u} + 2\vec{a} \cdot \vec{s}$	$v$ = final velocity $u$ = initial velocity $a$ = acceleration (constant) $t$ = time $s$ = displacement <b>Valid only when acceleration is constant</b>
13	Displacement in $n^{\text{th}}$ second ( $S_n$ )	$S_n = u + \frac{1}{2}a(2n - 1)$	$u$ = initial velocity $a$ = constant acceleration $n$ = time interval in sec

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14	Galileo's law of odd numbers	When particle starts from rest and moves with constant acceleration, ratio of distance travelled in successive equal intervals of time is: $1 : 3 : 5 : 7 : \dots : (2n - 1)$	$n$ = time interval in sec
15	Stopping distance ( $s$ ) & Stopping time ( $t$ )	$s = \frac{u_0^2}{2a_0}$ [since $a_0$ is constant] $t = \frac{u_0}{a_0}$ [since $a_0$ is constant] $s \propto u_0^2$ $t \propto u_0$	$u_0$ = initial speed $a_0$ = constant retardation
16	Position-time graph ( $x - t$ )	Slope of graph represents instantaneous velocity $\text{slope} = \tan \theta = \frac{\text{displacement}}{\text{time}} = \text{velocity}$	$\tan \theta$ = slope of the graph
17	Velocity-time graph ( $v - t$ )	Slope represents acceleration: $\tan \theta = \frac{\text{velocity}}{\text{time}} = \text{acceleration}$ Area of $v - t$ graph: $\int v dt = \text{displacement}$	$\tan \theta$ = slope $v$ = velocity $dt$ = time interval
18	Acceleration-time graph ( $a - t$ )	Area of $a - t$ graph: $\int a dt = dv = v_2 - v_1 = \text{change in velocity}$	$a$ = acceleration $v_2$ = final velocity $v_1$ = initial velocity
19	Motion under gravity	If object falling freely ( $u = 0$ ): (i) $v = u + gt$ (ii) $h = ut + \frac{1}{2}gt^2$ (iii) $v^2 = u^2 + 2gh$ If thrown upward, replace $g$ with $-g$	$h$ = displacement (height) $u$ = initial velocity $t$ = time $g$ = acceleration due to gravity $v$ = final velocity
20	Body thrown vertically up with velocity $u$	(i) Maximum height: $h = \frac{u^2}{2g}$ (ii) Time of ascent = Time of descent = $\frac{u}{g}$ (iii) Total time of flight = $\frac{2u}{g}$	$h$ = maximum height $u$ = initial velocity $g$ = gravitational acceleration
21	Effect of air resistance (Motion under gravity)	<b>Ascending:</b> Time to go up: $t_1 = \sqrt{\frac{2h}{g+a}}$ Velocity of projection: $v_1 = \sqrt{2h(g+a)}$ <b>Descending:</b> Time to go down: $t_2 = \sqrt{\frac{2h}{g-a}}$ Velocity on reaching ground: $v_2 = \sqrt{2h(g-a)}$	$h$ = height attained $g$ = gravitational acceleration $a$ = retardation due to air drag $t_1$ = time of ascent $t_2$ = time of descent
22	Body thrown upwards crosses a point at times $t_1$ & $t_2$	Height of point: $h = \frac{1}{2}gt_1t_2$ Maximum height: $H = \frac{1}{8}g(t_1 + t_2)^2$ Time of flight: $T = t_1 + t_2 = \frac{2u}{g}$	$t_1$ = time while ascending $t_2$ = time while descending (same point)
23	Relative velocity	Relative velocity of A w.r.t. B: $\vec{v}_{A/B} = \vec{v}_A - \vec{v}_B$ Relative velocity of B w.r.t. A: $\vec{v}_{B/A} = \vec{v}_B - \vec{v}_A$	$\vec{v}_A$ = velocity of A w.r.t. ground $\vec{v}_B$ = velocity of B w.r.t. ground