

# Compilers: Principles, Techniques, & Tools

---

*By Alfred V. Aho et al*

First Edition

---

# CONTENTS

<b>Contents</b>	<b>0</b>
<b>1 Introduction</b>	<b>1</b>
1 Language Processors . . . . .	2
2 The Structure of a Compiler . . . . .	2
2.1 Lexical Analysis . . . . .	2
2.2 Syntax Analysis . . . . .	2
2.3 Semantic Analysis . . . . .	3
2.4 Intermediate Code Generation . . . . .	3
2.5 The Grouping of Phases into Passes . . . . .	3
2.6 Compiler-Construction Tools . . . . .	3
3 The Evolution of Programming Language . . . . .	3
3.1 The Move to Higher-Level Languages . . . . .	3
4 Applications of Compiler Technology . . . . .	4
4.1 implementation of High-Level Programming Languages . . . . .	4
4.2 Optimizations for Computer Architectures . . . . .	4
5 Programming Language Basics . . . . .	4
5.1 The Static/Dynamic Distinction . . . . .	4
5.2 Environments and States . . . . .	4
5.3 Static Scope and Block Structure . . . . .	5
5.4 Explicit Access Control . . . . .	5
5.5 Dynamic Scope . . . . .	6
5.6 Parameter Passing Mechanisms . . . . .	6
5.7 Aliasing . . . . .	6
<b>2 A Simple Syntax-Directed Translator</b>	<b>7</b>
1 Introduction . . . . .	7
2 Syntax Definition . . . . .	7
2.1 Definition of Grammars . . . . .	8
2.2 Derivations . . . . .	8
2.3 Parse Trees . . . . .	8
2.4 Ambiguity . . . . .	9
2.5 Associativity of Operators . . . . .	9
2.6 Precedence of Operators . . . . .	9
3 Syntax-Directed Translation . . . . .	10
3.1 Postfix Notation . . . . .	10
3.2 Synthesized Attributes . . . . .	10
3.3 Tree Traversals . . . . .	10
3.4 Translation Schemes . . . . .	10
4 Parsing . . . . .	11

4.1	Top-Down Parsing . . . . .	11
4.2	Predictive Parsing . . . . .	11
4.3	Designing a Predictive Parser . . . . .	11
4.4	Left Recursion . . . . .	11
5	A Translator for Simple Expressions . . . . .	12
5.1	Abstract and Concrete Syntax . . . . .	12
5.2	Simplifying the Translator . . . . .	12
5.3	The Complete Program . . . . .	12
6	Lexical Analysis . . . . .	13
6.1	Recognizing Keywords and Identifiers . . . . .	13
7	Symbol Tables . . . . .	14
7.1	Symbol Table Per Scope . . . . .	14
8	Intermediate Code Generation . . . . .	14
8.1	Two Kinds of Intermediate Representations . . . . .	14
8.2	Construction of Syntax Trees . . . . .	14
8.3	Static Checking . . . . .	15
<b>3</b>	<b>Lexical Analysis</b>	<b>16</b>
1	The Role of the Lexical Analyzer . . . . .	16
1.1	Tokens, Patterns, and Lexemes . . . . .	16
2	Specification of Tokens . . . . .	17
2.1	Strings and Languages . . . . .	17
2.2	Operations and Languages . . . . .	17
2.3	Regular Expressions . . . . .	18
2.4	Regular Definitions . . . . .	18
2.5	Extensions of Regular Expressions . . . . .	18
3	Recognition of Tokens . . . . .	18
3.1	Transition Diagrams . . . . .	18
3.2	Recognition of Reserved Words and Identifiers . . . . .	18
4	The Lexical-Analyzer Generator <b>Lex</b> . . . . .	19
4.1	Structure of <b>Lex</b> Programs . . . . .	19
5	Finite Automata . . . . .	19
5.1	Nondeterministic Finite Automata . . . . .	19
5.2	Transition Tables . . . . .	20
5.3	Acceptance of Input Strings by Automata . . . . .	20
5.4	Deterministic Finite Automata . . . . .	20
6	From Regular Expressions to Automata . . . . .	21
6.1	Conversion of an NFA to a DFA . . . . .	21
6.2	Simulation of an NFA . . . . .	22
6.3	Efficiency of NFA Simulation . . . . .	23
6.4	Construction of an NFA from a Regular Expression . . . . .	23
7	Design of a Lexical-Analyzer Generator . . . . .	25
7.1	DFA's for Lexical Analyzers . . . . .	25
8	Optimization of DFA-Based Pattern Matchers . . . . .	25
8.1	Important States of an NFA . . . . .	25
8.2	Converting a Regular Expression Directly to a DFA . . . . .	25
8.3	Minimizing the Number of States of a DFA . . . . .	26
<b>4</b>	<b>Syntax Analysis</b>	<b>28</b>
1	Introduction . . . . .	28

