```
print test results
    print(T1_test1[T1_test1.nonzero()])
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>>> print(T1_test2[T1_test2.nonzero()])
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>>> print(T1_test3[T1_test3.nonzero()])
[4. 4. 3. 2. 1. 1. 4. 3. 1. 2. 1. 5. 1. 2. 1. 1. 1. 2. 1. 1. 1. 1. 1. 1.
1. 1. 1. 1. 1. 1. 1. 2. 1. 1. 1. 2. 1. 1. 1. 2. 1. 5. 1. 1. 1. 1. 1.
1. 1. 2. 1. 2. 1. 1. 1. 1. 1. 1. 1. 1. 3. 1. 1.]
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```
>>> # print test results
>>> print(T2_test1[T2_test1.nonzero()])
[1.92555059e-03 8.50478606e-04 3.65947527e-03 1.27515309e-03
7.26881462e-03 2.19975741e-03 2.66216132e-03 6.35871363e-03
3.43014584e-03 1.65693809e-03 9.44999233e-03 3.95217425e-03
4.19787791e-03 5.18781198e-03 6.54906258e-03 9.61804463e-06
9.42766276e-03 2.87951994e-03 5.38035007e-04 6.14710796e-03
9.49332595e-03 1.50258572e-02 3.37418661e-03 4.94317579e-03
5.98488082e-03 4.54842076e-03 4.99141867e-03 1.65903978e-02
4.91237317e-03 7.28885166e-03 6.36745621e-03 1.33917572e-02
6.28356577e-03 7.13964429e-03 7.13821425e-03 1.59751652e-02
6.41882998e-03 7.64721754e-03 1.62776158e-02 8.57654687e-03
7.64721754e-03 8.98232287e-03 8.13687431e-03 7.89645803e-03
8.90098531e-03 8.51964347e-03 8.08508990e-03 1.72643992e-02
8.86948389e-03 9.22023607e-03 2.01086375e-02 2.13909906e-02
1.05521284e-02 1.99249503e-02 1.03349188e-02 9.82126974e-03
1.04846708e-02 3.22766724e-02 4.18291549e-02 1.12750179e-02
1.09072460e-02 1.15831427e-02 1.14176787e-02 2.29934203e-02
1.12501771e-02 1.20844660e-02 1.10766217e-02 1.17285929e-02
1.13455801e-02 1.16161455e-02 1.18747446e-02 1.17746633e-02
2.43627756e-02 1.30455569e-02 1.22276075e-02 1.23083739e-02
1.35702072e-02 6.68355875e-02 2.64048707e-02 2.64227453e-02
1.24333419e-02 1.27369322e-02 6.59676107e-02 1.24404248e-02
5.50191332e-02 1.27837904e-02 1.36103441e-02 1.34238833e-02
2.67718630e-02 1.36407694e-02 3.04637923e-02 1.38510787e-02
1.67550858e-01 1.46863490e-02 1.49479000e-02 1.46724068e-02
1.51344992e-02 3.01422477e-02 2.99871466e-02 2.96874341e-02
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8.16808649e-02 1.54008745e-02 3.19745942e-02 1.59666661e-02
1.61138574e-02 1.61138574e-02 1.61354292e-02 3.41042871e-02
1.63132576e-02 3.39910789e-02 3.56393971e-02 7.18675593e-02
1.78924764e-02 1.74457237e-02 1.71389064e-02 1.04179133e-01
1.97732182e-02 1.82007228e-02 2.02620792e-02 1.83663202e-02
4.20396654e-02 7.50891528e-02 1.88696852e-02 1.89194795e-02
1.91265005e-02 5.63168646e-02 1.92350761e-02 1.93473329e-02
1.88206286e-02 1.92350761e-02 5.97170587e-02 3.92916929e-02
3.99479240e-02 2.01148879e-02 2.02620792e-02 1.32024656e-01
2.13165617e-02 1.40466044e-01 2.11158179e-02 2.34110073e-02
6.81339249e-02 2.11158179e-02 2.17587186e-02 4.35174373e-02
2.21339792e-02 2.27113083e-02 2.27113083e-02 2.28728651e-02
2.04083036e-01 4.64434820e-02 2.30427105e-02 2.42992986e-02
2.40539080e-02 2.48524578e-02 2.42992986e-02]
>>> print(T2 test2[T2 test2.nonzero()])
[5.54725111e-03 2.68605086e-03 7.39273306e-03 2.03178717e-03
5.06707738e-03 1.94545485e-03 4.31868710e-03 2.42388609e-03
2.46472840e-03 4.14154280e-03 1.62831955e-03 6.62550483e-03
3.22073049e-03 2.43657927e-03 1.69721414e-03 1.15698386e-03
1.93593964e-03 4.04824180e-03 3.94159141e-03 2.94504525e-03
9.88048494e-04 4.42826235e-03 1.49072312e-03 5.28678488e-04
1.04214371e-02 1.86094552e-03 1.49772974e-03 1.04087154e-03
1.64197257e-06 2.22622265e-03 4.73573904e-05 1.23392775e-02
1.00104738e-03 9.83171309e-04 9.65207547e-04 3.03599781e-03
3.98260227e-03 2.13198368e-03 3.57653570e-03 1.57413222e-03
2.17955958e-03 1.07444211e-03 5.40226952e-04 5.59517954e-04
3.84777461e-03 1.44634481e-03 2.21205679e-03 6.24049705e-03
5.63104209e-04 4.86079553e-03 4.90455048e-03 7.84729739e-03
1.77626038e-03 2.30413648e-03 7.10498595e-03 1.96850758e-03
2.16703483e-03 1.31035475e-03 1.36934217e-03 1.94164808e-03
5.81927334e-03 2.86998439e-03 1.36267792e-03 1.45303972e-03
3.47796655e-03 6.75110950e-03 2.96447004e-03 5.13676332e-03
