Functions

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0.1 Functions are first class objects

In Python, functions behave like any other object, such as an int or a list. That means that you can use functions as arguments to other functions, store functions as dictionary values, or return a function from another function. This leads to many powerful ways to use functions.

```
In [2]: def square(x):
            """Square of x."""
            return x*x
        def cube(x):
            """Cube of x."""
            return x*x*x
In [3]: # create a dictionary of functions
        funcs = {
            'square': square,
            'cube': cube,
        }
In [4]: x = 2
        print square(x)
        print cube(x)
        for func in sorted(funcs):
            print func, funcs[func](x)
4
8
cube 8
square 4
```

0.2 Function argumnents

This is caution to be careful of how Python treats function arguments.

0.2.1 Call by "object reference"

Some data types, such as strings and tuples, cannot be directly modified and are called immutable. Atomic variables such as integers or floats are always immutable. Other datatypes, such as lists and dictionaries, can be directly modified and are called mutable. Passing mutable variables as function arguments can have different outcomes, depending on what is done to the variable inside the function. When we call

```
x = [1,2,3] # mutable f(x)
```

what is passed to the function is a *copy* of the *name* x that refers to the content (a list) [1, 2, 3]. If we use this copy of the name to change the content directly (e.g. x[0] = 999) within the function, then x chanes *outside* the function as well. However, if we reassgne x within the function to a new object (e.g. another list), then the copy of the name x now points to the new object, but x outside the function is unhanged.

```
In [10]: def transmogrify(x):
             x[0] = 999
             return x
         x = [1,2,3]
         print x
         print transmogrify(x)
         print x
[1, 2, 3]
[999, 2, 3]
[999, 2, 3]
In [11]: def no_mogrify(x):
             x = [4,5,6]
             return x
         x = [1,2,3]
         print x
         print no_mogrify(x)
         print x
[1, 2, 3]
[4, 5, 6]
[1, 2, 3]
```

0.2.2 Binding of default arguments occurs at function definition

```
[1]
[1, 1]
[1, 1, 1]
[9, 9, 9, 1]
[1, 1, 1, 1]
[1, 1, 1, 1, 1]
In [14]: # Usually, this behavior is not desired and we would write
         def f(x = None):
             if x is None:
                 x = []
             x.append(1)
             return x
         print f()
         print f()
         print f()
         print f(x = [9,9,9])
         print f()
         print f()
[1]
[1]
[1]
[9, 9, 9, 1]
[1]
[1]
```

However, sometimes in advanced usage, the behavior is intetnional. See http://effbot.org/zone/default-values.htm for details.

0.3 Higher-order functions

A function that uses another function as an input argument or returns a function (HOF) is known as a higher-order function. The most familiar examples are map and filter.

```
Out[7]: [0, 4, 16]
In [8]: # The reduce function reduces a collection using a binary operator to combine items two at a ti
        def my_add(x, y):
            return x + y
        # another implementation of the sum function
       reduce(my_add, [1,2,3,4,5])
Out[8]: 15
In [10]: # Custom functions can of couse, also be HOFs
         def custom_sum(xs, transform):
             """Returns the sum of xs after a user specified transform."""
             return sum(map(transform, xs))
         xs = range(5)
         print custom_sum(xs, square)
         print custom_sum(xs, cube)
30
100
In [11]: # Returning a function is also useful
         # A closure
         def make_logger(target):
             def logger(data):
                 with open(target, 'a') as f:
                     f.write(data + '\n')
             return logger
         foo_logger = make_logger('foo.txt')
         foo_logger('Hello')
         foo_logger('World')
In [12]: !cat 'foo.txt'
Hello
World
Hello
World
Hello
World
```

