## Problem 2

```
dp[i] \doteq \text{The minimum penalty of the words from } 1..i \text{ with words}[i] \text{ being the last word.}
The words array represents our input of words.
dp[0] = 0
Recurrence:
j \leftarrow 0
minPenalty \leftarrow \infty
\mathrm{len} \leftarrow 0
while len < 32 and i - j > 0:
  len += words[i - j].length
  j = j + 1
  penalty = calculatePenalty(len)
  \min Penalty \leftarrow \min(dp[i - j] + penalty, \min Penalty)
  len += 1
Algorithm:
for i = 1 to n:
  j \leftarrow 0
  minPenalty \leftarrow \infty
  len \leftarrow 0
  while len < 32 and i - j > 0:
    len += words[i - j].length
    j = j + 1
    penalty \leftarrow (16 - len)^2
    if i = n:
      if len > 16 break out
      \min Penalty \leftarrow \min(dp[i - j], \min Penalty)
      \min Penalty \leftarrow \min(dp[i - j] + penalty, \min Penalty)
    len += 1
  dp[i] = minPenalty
return dp[n]
```

Runtime: We do n \* O(1) work meaning O(n) work overall.

We check when i = n to see if we are on the last line in order to both ignore the penalty and also throw out any invalid solutions that use more than 16 characters on the last line.

By the time we get to dp[i], we have filled dp[1..i-1], through our bottom up loop.

Gabe McKay Terisa Le Reeve Masilamani

## Homework 2

ECS 122A October 23, 2025

In each recurrence call, we consider filling a line with a number of words. We look at many cases where a line could be filled with one word up to 32 characters + extra characters from the last word. This covers all potential cases since any line with more than 32 characters, a potential word would incur a bigger penalty at the end of such a line rather than just being put on the next line.

Overall, this means that the algorithm looks at every possible case and returns dp[n] as the final answer minimizing the penalty.