1.1	Representative Grammars . . . . .	28
1.2	Syntax Error Handling . . . . .	28
1.3	Error-Recovery Strategies . . . . .	29
2	Context-Free Grammars . . . . .	29
2.1	The Formal Definition of a Context-Free Grammar . . . . .	29
2.2	Derivations . . . . .	29
2.3	Parse Trees and Derivations . . . . .	30
2.4	Ambiguity . . . . .	30
3	Writing a Grammar . . . . .	30
3.1	Eliminating Ambiguity . . . . .	30
3.2	Elimination of Left Recursion . . . . .	31
3.3	Left Factoring . . . . .	31
3.4	LL(1) Grammars . . . . .	32
3.5	Nonrecursive Predictive Parsing . . . . .	32
4	Bottom-Up Parsing . . . . .	33
4.1	Reductions . . . . .	33
4.2	Shift-Reduce Parsing . . . . .	33
4.3	Conflicts During Shift-Reduce Parsing . . . . .	33
5	Introduction to LR Parsing: Simple LR . . . . .	33
5.1	Items and the LR(0) Automaton . . . . .	33
5.2	The LR-Parsing Algorithm . . . . .	34
5.3	Constructing SLR-Parsing Tables . . . . .	34
5.4	Viable Prefixes . . . . .	35

---

---

# CHAPTER 1

---

## INTRODUCTION

The world as we know it depends on programming languages, because all the software running on all the computers was written in some programming language. But, before a program can be run, it first must be translated into a form in which it can be executed by a computer.

The software systems that do this translation are called *compilers*.

### 1 Language Processors

Simply stated, a compiler is a program that can read a program in one language—the *source* language—and translate it into an equivalent program in another language—the *target* language.

An *interpreter* is another common kind of language processor.

The task of collecting the source program is sometimes entrusted to a separate program, called a *preprocessor*.

The compiler may produce an assembly-language program as its output, because assembly language is easier to produce as output and is easier to debug. The assembly language is then processed by a program called an *assembler* that produces relocatable machine code as its output.

The *linker* resolves external memory addresses, where the code in one file may refer to a location in another file. The *loader* then puts together all of the executable object files into memory for execution.

### 2 The Structure of a Compiler

Up to this point we have treated a compiler as a single box that maps a source program into a semantically equivalent target program. If we open up this box a little, we see that there are two parts to this mapping: analysis and synthesis.

The *analysis* part breaks up the source program into constituent pieces and imposes a grammatical structure on them. The analysis part also collects information about the source program and stores it in a data structure called a *symbol table*, which is passed along with the intermediate representation to the synthesis part.

The *synthesis* part constructs the desired target program from the intermediate representation and the information in the symbol table. The analysis part is often called the *front end* of the compiler; the synthesis part is the *back end*.

If we examine the compilation process in more detail, we see that it operates as a sequence of *phases*, each of which transforms one representation of the source program to another.

## 2.1 Lexical Analysis

The first phase of a compiler is called *lexical analysis* or *scanning*. The lexical analyzer reads the stream of characters making up the source program and groups the characters into meaningful sequences called *lexemes*. For each lexeme, the lexical analyzer produces as output a *token* of the form

$$\langle token\text{-}name, attribute\text{-}value \rangle$$

that is passes on to the subsequent phase, syntax analysis. In the token, the first component *token-name* is an abstract symbol that is used during syntax analysis, and the second component *attribute-value* points to an entry in the symbol table for this token.

## 2.2 Syntax Analysis

The second phase of the compiler is *syntax analysis* or *parsing*. A typical representation is a *syntax tree* in which each interior node represents an operation and the children of the node represent the arguments of the operation.

## 2.3 Semantic Analysis

The *semantic analyzer* uses the syntax tree and the information in the symbol table to check the source program for semantic consistency with the language definition.

An important part of semantic analysis is *type checking*, where the compiler checks that each operator has matching operands.