0.4 Anonymous functions

When using functional style, there is often the need to create small specific functions that perform a limited task as input to a HOF such as map or filter. In such cases, these functions are often written as anonymous or lambda functions. If you find it hard to understand what a lambda function is doing, it should probably be rewritten as a regular function.

```
In [37]: # Using standard functions
```

```
def square(x):
             return x*x
         print map(square, range(5))
[0, 1, 4, 9, 16]
In [38]: # Using an anonymous function
         print map(lambda x: x*x, range(5))
[0, 1, 4, 9, 16]
In [4]: # what does this function do?
        s1 = reduce(lambda x, y: x+y, map(lambda x: x**2, range(1,10)))
       print(s1)
       print
        # functional expressions and lambdas are cool
        # but can be difficult to read when over-used
        # Here is a more comprehensible version
        s2 = sum(x**2 for x in range(1, 10))
        print(s2)
        # we will revisit map-reduce when we look at high-performance computing
        # where map is used to distribute jobs to multiple processors
        # and reduce is used to calculate some aggreate function of the results
        # returned by map
285
285
```

0.5 Pure functions

Functions are pure if they do not have any *side effects* and do not depend on global variables. Pure functions are similar to mathematical functions - each time the same input is given, the same output will be returned. This is useful for reducing bugs and in parallel programming since each function call is independent of any other function call and hence trivially parallelizable.

```
In [16]: xs = range(5)
         print "xs =", xs
         print impure(xs)
         print "xs =", xs
xs = [0, 1, 2, 3, 4]
[0, 2, 4, 6, 8]
xs = [0, 2, 4, 6, 8]
In [17]: # Note that mutable functions are created upon function declaration, not use.
         # This gives rise to a common source of beginner errors.
         def f1(x, y=[]):
             """Never give an empty list or other mutable structure as a default."""
             y.append(x)
             return sum(y)
In [18]: print f1(10)
         print f1(10)
         print f1(10, y = [1,2])
10
20
13
In [19]: # Here is the correct Python idiom
         def f2(x, y=None):
             """Check if y is None - if so make it a list."""
             if v is None:
                 y = []
             y.append(x)
             return sum(y)
In [20]: print f1(10)
         print f1(10)
         print f1(10, y = [1,2])
30
40
13
```

0.6 Recursion

A recursive function is one that calls itself. Recursive functions are extremely useful examples of the divideand-conquer paradigm in algorithm development and are a direct expression of finite diffference equations. However, they can be computationally inefficient and their use in Python is quite rare in practice.

Recursive functions generally have a set of *base cases* where the answer is obvious and can be returned immediately, and a set of recursive cases which are split into smaller pieces, each of which is given to the same function called recursively. A few examples will make this clearer.

```
if n==0:
                 return 1
             # recursive case
             else:
                 return n * fact(n-1)
         print [fact(n) for n in range(10)]
[1, 1, 2, 6, 24, 120, 720, 5040, 40320, 362880]
In [18]: # The Fibonacci sequence is another classic recursion example
         def fib1(n):
             """Fib with recursion."""
             # base case
             if n==0 or n==1:
                 return 1
             # recurssive caae
             else:
                 return fib1(n-1) + fib1(n-2)
         print [fib1(i) for i in range(10)]
[1, 1, 2, 3, 5, 8, 13, 21, 34, 55]
In [19]: # In Python, a more efficient version that does not use recursion is
         def fib2(n):
             """Fib without recursion."""
             a, b = 0, 1
             for i in range(1, n+1):
                 a, b = b, a+b
             return b
         print [fib2(i) for i in range(10)]
[1, 1, 2, 3, 5, 8, 13, 21, 34, 55]
In [20]: # Note that the recursive version is much slower than the non-recursive version
         %timeit fib1(20)
         %timeit fib2(20)
         # this is because it makes many duplicate function calls
         # Note duplicate calls to fib(2) and fib(1) below
         # fib(4) -> fib(3), fib(2)
         # fib(3) -> fib(2), fib(1)
         # fib(2) -> fib(1), fib(0)
         # fib(1) -> 1
         # fib(0) -> 1
100 loops, best of 3: 5.68 ms per loop
100000 loops, best of 3: 2.82 \mu \mathrm{s} per loop
```

```
In [29]: # Use of cache to speed up the recursive version.
         # Note biding of the (mutable) dictionary as a default at run-time.
         def fib3(n, cache={0: 1, 1: 1}):
             """Fib with recursion and caching."""
             try:
                 return cache[n]
             except KeyError:
                 cache[n] = fib3(n-1) + fib3(n-2)
                 return cache[n]
         print [fib3(i) for i in range(10)]
         %timeit fib1(20)
         %timeit fib2(20)
         %timeit fib3(20)
[1, 1, 2, 3, 5, 8, 13, 21, 34, 55]
100 loops, best of 3: 5.68 ms per loop
100000 loops, best of 3: 2.82 \mus per loop
1000000 loops, best of 3: 256 ns per loop
In [25]: # Recursion is used to show off the divide-and-conquer paradigm
         def almost_quick_sort(xs):
             """Almost a quick sort."""
             # base case
             if xs == []:
                 return xs
             # recursive case
             else:
                 pivot = xs[0]
                 less_than = [x for x in xs[1:] if x <= pivot]</pre>
                 more_than = [x for x in xs[1:] if x > pivot]
                 return almost_quick_sort(less_than) + [pivot] + almost_quick_sort(more_than)
         xs = [3,1,4,1,5,9,2,6,5,3,5,9]
         print almost_quick_sort(xs)
[1, 1, 2, 3, 3, 4, 5, 5, 5, 6, 9, 9]
```

