第四章 机械振动 作业 参考答案

一、选择题

二、填空题

4.2.1. 答:
$$T = 2\pi \sqrt{\frac{m_1 \Delta x_0}{m_2 g}}$$

4.2.2. 答:
$$A = 0.05 \text{ m}$$
, $\varphi = \arccos(4/5) = -36.87^0 = -36^0 52' 12''$ (第 4 象限)

4.2.3.
$$\stackrel{\triangle}{\cong} : \frac{E_k}{E} = \frac{3}{4}, \quad T = 2\pi \sqrt{\frac{\Delta l}{g}}$$

4.2.4. 答:
$$A = 0.02 \text{ m}$$

4. 2. 5.
$$\approx x = 0.05\sqrt{2}\cos\left(\frac{\pi}{2}t - \frac{3\pi}{4}\right), \quad \phi = \frac{3\pi}{4}$$

4.2.6. 答: 直线 (
$$\frac{x}{A} + \frac{y}{B} = 0$$
)

4.2.7. 答: 椭圆
$$(\frac{x^2}{A^2} + \frac{y^2}{B^2} = 1)$$

4. 2. 8.
$$\stackrel{\triangle}{\text{e}}: \frac{T_x}{T_y} = \frac{2}{3}, \quad \frac{\omega_x}{\omega_y} = \frac{3}{2}$$

4.2.9. 答:
$$\omega = \sqrt{{\omega_0}^2 - 2\beta^2}$$
 , $\omega = \omega_0$

三、计算题

4.3.1.
$$T = \frac{2\pi}{\omega} \approx 0.36 \,\text{s}$$
, $A = 4.176 \,\text{cm}$, $\varphi = 16.694^{\circ}$

$$x = 0.04176\cos(17.5t + 16.694^{\circ})$$

4.3.2.
$$x = 5 \times 10^{-2} \cos(2t + 53.13^{\circ})$$
 (m)

4. 3. 3.
$$x = 0.04 \cos\left(\frac{\pi}{2}t - \frac{\pi}{4}\right) \text{m}$$
,

$$v = -0.0628 \sin\left(\frac{\pi}{2}t - \frac{\pi}{4}\right) \text{m} \cdot \text{s}^{-1}, \quad a = -0.0986 \cos\left(\frac{\pi}{2}t - \frac{\pi}{4}\right) \text{m} \cdot \text{s}^{-2}$$

4.3.4. (1)
$$x = 0.04 \cos \left(2\pi t - \frac{\pi}{2} \right) \text{m}$$
; (2) $x = 0.04 \cos \left(2\pi t + \pi \right) \text{m}$

(3)
$$x = 0.04 \cos \left(2\pi t + \frac{3\pi}{4} \right) \text{m};$$
 (4) $x = 0.04 \cos \left(2\pi t - \frac{\pi}{3} \right) \text{m}$

4.3.5. (1)
$$x = 0.04 \cos \left(\pi t + \frac{\pi}{4} \right) \text{m}$$
; (2) $t_2 = \frac{13}{12} \text{ s}$

4.3.6. (1)
$$T = \frac{\pi}{10}$$
 s; (2) $x = 0.01\cos\left(20t - \frac{\pi}{2}\right)$ m; (3) $x_1 = \pm \frac{1}{2}A$

4.3.7. (1)
$$x_0 = 0$$
, $v_0 = 0.2 \text{ m} \cdot \text{s}^{-1}$

(2)
$$x_1 = 4 \times 10^{-2} \cos(\pi/6) \,\text{m}$$
, $v_1 = -2 \times 10^{-1} \sin(\pi/6) \,\text{m} \cdot \text{s}^{-1}$, $a_1 = -\cos(\pi/6) \,\text{m} \cdot \text{s}^{-2}$

(3)
$$v_2 = -2 \times 10^{-1} \sin(-\pi/3) \,\mathrm{m \cdot s^{-1}}$$
, $a_2 = -\cos(-\pi/3) \,\mathrm{m \cdot s^{-2}}$
 $F_2 = -0.04 \cos(-\pi/3) \,\mathrm{N}$

4.3.8. (1)
$$E_k 0.002 \,\text{J}$$
, $E = 0.002 \,\text{J}$; (2) $x_1 = \pm \frac{\sqrt{2}}{2} \times 0.01 \approx \pm 0.071 \,\text{m}$

4.3.9. (1)
$$A_{12} = 0.5 \text{ m}$$
, $\varphi_{12} = 81.87^{\circ}$; (2) $\varphi_{3} = \varphi_{1} = \frac{3}{4}\pi$; (3) $\varphi_{3} = -\frac{3}{4}\pi$