The language specification may permit some type conversions called *coercions*.

## 2.4 Intermediate Code Generation

We consider an intermediate form called *three-address code*, which consists of a sequence of assembly-like instructions with three operands per instruction.

## 2.5 The Grouping of Phases into Passes

In an implementation, activities from several phases may be grouped together into a *pass* that reads an input file and writes an output file.

## 2.6 Compiler-Construction Tools

Some commonly used compiler-construction tools include

1. *Parser generators* that automatically produce syntax analyzers from a grammatical description of a programming language.
2. *Scanner generators* that produce lexical analyzers from a regular-expression description of the tokens of a language.

3. *Syntax-directed translation engines* that produce collections of routines for walking a parse tree and generating intermediate code.
4. *Code-generator generators* that produce a code generator from a collection of rules for translating each operation of the intermediate language into the machine language for a target machine.
5. *Data-flow analysis engines* that facilitate the gathering of information about how values are transmitted from one part of a program to each other part.
6. *Compiler-construction toolkits* that provide an integrated set of routines for construction various phases of a compiler.

## 3 The Evolution of Programming Language

### 3.1 The Move to Higher-Level Languages

One classification is by generation. *First-generation languages* are the machine languages, *second-generation* the assembly languages, and *third-generation* the higher-level languages. *Fourth-generation languages* are languages designed for specific applications. The term *fifth-generation language* has been applied to logic- and constraint-based languages.

Another classification of languages uses the term *imperative* for languages in which a program specifies *how* a computation is to be done and *declarative* for languages in which a program specifies *what* computation is to be done.

The term *von Neumann language* is applied to programming languages whose computational model is based on the von Neumann computer architecture.

An *object-oriented language* is one that supports object-oriented programming, a programming style in which a program consists of a collection of objects that interact with one another.

*Scripting languages* are interpreted languages with high-level operators designed for "gluing together" computations.

## 4 Applications of Compiler Technology

### 4.1 implementation of High-Level Programming Languages

A body of compiler optimizations, known as *data-flow optimizations*, has been developed to analyze the flow of data through the program and removes redundancies across these constructs.

Object-oriented programs are different from those written in many other languages, in that they consist of many more, but smaller, procedures (called *methods* in object-oriented terms).

### 4.2 Optimizations for Computer Architectures

Almost all high-performance systems take advantage of the same two basic techniques: *parallelism* and *memory hierarchies*. Parallelism can be found at several levels: at the *in-*

*struction level*, where multiple operations are executed simultaneously and at the *processor level*, where different threads of the same application are run on different processors.

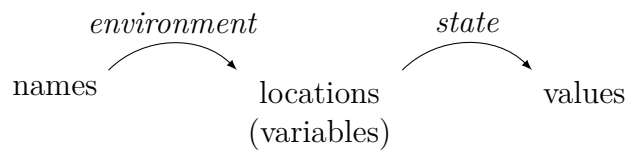
## 5 Programming Language Basics

### 5.1 The Static/Dynamic Distinction

If a language uses a policy that allows the compiler to decide an issue, then we say that the language uses a *static* policy or that the issue can be decided at *compile time*. On the other hand, a policy that only allows a decision to be made when we execute the program is said to be a *dynamic policy* or to require a decision at *run time*.

The *scope* of a declaration of  $x$  is the region of the program in which uses of  $x$  refer to this declaration. A language uses *static scope* or *lexical scope* if it is possible to determine the scope of a declaration by looking only at the program. Otherwise, the language uses *dynamic scope*.

### 5.2 Environments and States



**Figure 1.1:** Two-stage mapping from names to values

The association of names with locations in memory (the *store*) and then with values can be described by two mappings that change as the program runs:

1. The *environment* is a mapping from names to locations in the store.
2. The *state* is a mapping from locations in store to their values.

The environment and state mappings in Fig. 1.1 are dynamic, but there are a few exceptions:

1. *Static versus dynamic binding* of names to locations.
2. *Static versus dynamic binding* of locations to values.

### Names, Identifiers, and Variables

An *identifier* is a string of characters, typically letters or digits, that refers to (identifies) an entity. Composite names are called *qualified* names.

A *variable* refers to a particular location of the store.



### 5.3 Static Scope and Block Structure

The scope rules for C are based on program structure; the scope of a declaration is determined implicitly by where the declaration appears in the program. Later languages also provide explicit control over scopes through the use of keywords like **public**, **private** and **protected**.