1.55299386e-03 1.39374925e-03 7.44483602e-04 1.48960041e-03
8.19877288e-04 1.73294509e-03 1.59879298e-03 8.04183656e-04
5.12938309e-03 2.50805724e-03 2.55637383e-03 2.43592804e-03
8.68439688e-04 8.90132820e-04 1.51500388e-03 1.87415561e-03
1.47175815e-03 3.73352652e-03 2.91159940e-03 8.95481969e-04
2.74919301e-03 2.73594560e-03 3.94921536e-03 6.43284322e-03
9.41246420e-04 2.15148451e-03 9.90881645e-04 2.99283121e-03
2.01554418e-03 9.63339843e-04 4.03647370e-03 6.18664562e-03
3.09437419e-03 1.14412419e-02 1.04727765e-03 6.46812994e-03
2.94738368e-03 8.38630128e-04 3.02887238e-03 1.24561624e-03
2.07560755e-03 1.04475964e-03 1.06858419e-03 9.54857618e-04
3.66614576e-03 3.47542870e-03 2.19044071e-03 5.46533058e-03
2.17407776e-03 2.28621293e-03 2.17989452e-03 2.14543455e-03
1.21594255e-03 1.35797367e-03 1.14847082e-03 1.20463876e-03
1.23571864e-03 3.65586326e-03 1.48294476e-03 1.19122644e-03
1.72118288e-03 1.19472526e-03 4.10036054e-03 3.68466389e-03
5.05531136e-03 1.23345898e-03 1.23120831e-03 6.42692941e-03
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1.26171657e-03 1.22971283e-03 2.77888071e-03 8.50936495e-03
2.67244625e-03 2.57242105e-03 1.30665677e-03 1.32609646e-03
1.36646971e-03 1.33113712e-03 1.39175645e-03 1.34196217e-03
4.06737502e-03 6.66015665e-03 1.33203133e-03 1.35516979e-03
1.47751669e-03 1.40044312e-03 2.74441105e-03 1.77340069e-03
1.40789911e-03 1.49754646e-03 9.17519717e-03 1.79193649e-03
1.55162439e-03 2.80764004e-03 1.41476369e-03 4.55867309e-03
2.84412471e-03 1.46947107e-03 1.52289276e-03 4.36336743e-03
2.94734231e-03 3.08925841e-03 4.56617143e-03 1.48000188e-02
1.48294476e-03 1.51417984e-03 1.65512923e-03 1.48607009e-03
3.03248439e-03 4.51193830e-03 1.53771952e-03 3.30814720e-03
9.82160631e-03 1.65301994e-03 1.64310687e-03 3.16100856e-03
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4.03094902e-03 1.67742926e-02 1.32683369e-02 8.71239453e-03
4.29663790e-03 8.38714629e-03 4.10643313e-03 8.59327580e-03
4.14832571e-03]
>> print(T2 test3[T2 test3.nonzero()])
[2.34482371e-03 4.14265386e-03 4.42577019e-03 2.92148526e-03
1.33936842e-03 2.16121698e-03 1.08191180e-02 8.05687963e-03
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2.16014850e-02 2.17616535e-02 2.77570110e-02 2.30871061e-02
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2.58076567e-02 2.72681028e-02 3.02984539e-02 2.82909350e-02
6.64934520e-02 3.03504273e-02 3.12699320e-02 3.30500207e-02
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3.48071684e-02 3.87869947e-02 3.79869411e-02 4.06113152e-02
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8.94617535e-02 4.18132151e-02 4.35768377e-02 4.37580704e-02
4.41332318e-02 4.24887787e-02 4.76963992e-02 4.50471728e-02
5.07453196e-02 4.99174635e-02 1.62708477e-01 5.61201497e-02
5.70171306e-02]
```

```
>>> print(T3_test1)
comp.graphics
>>> print(T3_test2)
talk.religion.misc
>>> print(T3_test3)
alt.atheism
>>> print(T3_test4)
alt.atheism
>>> print(T3_test5)
sci.space
>>> print(T3_test6)
talk.politics.misc
>>> print(T3_test7)
talk.politics.guns
>>> print(T3_test8)
talk.politics.mideast
```

```
In [6]: import re import numpy as np
```

```
In [1]: # Data Loading
        corpus = sc.textFile ("s3://chrisjermainebucket/comp330 A6/20 news same line.tx
        t")
        # each entry in validLines will be a line from the text file
        validLines = corpus.filter(lambda x: 'id' in x)
        # now we transform it into a bunch of (docID, text) pairs
        keyAndText = validLines.map(lambda x :(x[x.index('id="') + 4 : x.index('" url='
        )], x[x.index('">') + 2:]))
        # now we split the text in each (docID, text) pair into a list of words
        # after this, we have a data set with (docID, ["word1", "word2", "word3", ...])
        # we have a bit of fancy regular expression stuff here to make sure that we do n
        # die on some of the documents
        regex = re.compile('[^a-zA-Z]')
        keyAndListOfWords = keyAndText.map(lambda x : (str(x[0]), regex.sub(' ', x[1]).1
        ower().split()))