0.7 Iterators

Iterators represent streams of values. Because only one value is consumed at a time, they use very little memory. Use of iterators is very helpful for working with data sets too large to fit into RAM.

```
In [26]: # Iterators can be created from sequences with the built-in function iter()
    xs = [1,2,3]
    x_iter = iter(xs)
    print x_iter.next()
    print x_iter.next()
```

```
print x_iter.next()
         print x_iter.next()
1
2
3
    StopIteration
                                               Traceback (most recent call last)
        <ipython-input-26-eb1a17442aa0> in <module>()
          7 print x_iter.next()
          8 print x_iter.next()
    ----> 9 print x_iter.next()
        StopIteration:
In [27]: # Most commonly, iterators are used (automatically) within a for loop
         # which terminates when it encouters a StopIteration exception
         x_iter = iter(xs)
         for x in x_iter:
             print x
1
2
3
0.8
     Generators
Generators create iterator streams.
In [28]: # Functions containing the 'yield' keyword return iterators
         # After yielding, the function retains its previous state
         def count_down(n):
             for i in range(n, 0, -1):
                 yield i
In [29]: counter = count_down(10)
         print counter.next()
         print counter.next()
         for count in counter:
             print count,
10
8 7 6 5 4 3 2 1
In [30]: # Iterators can also be created with 'generator expressions'
         # which can be coded similar to list generators but with parenthesis
         # in place of square brackets
```

```
xs1 = [x*x for x in range(5)]
         print xs1
         xs2 = (x*x for x in range(5))
         print xs2
         for x in xs2:
             print x,
         print
[0, 1, 4, 9, 16]
<generator object <genexpr> at 0x1130a5820>
0 1 4 9 16
In [31]: # Iterators can be used for infinte functions
         def fib():
             a, b = 0, 1
             while True:
                 yield a
                 a, b = b, a+b
In [32]: for i in fib():
             # We must have a stopping condiiton since the generator returns an infinite stream
             if i > 1000:
                 break
             print i,
0 1 1 2 3 5 8 13 21 34 55 89 144 233 377 610 987
In [38]: # Many built-in Python functions return iterators
         # including file handlers
         # so with the idiom below, you can process a 1 terabyte file line by line
         # on your laptop without any problem
         # Inn Pyhton 3, map and filter return itnrators, not lists
         for line in open('foo.txt'):
             print line,
Hello
World
Hello
World
Hello
World
0.8.1 Generators and comprehensions
In [39]: # A geneeratorr expression
         print (x for x in range(10))
         # A list comprehesnnion
         print [x for x in range(10)]
```

```
# A set comprehension
         print {x for x in range(10)}
         # A dictionary comprehension
         print {x: x for x in range(10)}
<generator object <genexpr> at 0x102d8a410>
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9]
set([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
\{0: 0, 1: 1, 2: 2, 3: 3, 4: 4, 5: 5, 6: 6, 7: 7, 8: 8, 9: 9\}
0.8.2 Utilites - enumerate, zip and the ternary if-else operator
Two useful functions and an unusual operator.
In [34]: # In many programming languages, loops use an index.
         # This is possible in Python, but it is more
         # idiomatic to use the enumerate function.
         # using and index in a loop
         xs = [1,2,3,4]
         for i in range(len(xs)):
             print i, xs[i]
         print
         # using enumerate
         for i, x in enumerate(xs):
             print i, x
0 1
1 2
2 3
3 4
0 1
1 2
2 3
3 4
In [35]: # zip is useful when you need to iterate over matched elements of
         # multiple lists
         xs = [1, 2, 3, 4]
         ys = [10, 20, 30, 40]
         zs = ['a', 'b', 'c', 'd', 'e']
         for x, y, z in zip(xs, ys, zs):
             print x, y, z
         # Note that zip stops when the shortest list is exhausted
1 10 a
2 20 b
3 30 c
```