A *block* is a grouping of declarations and statements. C uses braces { and } to delimit a block; the alternative use of **begin** and **end** for the same purpose dates back to Algol.

In C, the syntax of blocks is given by

1. One type of statement is a block. Blocks can appear anywhere that other types of statement can appear.
2. A block is a sequence of declarations followed by a sequence of statements, all surrounded by braces.

Note that this syntax allows blocks to be nested inside each other. This nesting property is referred to as *block structure*.

### 5.4 Explicit Access Control

Through the use of keywords like **public**, **private**, and **protected**, object-oriented languages provide explicit control over access to member names in a superclass. These keywords support *encapsulation* by restricting access.

### 5.5 Dynamic Scope

Technically, any scoping policy is dynamic if it is based on factor(s) that can be known only when the program executes. The term *dynamic scope*, however, usually refers to the following policy: a use of a name  $x$  refers to the declaration of  $x$  in the most recently called procedure with such a declaration.

#### Declarations and Definitions

In C++, a method is declared in a class definition, by giving the types of the arguments and result of the method (often called the *signature* for the method).

### 5.6 Parameter Passing Mechanisms

*Actual parameters* (the parameters used in the call of a procedure) are associated with the *formal parameters* (those used in the procedure definition).

#### Call-by-Value

In *call-by-value*, the actual parameter is evaluated (if it is an expression) or copied (if it is a variable).

## Call-by-Reference

In *call-by-reference*, the address of the actual parameter is passed to the callee as the value of the corresponding formal parameter.

## 5.7 Aliasing

It is possible that two formal parameters can refer to the same location; such variables are said to be *aliases* of one another.

---

---

# CHAPTER 2

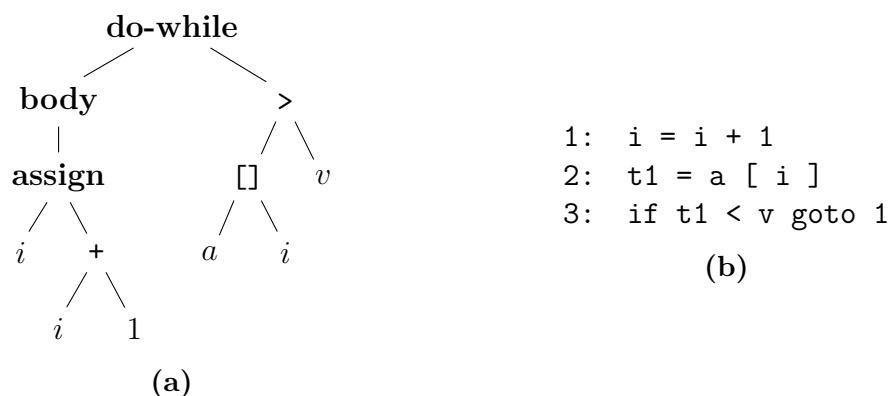
---

## A SIMPLE SYNTAX-DIRECTED TRANSLATOR

### 1 Introduction

The *syntax* of a programming language defines what its programs, while the *semantics* of the language defines what its program mean; that is, what each program does when it executes.

A lexical analyzer allows a translator to handle mutlicharacter constructs like identifiers, which are written as sequences of charactersm, but are treated as units called *tokens* during syntax analysis.



**Figure 2.1:** Intermediate code for "do i=i+1; while(a[i]<v);"

Two forms of intermediate code are illustrated in Fig. 2.1. One form, called *abstract syntax trees* or simply *syntax trees*, represents the hierarchical systematic structure of the source program.

### 2 Syntax Definition

A grammar naturally describes the hierarchical structure of most programming language constructs. For example, an if-else statement in Java can have the form

**if** (expression) statement **else** statement

Using the variable *expr* to denote an expression and the variable *stmt* to denote a statement, this structuring rule can be expressed as

$$stmt \rightarrow \text{if } (expr) \text{ } stmt \text{ else } stmt$$

in which the arrow may be read as "can have the form." Such a rule is called a *production*. In a production, lexical elements are called *terminals*. Variables like *expr* and *stmt* represent sequences of terminals and are called *nonterminals*.