        # now get the top 20,000 words... first change (docID, ["word1", "word2", "word
        # to ("word1", 1) ("word2", 1)...
        allWords = keyAndListOfWords.flatMap(lambda x:((j, 1) for j in x[1]))
        # now, count all of the words, giving us ("word1", 1433), ("word2", 3423423), et
        allCounts = allWords.reduceByKey(lambda a, b: a + b)
        # and get the top 20,000 words in a local array
        # each entry is a ("word1", count) pair
        topWords = allCounts.top(20000, lambda x : x[1])
In [ ]: # define a python dictionary to refer each word's position
        Dict wPos = {}
        for i in range(len(topWords)):
            Dict wPos[topWords[i][0]] = i
        def list2Arr(lis, wordPos):
            wcnt = np.zeros(len(wordPos))
            for word in lis:
                try:
                    wcnt[wordPos[word]] += 1
                except:
                    continue
            return wont
        T1res = keyAndListOfWords.map(lambda x:(x[0], list2Arr(x[1], Dict_wPos)))
In [ ]: T1_test1 = T1res.lookup("20_newsgroups/comp.graphics/37261")[0]
        T1 test2 = T1res.lookup("20 newsgroups/talk.politics.mideast/75944")[0]
        T1 test3 = T1res.lookup("20 newsgroups/sci.med/58763")[0]
        # print test results
        print(T1_test1[T1_test1.nonzero()])
        print(T1_test2[T1_test2.nonzero()])
        print(T1_test3[T1_test3.nonzero()])
```

```
In [ ]: # TF
        tf = Tlres.map(lambda x: (x[0], x[1] / x[1].sum()))
        # IDF
        nDoc = corpus.count()
        p = T1res.map(lambda x: (x[0], np.clip(x[1], 0, 1)))
        q = p.map(lambda x: ("nDoc", x[1]))
        nWinDoc = q.reduceByKey(lambda a, b: a + b)
        idf = np.log(nDoc / nWinDoc.lookup("nDoc")[0])
        # TF-IDF for each doc
        T2res = tf.map(lambda x: (x[0], x[1] * idf))
In [ ]: T2_test1 = T2res.lookup("20_newsgroups/comp.graphics/37261")[0]
        T2_test2 = T2res.lookup("20_newsgroups/talk.politics.mideast/75944")[0]
        T2 test3 = T2res.lookup("20 newsgroups/sci.med/58763")[0]
        # print test results
        print(T2_test1[T2_test1.nonzero()])
        print(T2_test2[T2_test2.nonzero()])
        print(T2_test3[T2_test3.nonzero()])
```

```
In [3]: def MaxValK(dic):
            v = list(dic.values())
            k = list(dic.keys())
            return k[v.index(max(v))]
        def predictLabel(k, str):
            listofwords = regex.sub(' ', str).lower().split()
            wordvec = list2Arr(listofwords, Dict wPos)
            tfIDF = (wordvec / wordvec.sum()) * idf
            12Norm = T2res.map(lambda x:(x[0], np.linalg.norm(x[1] - tfIDF)))
            kNearest = 12Norm.top(k, lambda x: -x[1])
            kNearest = list(map(lambda x: (x[0][14:], x[1]), kNearest))
            kNearest = list(map(lambda x: (x[0][:x[0].index("/")], x[1]), kNearest))
            kNearest = list(map(lambda x: x[0], kNearest))
            # most frequent document class
            mf = \{\}
            for doc in kNearest:
                try:
                    mf[doc] += 1
                except:
                    mf[doc] = 1
            return MaxValK(mf)
```

In [ ]: T3 test1 = predictLabel (10, 'Graphics are pictures and movies created using com puters - usually referring to image data created by a computer specifically with help from specialized graphical hardware and software. It is a vast and recent a rea in computer science. The phrase was coined by computer graphics researchers Verne Hudson and William Fetter of Boeing in 1960. It is often abbreviated as C G, though sometimes erroneously referred to as CGI. Important topics in computer graphics include user interface design, sprite graphics, vector graphics, 3D mod eling, shaders, GPU design, implicit surface visualization with ray tracing, and computer vision, among others. The overall methodology depends heavily on the un derlying sciences of geometry, optics, and physics. Computer graphics is respons ible for displaying art and image data effectively and meaningfully