4 40 d

0.9 Decorators

Decorators are a type of HOF that take a function and return a wrapped function that provides additional useful properties.

Examples:

- logging
- profiling
- Just-In-Time (JIT) compilation

```
In [6]: # Here is a simple decorator to time an arbitrary function
        def func_timer(func):
            """Times how long the function took."""
            def f(*args, **kwargs):
                import time
                start = time.time()
                results = func(*args, **kwargs)
                print "Elapsed: %.2fs" % (time.time() - start)
                return results
            return f
In [7]: # There is a special shorthand notation for decorating functions
        @func_timer
        def sleepy(msg, sleep=1.0):
            """Delays a while before answering."""
            import time
            time.sleep(sleep)
            print msg
        sleepy("Hello", 1.5)
Hello
Elapsed: 1.50s
```

0.10 The operator module

The operator module provides "function" versions of common Python operators (+, *, [] etc) that can be easily used where a function argument is expected.

```
In [46]: import operator as op

# Here is another way to express the sum function
print reduce(op.add, range(10))

# The pattern can be generalized
print reduce(op.mul, range(1, 10))
```

```
45
362880

In [49]: my_list = [('a', 1), ('bb', 4), ('ccc', 2), ('dddd', 3)]

# standard sort
print sorted(my_list)

# return list sorted by element at position 1 (remember Python counts from 0)
print sorted(my_list, key=op.itemgetter(1))

# the key argument is quite flexible
print sorted(my_list, key=lambda x: len(x[0]), reverse=True)

[('a', 1), ('bb', 4), ('ccc', 2), ('dddd', 3)]
[('a', 1), ('ccc', 2), ('dddd', 3), ('bb', 4)]
[('dddd', 3), ('ccc', 2), ('bb', 4), ('a', 1)]
```

0.11 The functools module

The most useful function in the functools module is partial, which allows you to create a new function from an old one with some arguments "filled-in".

```
In [54]: from functools import partial
         sum_ = partial(reduce, op.add)
         prod_ = partial(reduce, op.mul)
         print sum_([1,2,3,4])
         print prod_([1,2,3,4])
10
24
In [58]: # This is extremely useful to create functions
         # that expect a fixed number of arguments
         import scipy.stats as stats
         def compare(x, y, func):
             """Returne p-value for some appropriate comparison test."""
             return func(x, y)[1]
In [83]: x, y = np.random.normal(0, 1, (100,2)).T
         print "p value assuming equal variance
                                                   =%.8f" % compare(x, y, stats.ttest_ind)
         test = partial(stats.ttest_ind, equal_var=False)
         print "p value not assuming equal variance=%.8f" % compare(x, y, test)
p value assuming equal variance
                                   =0.19593077
p value not assuming equal variance=0.19599306
```