## 2.1 Definition of Grammars

A *context-free grammar* has four components:

1. A set of *terminal* symbols, sometimes referred to as "tokens."
2. A set of *nonterminals*, sometimes called "syntactic variables."
3. A set of *productions*, where each production consists of a nonterminal, called the *head* or *left side* of the production, an arrow, and a sequence of terminals and/or nonterminals, called the *body* or *right side* of the production.
4. A designation of one of the nonterminals as the *start* symbol.

### Tokens Versus Terminals

A token consists of two components, a token name and an attribute value. The token names are abstract symbols that are used by the parser for syntax analysis. Often, we shall call these token names *terminals*, since they appear as terminal symbols in the grammar for a programming language.

We say a production is *for* a nonterminal if the nonterminal is the head of the production. The string of zero terminals, written as  $\epsilon$ , is called the *empty* string.

## 2.2 Derivations

The terminal strings that can be derived from the start symbol form the *language* defined by the grammar.

*Parsing* is the problem of taking a string of terminals and figuring out how to derive it from the start symbol of the grammar, and if it cannot be derived from the start symbol of the grammar, then reporting syntax errors within the string.

## 2.3 Parse Trees

A parse tree pictorially shows how the start symbol of a grammar derives a string in the language.

Formally, given a context-free grammar, a *parse tree* according to the grammar is a tree with the following properties:

1. The root is labeled by the start symbol.

2. Each leaf is labeled by a terminal or by  $\epsilon$ .
3. Each interior node is labeled by a nonterminal.
4. If  $A$  is the nonterminal labeling some interior node and  $X_1, X_2, \dots, X_n$  are the labels of the children of that node from left to right, then there must be a production  $A \rightarrow X_1 X_2 \dots X_n$ .

### Tree Terminology

Tree data structures figure prominently in compiling.

- A tree consists of one or more *nodes*. Nodes may have *labels*.
- Exactly one node is the *root*. All nodes except the root have a unique *parent*; the root has no parent.
- If node  $N$  is the parent of node  $M$ , then  $M$  is a *child* of  $N$ . The children of one node are called *siblings*. They have an order, *from the left*, and when we draw trees, we order the children
- A node with no children is called a *leaf*. Other nodes – those with one or more children – are *interior nodes*.
- A *descendant* of a node  $N$  is either  $N$  itself, a child of  $N$ , a child of a child of  $N$ , and so on, for any number of levels. We say node  $N$  is an *ancestor* of node  $M$  if  $M$  is a descendant of  $N$ .

From left to right, the leaves of a parse tree form the *yield* of the tree, which is the string *generated* or *derived* from the nonterminal at the root of the parse tree.

The process of finding a parse tree for a given string of terminals is called *parsing* that string.

## 2.4 Ambiguity

We have to be careful in talking about *the* structure of a string according to a grammar. A grammar can have more than one parse tree generating a given string of terminals. Such a grammar is said to be *ambiguous*.

## 2.5 Associativity of Operators

We say that the operator  $+$  *associates* to the left, because an operand with plus signs on both sides of it belongs to the operator to its left.

## 2.6 Precedence of Operators

We say that  $*$  has *higher precedence* than  $+$  if  $*$  takes its operands before  $+$  does.

### 3 Syntax-Directed Translation

This section introduces two concepts related to syntax-directed translation:

- *Attributes*. An *attribute* is any quantity associated with a programming construct.
- (*Syntax-directed*) *translation schemes*. A *translation scheme* is a notation for attaching program fragments to the productions of a grammar.

#### 3.1 Postfix Notation

The *postfix notation* for an expression  $E$  can be defined inductively as follows:

1. If  $E$  is a variable or constant, then the postfix notation for  $E$  is  $E$  itself.
2. If  $E$  is an expression of the form  $E_1 \text{ op } E_2$ , where **op** is any binary operator, then the postfix notation for  $E$  is  $E'_1 E'_2 \text{ op}$ , where  $E'_1$  and  $E'_2$  are the postfix notations for  $E_1$  and  $E_2$ , respectively.
3. If  $E$  is a parenthesized expression of the form  $(E_1)$ , then the postfix notation for  $E$  is the same as the postfix notation for  $E_1$ .

No parentheses are needed in postfix notation, because the position and *arity* (number of arguments) of the operators permits only one decoding of a postfix expression.

#### 3.2 Synthesized Attributes

A *syntax-directed definition* associates:

1. With each grammar symbol, a set of attributes, and
2. With each production, a set of *semantic rules* for computing the values of the attributes associated with the symbols appearing in the production.