to the user, and processing image data received from the physical world. The interaction and understanding of computers and interpretation of data has been made easier beca use of computer graphics. Computer graphic development has had a significant imp act on many types of media and has revolutionized animation, movies, advertisin g, video games, and graphic design generally.') T3 test2 = predictLabel (10, 'A deity is a concept conceived in diverse ways in various cultures, typically as a natural or supernatural being considered divin e or sacred. Monotheistic religions accept only one Deity (predominantly referre d to as God), polytheistic religions accept and worship multiple deities, henoth eistic religions accept one supreme deity without denying other deities consider ing them as equivalent aspects of the same divine principle, while several non-t heistic religions deny any supreme eternal creator deity but accept a pantheon o f deities which live, die and are reborn just like any other being. A male deity is a god, while a female deity is a goddess. The Oxford reference defines deity as a god or goddess (in a polytheistic religion), or anything revered as divin e. C. Scott Littleton defines a deity as a being with powers greater than those of ordinary humans, but who interacts with humans, positively or negatively, in ways that carry humans to new levels of consciousness beyond the grounded preocc upations of ordinary life.') T3 test3 = predictLabel (10, 'Egypt, officially the Arab Republic of Egypt, is a transcontinental country spanning the northeast corner of Africa and southwest c orner of Asia by a land bridge formed by the Sinai Peninsula. Egypt is a Mediter ranean country bordered by the Gaza Strip and Israel to the northeast, the Gulf of Agaba to the east, the Red Sea to the east and south, Sudan to the south, an d Libya to the west. Across the Gulf of Agaba lies Jordan, and across from the S inai Peninsula lies Saudi Arabia, although Jordan and Saudi Arabia do not share a land border with Egypt. It is the worlds only contiquous Eurafrasian nation. Egypt has among the longest histories of any modern country, emerging as one of the worlds first nation states in the tenth millennium BC. Considered a cradle o f civilisation, Ancient Egypt experienced some of the earliest developments of w riting, agriculture, urbanisation, organised religion and central government. Ic onic monuments such as the Giza Necropolis and its Great Sphinx, as well the rui ns of Memphis, Thebes, Karnak, and the Valley of the Kings, reflect this legacy and remain a significant focus of archaeological study and popular interest wor ldwide. Egypts rich cultural heritage is an integral part of its national identi ty, which has endured, and at times assimilated, various foreign influences, inc luding Greek, Persian, Roman, Arab, Ottoman, and European. One of the earliest c enters of Christianity, Egypt was Islamised in the seventh century and remains a predominantly Muslim country, albeit with a significant Christian minority.') T3\_test4 = predictLabel (10, 'The term atheism originated from the Greek atheos, meaning without god(s), used as a pejorative term applied to those thought to re ject the gods worshiped by the larger society. With the spread of freethought, s keptical inquiry, and subsequent increase in criticism of religion, application of the term narrowed in scope. The first individuals to identify themselves usi ng the word atheist lived in the 18th century during the Age of Enlightenment. T he French Revolution, noted for its unprecedented atheism, witnessed the first m ajor political movement in history to advocate for the supremacy of human reaso n. Arguments for atheism range from the philosophical to social and historical a pproaches. Rationales for not believing in deities include arguments that there is a lack of empirical evidence; the problem of evil; the argument from inconsi stent revelations; the rejection of concepts that cannot be falsified; and the a rgument from nonbelief. Although some atheists have adopted secular philosophies (eg. humanism and skepticism), there is no one ideology or set of behaviors to w hich all atheists adhere.') T3\_test5 = predictLabel (10, 'President Dwight D. Eisenhower established NASA in 1958 with a distinctly civilian (rather than military) orientation encouraging p eaceful applications in space science. The National Aeronautics and Space Act wa