0.12 The itertools module

This provides many essential functions for working with iterators. The permuations and combinations generators may be particularly useful for simulations, and the groupby gnerator is useful for data analysis.

```
In [84]: from itertools import cycle, groupby, islice, permutations, combinations
         print list(islice(cycle('abcd'), 0, 10))
         print
         animals = sorted(['pig', 'cow', 'giraffe', 'elephant',
                            'dog', 'cat', 'hippo', 'lion', 'tiger'], key=len)
         for k, g in groupby(animals, key=len):
             print k, list(g)
         print
         print [''.join(p) for p in permutations('abc')]
         print
         print [list(c) for c in combinations([1,2,3,4], r=2)]
['a', 'b', 'c', 'd', 'a', 'b', 'c', 'd', 'a', 'b']
3 ['pig', 'cow', 'dog', 'cat']
4 ['lion']
5 ['hippo', 'tiger']
7 ['giraffe']
8 ['elephant']
['abc', 'acb', 'bac', 'bca', 'cab', 'cba']
[[1, 2], [1, 3], [1, 4], [2, 3], [2, 4], [3, 4]]
```

0.13 The toolz, fn and funcy modules

If you wish to program in the functional style, check out the following packages

- toolz
- fn
- funcy

```
In [85]: # Here is a small example to convert the DNA of a
         # bacterial enzyme into the protein sequence
         # using the partition function to generate
         # cddons (3 nucleotides) for translation.
         codon_table = {
             'ATA':'I', 'ATC':'I', 'ATT':'I', 'ATG':'M',
             'ACA':'T', 'ACC':'T', 'ACG':'T', 'ACT':'T',
             'AAC':'N', 'AAT':'N', 'AAA':'K', 'AAG':'K',
             'AGC':'S', 'AGT':'S', 'AGA':'R', 'AGG':'R',
             'CTA':'L', 'CTC':'L', 'CTG':'L', 'CTT':'L',
             'CCA':'P', 'CCC':'P', 'CCG':'P', 'CCT':'P',
             'CAC':'H', 'CAT':'H', 'CAA':'Q', 'CAG':'Q',
             'CGA':'R', 'CGC':'R', 'CGG':'R', 'CGT':'R',
             'GTA':'V', 'GTC':'V', 'GTG':'V', 'GTT':'V',
             'GCA':'A', 'GCC':'A', 'GCG':'A', 'GCT':'A',
             'GAC':'D', 'GAT':'D', 'GAA':'E', 'GAG':'E',
             'GGA':'G', 'GGC':'G', 'GGG':'G', 'GGT':'G',
             'TCA':'S', 'TCC':'S', 'TCG':'S', 'TCT':'S',
```

```
'TTC':'F', 'TTT':'F', 'TTA':'L', 'TTG':'L',
'TAC':'Y', 'TAT':'Y', 'TAA':'_', 'TAG':'_',
'TGC':'C', 'TGT':'C', 'TGA':'_', 'TGG':'W',
}
```

gene = """