A parse tree showing the attribute values at each node is called an *annotated* parse tree.

An attribute is said to be *synthesized* if its value at a parse-tree node  $N$  is determined from attribute values at the children of  $N$  and at  $N$  itself.

#### 3.3 Tree Traversals

A *traversal* of a tree starts at the root and visits each node of the tree in some order.

A *depth-first* traversal starts at the root and recursively visits the children of each node in any order, not necessarily from left to right.

Synthesized attributes can be evaluated during any *bottom-up* traversal, that is, a traversal that evaluates attributes at a node after having evaluated attributes at its children.

#### 3.4 Translation Schemes

## Preorder and Postorder Traversals

Often, we traverse a tree to perform some particular action at each node. If the action is done when we first visit a node, then we may refer to the traversal as a *preorder traversal*. Similarly, if the action is done just before we leave a node for the last time, then we say it is a *postorder traversal* of the tree.

The *preorder* of a (sub)tree rooted at node  $N$  consists of  $N$ , followed by the preorders of the subtrees of each of its children, if any, from the left. The *postorder* of a (sub)tree rooted at  $N$  consists of the postorders of each of the subtrees for the children of  $N$ , if any, from the left, followed by  $N$  itself.

Program fragments embedded within production bodies are called *semantic actions*.

## 4 Parsing

Most parsing methods fall into one of two classes, called the *top-down* and *bottom-up* methods.

### 4.1 Top-Down Parsing

The current terminal being scanned in the input is frequently referred to as the *lookahead* symbol.

### 4.2 Predictive Parsing

*Recursive-descent parsing* is a top-down method of syntax analysis in which a set of recursive procedures is used to process the input. Here, we consider a simple form of recursive-descent parsing, called *predictive parsing*, in which the lookahead symbol unambiguously determines the flow of control through the procedure body for each nonterminal.

### 4.3 Designing a Predictive Parser

Recall that a *predictive parser* is a program consisting of a procedure for every nonterminal.

### 4.4 Left Recursion

Consider a nonterminal  $A$  with two productions

$$A \rightarrow A\alpha \mid \beta$$

where  $\alpha$  and  $\beta$  are sequences of terminals and nonterminals that do not start with  $A$ .

The nonterminal  $A$  and its production are said to be *left recursive*, because the production  $A \rightarrow A\alpha$  has  $A$  itself as the leftmost symbol on the right side.

The same effect can be achieved by rewriting the productions for  $A$  in the following manner, using a new nonterminal  $R$ :

$$\begin{aligned} A &\rightarrow \beta R \\ R &\rightarrow \alpha R \mid \epsilon \end{aligned}$$

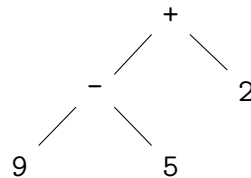
Nonterminal  $R$  and its production  $R \rightarrow \alpha R$  are *right recursive* because this production for  $R$  has  $R$  itself as the last symbol on the right side.

## 5 A Translator for Simple Expressions

### 5.1 Abstract and Concrete Syntax

In an *abstract syntax tree* for an expression, each interior node represents an operator; the children of the node represent the operands of the operator.

Abstract syntax trees, or simply *syntax trees*, resemble parse trees to an extent. Many nonterminals of a grammar represent programming constructs, but others are "helpers" of one sort or another. In the syntax tree, these helpers typically are not needed and are hence dropped. To emphasize the contrast, a parse tree is sometimes called a *concrete syntax tree*, and the underlying grammar is called a *concrete syntax* for the language.



**Figure 2.2:** Syntax tree for 9-5+2

In the syntax tree in Fig. 2.2, each interior node is associated with an operator, with no "helper" nodes for *single productions* (a production whose body consists of a single nonterminal, and nothing else) or for  $\epsilon$ -productions.

### 5.2 Simplifying the Translator

When the last statement executed in a procedure body is a recursive call to the same procedure, the call is said to be *tail recursive*.