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s passed on July 29, 1958, disestablishing NASAs predecessor, the National Advis
ory Committee for Aeronautics (NACA). The new agency became operational on Octob
er 1, 1958. Since that time, most US space exploration efforts have been led by
NASA, including the Apollo moon-landing missions, the Skylab space station, and
later the Space Shuttle. Currently, NASA is supporting the International Space S
tation and is overseeing the development of the Orion Multi-Purpose Crew Vehicl
e, the Space Launch System and Commercial Crew vehicles. The agency is also resp
onsible for the Launch Services Program (LSP) which provides oversight of launch
operations and countdown management for unmanned NASA launches.')
T3_test6 = predictLabel (10, 'The transistor is the fundamental building block o
f modern electronic devices, and is ubiquitous in modern electronic systems. Fir
st conceived by Julius Lilienfeld in 1926 and practically implemented in 1947 by
American physicists John Bardeen, Walter Brattain, and William Shockley, the tra
nsistor revolutionized the field of electronics, and paved the way for smaller a
nd cheaper radios, calculators, and computers, among other things. The transisto
r is on the list of IEEE milestones in electronics, and Bardeen, Brattain, and S
hockley shared the 1956 Nobel Prize in Physics for their achievement.')
T3 test7 = predictLabel (10, 'The Colt Single Action Army which is also known as
the Single Action Army, SAA, Model P, Peacemaker, M1873, and Colt .45 is a singl
e-action revolver with a revolving cylinder holding six metallic cartridges. It
was designed for the U.S. government service revolver trials of 1872 by Colts P
atent Firearms Manufacturing Company - todays Colts Manufacturing Company - and
was adopted as the standard military service revolver until 1892. The Colt SAA
has been offered in over 30 different calibers and various barrel lengths. Its
overall appearance has remained consistent since 1873. Colt has discontinued it
s production twice, but brought it back due to popular demand. The revolver was
popular with ranchers, lawmen, and outlaws alike, but as of the early 21st cent
ury, models are mostly bought by collectors and re-enactors. Its design has infl
uenced the production of numerous other models from other companies.')
T3 test8 = predictLabel (10, 'Howe was recruited by the Red Wings and made his N
HL debut in 1946. He led the league in scoring each year from 1950 to 1954, then
again in 1957 and 1963. He ranked among the top ten in league scoring for 21 con
secutive years and set a league record for points in a season (95) in 1953. He w
on the Stanley Cup with the Red Wings four times, won six Hart Trophies as the 1
eagues most valuable player, and won six Art Ross Trophies as the leading score
r. Howe retired in 1971 and was inducted into the Hockey Hall of Fame the next y
ear. However, he came back two years later to join his sons Mark and Marty on th
e Houston Aeros of the WHA. Although in his mid-40s, he scored over 100 points t
wice in six years. He made a brief return to the NHL in 1979-80, playing one sea
son with the Hartford Whalers, then retired at the age of 52. His involvement wi
th the WHA was central to their brief pre-NHL merger success and forced the NHL
to expand their recruitment to European talent and to expand to new markets.')
# print test results
print(T3_test1)
print(T3_test2)
print(T3_test3)
print(T3_test4)
print(T3 test5)
print(T3 test6)
print(T3 test7)
print(T3 test8)
```