>ENA|BAE76126|BAE76126.1 Escherichia coli str. K-12 substr. W3110 beta-D-galactosidase ATGACCATGATTACGGATTCACTGGCCGTCGTTTTACAACGTCGTGACTGGGAAAACCCT GGCGTTACCCAACTTAATCGCCTTGCAGCACATCCCCCTTTCGCCAGCTGGCGTAATAGC GAAGAGGCCCGCACCGATCGCCCTTCCCAACAGTTGCGCAGCCTGAATGGCGAATGGCGC GAGGCCGATACTGTCGTCCCCTCAAACTGGCAGATGCACGGTTACGATGCGCCCATC TACACCAACGTGACCTATCCCATTACGGTCAATCCGCCGTTTGTTCCCACGGAGAATCCG ACGGGTTGTTACTCGCTCACATTTAATGTTGATGAAAGCTGGCTACAGGAAGGCCAGACG CGAATTATTTTTGATGGCGTTAACTCGGCGTTTCATCTGTGGTGCAACGGGCGCTGGGTC GGTTACGGCCAGGACAGTCGTTTGCCGTCTGAATTTGACCTGAGCGCATTTTTACGCGCC GGAGAAAACCGCCTCGCGGTGATGGTGCTGCGCTGGAGTGACGGCAGTTATCTGGAAGAT CAGGATATGTGGCGGATGAGCGGCATTTTCCGTGACGTCTCGTTGCTGCATAAACCGACT ACACAAATCAGCGATTTCCATGTTGCCACTCGCTTTAATGATGATTTCAGCCGCGCTGTA TTATGGCAGGTGAAACGCAGGTCGCCAGCGCCACCGCCCTTTCGGCGGTGAAATTATC GATGAGCGTGGTGGTTATGCCGATCGCGTCACACTACGTCTGAACGTCGAAAACCCGAAA CTGTGGAGCGCCGAAATCCCGAATCTCTATCGTGCGGTGGTTGAACTGCACACCGCCGAC GGCACGCTGATTGAAGCAGAAGCCTGCGATGTCGGTTTCCGCGAGGTGCGGATTGAAAAT GGTCTGCTGCTGAACGGCAAGCCGTTGCTGATTCGAGGCGTTAACCGTCACGAGCAT CATCCTCTGCATGGTCATGGATGAGCAGACGATGGTGCAGGATATCCTGCTGATG AAGCAGAACAACTTTAACGCCGTGCGCTGTTCGCATTATCCGAACCATCCGCTGTGGTAC ACGCTGTGCGACCGCTACGGCCTGTATGTGGTGGATGAAGCCAATATTGAAACCCACGGC ATGGTGCCAATGAATCGTCTGACCGATGATCCGCGCTGGCTACCGGCGATGAGCGAACGC AATGAATCAGGCCACGGCGCTAATCACGACGCGCTGTATCGCTGGATCAAATCTGTCGAT ${\tt CCTTCCCGCCCGGTGCAGTATGAAGGCGGCGGAGCCGACACCACGGCCACCGATATTATT}$ TGCCCGATGTACGCGCGCGTGGATGAAGACCAGCCCTTCCCGGCTGTGCCGAAATGGTCC ATCAAAAAATGGCTTTCGCTACCTGGAGAGACGCGCCCGCTGATCCTTTGCGAATACGCC CACGCGATGGGTAACAGTCTTGGCGGTTTCGCTAAATACTGGCAGGCGTTTCGTCAGTAT $\tt CCCCGTTTACAGGGCGGCTTCGTCTGGGACTGGGTGGATCAGTCGCTGATTAAATATGAT$ GAAAACGGCAACCCGTGGTCGGCTTACGGCGGTGATTTTGGCGATACGCCGAACGATCGC CAGTTCTGTATGAACGGTCTGGTCTTTGCCGACCGCACGCCGCATCCAGCGCTGACGGAA GCAAAACACCAGCAGCAGTTTTTCCAGTTCCGTTTATCCGGGCAAACCATCGAAGTGACC AGCGAATACCTGTTCCGTCATAGCGATAACGAGCTCCTGCACTGGATGGTGGCGCTGGAT GGTAAGCCGCTGGCAAGCGGTGAAGTGCCTCTGGATGTCGCTCCACAAGGTAAACAGTTG ATTGAACTGCCTGAACTACCGCAGCCGGAGAGCGCCGGGCAACTCTGGCTCACAGTACGC GTAGTGCAACCGAACGCGACCGCATGGTCAGAAGCCGGGCACATCAGCGCCTGGCAGCAG TGGCGTCTGGCGGAAAACCTCAGTGTGACGCTCCCCGCCGCGTCCCACGCCATCCCGCAT CTGACCACCAGCGAAATGGATTTTTGCATCGAGCTGGGTAATAAGCGTTGGCAATTTAAC CGCCAGTCAGGCTTTCTTTCACAGATGTGGATTGGCGATAAAAAACAACTGCTGACGCCG ${\tt CGCATTGACCCTAACGCCTGGGTCGAACGCTGGAAGGCGGCCGGTTACCAGGCCGAA}$ GCAGCGTTGTTGCAGTGCACGGCAGATACACTTGCTGATGCGGTGCTGATTACGACCGCT CACGCGTGGCAGCATCAGGGGAAAACCTTATTTATCAGCCGGAAAACCTACCGGATTGAT GCGCGGATTGGCCTGAACTGCCAGCTGGCGCAGGTAGCAGAGCGGGTAAACTGGCTCGGA TTAGGGCCGCAAGAAACTATCCCGACCGCCTTACTGCCGCCTGTTTTGACCGCTGGGAT $\tt CTGCCATTGTCAGACATGTATACCCCGTACGTCTTCCCGAGCGAAAACGGTCTGCGCTGC$

```
GGGACGCGCGAATTGAATTATGGCCCACACCAGTGGCGCGCGACTTCCAGTTCAACATC
         AGCCGCTACAGTCAACAGCAACTGATGGAAACCAGCCATCGCCATCTGCTGCACGCGGAA
         GAAGGCACATGGCTGAATATCGACGGTTTCCATATGGGGATTGGTGGCGACGACTCCTGG
         AGCCCGTCAGTATCGGCGGAATTCCAGCTGAGCGCCGGTCGCTACCATTACCAGTTGGTC
         TGGTGTCAAAAATAA
         from toolz import partition
         # convert FASTA into single DNA sequence
         dna = ''.join(line for line in gene.strip().split('\n')
                        if not line.startswith('>'))
         # partition DNA into codons (of length 3) and translate to amino acid
         codons = (''.join(c) for c in partition(3, dna))
         ''.join(codon_table[codon] for codon in codons)
Out [85]: 'MTMITDSLAVVLQRRDWENPGVTQLNRLAAHPPFASWRNSEEARTDRPSQQLRSLNGEWRFAWFPAPEAVPESWLECDLPEADTVVVPSNWQM
   The partition function can also be used for doing statistics on sequence windows, for example, in
calculating a moving average.
0.14 Exercises
1. Rewrite the following nested loop as a list comprehension
ans = []
for i in range(3):
    for j in range(4):
        ans.append((i, j))
print ans
In [46]: # YOUR CODE HERE
   2. Rewrite the following as a list comprehension
ans = map(lambda x: x*x, filter(lambda x: x%2 == 0, range(5)))
print ans
In [47]: # YOUR CODE HERE
   3. Convert the function below into a pure function with no global variables or side effects
def f(alist):
    for i in range(x):
        alist.append(i)
    return alist
alist = [1,2,3]
ans = f(alist)
print ans
print alist # alist has been changed!
```