### 5.3 The Complete Program

```

import java.io.*
class Parser {
    static int lookahead;

    public Parser() throws IOException {
        lookahead = System.in.read();
    }

    void expr() throws IOException {

```



```

        term();
    while(true) {
        if (lookahead == '+') {
            match('+'); term(); System.out.write('+');
        }
        else if (lookahead == '-') {
            match('-'); term(); System.out.write('-');
        }
        else return;
    }
}

void term() throws IOException {
    if (Character.isDigit((char)lookahead)) {
        System.out.write((char)lookahead); match(lookahead);
    }
    else throw new Error("syntax error");
}

}

public class Postfix {
    public static void main(String[] args) throws IOException {
        Parser parse = new Parser();
        parse.expr(); System.out.write('\n');
    }
}

```

**Figure 2.3:** Java program to translate infix expressions into postfix form

The function `Parser`, with the same name as its class, is a *constructor*; it is called automatically when an object of the class is created.

The construction `(char)lookahead` *casts* or coerces `lookahead` to be a character.

## 6 Lexical Analysis

A sequence of input characters that comprises a single token is called a *lexeme*.

### 6.1 Recognizing Keywords and Identifiers

Most languages use fixed character strings as punctuation marks or to identify constructs. Such character strings are called *keywords*.

Keywords generally satisfy the rules for forming identifiers, so a mechanism is needed for deciding when a lexeme forms a keyword and when it forms an identifier. The problem is easier to resolve if keywords are *reserved*; i.e., if they cannot be used as identifiers.

The lexical analyzer in this section solves two problems by using a table to hold character strings:

- *Single Representation.*
- *Reserved Words.*

In Java, a string table can be implemented as a hash table using a class called *Hashtable*.

## 7 Symbol Tables

*Symbol tables* are data structures that are used by compilers to hold information about source-program constructs.

### 7.1 Symbol Table Per Scope

The term *scope* by itself refers to a portion of a program that is the scope of one or more declarations.

The *most-closely nested* rule for blocks is that an identifier  $x$  is in the scope of the most-closely nested declaration of  $x$ ; that is, the declaration of  $x$  found by examining blocks inside-out, starting with the block in which  $x$  appears.

## 8 Intermediate Code Generation

### 8.1 Two Kinds of Intermediate Representations

In addition to creating an intermediate representation, a compiler front end checks that the source program follows the syntactic and semantic rules of the source language. This checking is called *static checking*; in general "static" means "done by the compiler."

### 8.2 Construction of Syntax Trees

#### Syntax Trees for Expressions

The table in Fig. 2.4 specifies the correspondence between the concrete and abstract syntax for several of the operators of Java.

The subscript *unary* in  $\neg_{unary}$  is solely to distinguish a leading unary minus sign from a binary minus sign.

Concrete Syntax	Abstract Syntax
=	<b>assign</b>
	<b>cond</b>
&&	<b>cond</b>
== !=	<b>rel</b>
< <= >= >	<b>rel</b>
+ -	<b>op</b>
* / %	<b>op</b>
!	<b>not</b>
$\neg_{unary}$	<b>minus</b>
[]	<b>access</b>

**Figure 2.4:** Concrete and abstract syntax for several Java operators

### 8.3 Static Checking

Static checking includes:

- *Syntactic Checking.*
- *Type Checking.*

#### L-values and R-values

The terms *l-value* and *r-value* refer to values that are appropriate on the left and right sides of an assignment, respectively.

#### Type Checking

Type checking assures that the type of a construct matches that expected by its context.

The idea of matching actual with expected types continues to apply, even in the following situations:

- *Coercions.* A *coercion* occurs if the type of an operand is automatically converted to the type expected by the operator.
- *Overloading.* A symbol is said to be *overloaded* if it has different meanings depending on its context.

---

---

# CHAPTER 3

---

## LEXICAL ANALYSIS

To implement a lexical analyzer by hand, it helps to start with a diagram or other description for the lexemes of each token. We can then write code to identify each occurrence of each lexeme on the input and to return information about the token identified.

We can also produce a lexical analyzer automatically by specifying the lexeme patterns to a *lexical-analysis generator* and compiling those patterns into code that functions as a lexical analyzer.

### 1 The Role of the Lexical Analyzer

Since the lexical analyzer is the part of the compiler that reads the source text, it may perform certain other tasks besides identification of lexemes. One such task is stripping out comments and *whitespace* (blank, newline, tab, and perhaps other characters that are used to separate tokens in the input).

Sometimes, lexical analyzers are divided into a cascade of two processes:

- a) *Scanning* consists of the simple processes that do not require tokenization of the input.
- b) *Lexical analysis* proper is the more complex portion, where the scanner produces the sequence of tokens as output.

