- 1) Tangent and normal lines /
- 2) Implicit differentiation
- 3) Higher Derivatives

Tangent has gradient = denivotive

$$f(x) = x \sin x$$

$$f'(x) = 1 \sin x + x \cos x$$

T/2

What is the targent line at the origin

$$f'(0) = 1.\sin 0 + 0\cos 0 = 0$$

$$f(x) = x^2 + 2x$$

What is the tangent line at x = -3

$$f'(x) = 2x + 2$$
 $f'(-3) = -6+2 = \frac{4}{-4}$

$$x = -3$$
, $y = f(-3) = |2 + c|$
 $9 - 6 = |2 + c| = > c = -9$
 $y = -4x - 9$

General formula

Tangent line to the curve y = f(x)at some point x = c is $y = f'(c) \times + (f(c) - f'(c)c)$ gradient m Goes through (c, f(c)) Normal line gradient perpendicular -1/m $f(\alpha) = \chi^2 + 2\chi$ Normal line has gradient - $y = \frac{1}{4}x + 3 + \frac{3}{4}$ x = -3, y = 3 15/4

Chain Rule Implicit definition of y

$$y = f(x)$$
 with $y^5x + x^3 + \sin(x) = 0$
 $y' = f'(x)$ $\frac{dy}{dx}$ $\frac{dy}{dx}$ $\frac{dx}{dx}$ $\frac{dx}{dx}$

Higher Derivatives
$$f'(x)$$

 $f(x)=y=x^3+7x^2$ $\frac{dy}{dx}=3x^2+14x$
 $\frac{d}{dx}\left(\frac{d}{dx}y\right)=\frac{d^2y}{dx^2}=f''(x)=6x+14$
 $\frac{d^3y}{dx^3}=f'''(x)=6$
 $\frac{d^4y}{dx^4}=\left(\frac{\pi}{\pi}\right)\left(\frac{\pi}{x}\right)=6$

$$f'(x) = \sin x \qquad f'(x) = \cos x$$

$$f''(x) = -\sin x \qquad f'''(x) = -\cos x$$

$$f''''(x) = \sin x \qquad = f(x) \qquad = f^{(100)}(x)$$
In larger than degree of polynomial
$$f^{(n)}(x) = 0$$

$$f(x) = x^5 \qquad 5x^9, \qquad 20x^3, \qquad 60x^2, \qquad 120x, \qquad 120, \qquad 0$$

$$u(x) v(x) \qquad (u.v) = uv' + u'v' + u'v' + uv'' + uv''$$