4. Write a decorator hello that makes every wrapped function print "Hello!" For example

x = 5

In [48]: # YOUR CODE HERE

```
@hello
def square(x):
    return x*x
   when called will give the following result
[In]
square(2)
[Out]
Hello!
In [49]: # YOUR CODE HERE
   5. Rewrite the factorial function so that it does not use recursion.
def fact(n):
    """Returns the factorial of n."""
    # base case
    if n==0:
        return 1
    # recursive case
    else:
        return n * fact(n-1)
In [50]: # YOUR CODE HERE
```

Exercise 6. Rewrite the same factoral function so that it uses a cache to speed up calculations

```
In [50]: # YOUR CODE HERE
```

7. Rewrite the following anonymous function as a regular named function.

```
lambda x, y: x**2 + y**2
In [51]: # YOUR CODE HERE
```

8. Find an efficient way to extrac a subset of dict1 into a a new dictionary dict2 that only contains entrires with the keys given in the set good_keys. Note that good_keys may include keys not found in dict1 - these must be excluded when building dict2.

```
In [110]: import numpy as np
    import cPickle

try:
        dict1 = cPickle.load(open('dict1.pic'))
    except:
        numbers = np.arange(1e6).astype('int') # 1 million entries
        dict1 = dict(zip(numbers, numbers))
        cPickle.dump(dict1, open('dict1.pic', 'w'), protocol=2)

good_keys = set(np.random.randint(1, 1e7, 1000))

# YOUR CODE HERE$
In []:
```