#### 1.1 Tokens, Patterns, and Lexemes

When discussing lexical analysis, we use three related but distinct terms:

- A *token* is a pair consisting of a token name and an optional attribute value.
- A *pattern* is a description of the form that the lexemes of a token may take. In the case of a keyword as a token, the pattern is just the sequence of characters that form the keyword. For identifiers and some other tokens, the pattern is a more complex structure that is *matched* by many strings.
- A *lexeme* is a sequence of characters in the source program that matches the pattern for a token and is identified by the lexical analyzer as an instance of that token.

## 2 Specification of Tokens

### Can We Run Out of Buffer Space

To avoid problems with long character strings, we can treat them as a concatenation of components, one from each line over which the string is written.

A more difficult problem occurs when arbitrarily long lookahead may be needed. For example, some languages like PL/I do not treat keywords as *reserved*; that is, you can use identifiers with the same name as a keyword.

### 2.1 Strings and Languages

An *alphabet* is any finite set of symbols. The set  $\{0, 1\}$  is the *binary alphabet*.

A *string* over an alphabet is a finite sequence of symbols drawn from that alphabet. The *empty string*, denoted  $\epsilon$ , is the string of length zero.

A *language* is any countable set of strings over some fixed alphabet. Abstract languages like  $\emptyset$ , the *empty set* are languages under this definition.

### Terms for Parts of Strings

The following string-related terms are commonly used:

1. A *prefix* of string  $s$  is any string obtained by removing zero or more symbols from the end of  $s$ .
2. A *suffix* of string  $s$  is any string obtained by removing zero or more symbols from the beginning of  $s$ .
3. A *substring* of  $s$  is obtained by deleting any prefix and any suffix from  $s$ .
4. The *proper* prefixes, suffixes, and substrings of a string  $s$  are those, prefixes, suffixes, and substrings, respectively, of  $s$  that are not  $\epsilon$  or not equal to  $s$  itself.
5. A *subsequence* of  $s$  is any string formed by deleting zero or more not necessarily consecutive positions of  $s$ .

If  $x$  and  $y$  are strings, then the *concatenation* of  $x$  and  $y$ , denoted  $xy$ , is the string formed by appending  $y$  to  $x$ .

### 2.2 Operations and Languages

The (*Kleene*) *closure* of a language  $L$ , denoted  $L^*$ , is the set of strings you get by concatenating  $L$  zero or more times.

## 2.3 Regular Expressions

A language that can be defined by a regular expression is called a *regular set*. If two regular expressions  $r$  and  $s$  denote the same regular set, we say they are *equivalent* and write  $r = s$ .

## 2.4 Regular Definitions

If  $\Sigma$  is an alphabet of basic symbols, then a *regular definition* is a sequence of definitions of the form:

$$\begin{array}{lcl} d_1 & \rightarrow & r_1 \\ d_2 & \rightarrow & r_2 \\ & \dots & \\ d_n & \rightarrow & r_n \end{array}$$

where:

1. Each  $d_i$  is a new symbol, not in  $\Sigma$  and not the same as any other of the  $d$ 's, and
2. Each  $r_i$  is a regular expression over the alphabet  $\Sigma \cup \{d_1, d_2, \dots, d_{i-1}\}$ .

## 2.5 Extensions of Regular Expressions

Here we mention a few notational extensions that were first incorporated into Unix utilities that are particularly useful in the specification lexical analyzer.

1. *One or more instances.*
2. *Zero or one instance.*
3. *Character classes.*

# 3 Recognition of Tokens

## 3.1 Transition Diagrams

*Transition diagrams* have a collection of nodes or circles, called *states*.

*Edges* are directed from one state of the transition diagram to another. Each edge is *labeled* by a symbol or set of symbols. We shall assume that all our transition diagrams are *deterministic*, meaning that there is never more than one edge out of a given state with a given symbol among its labels. Some important conventions about transition diagrams are:

- Certain states are said to be *accepting*, or *final*.
- One state is designated the *start state*, or *initial state*; it is indicated by an edge, labeled "start," entering from nowhere.

## 3.2 Recognition of Reserved Words and Identifiers

Usually, keywords are reserved, so they are not identifiers even though they look like identifiers.

## 4 The Lexical-Analyzer Generator Lex

The input notation for the **Lex** tool is referred to as the *Lex language* and the tool itself is the *Lex compiler*.

### 4.1 Structure of Lex Programs

A **Lex** program has the following form:

```
declarations
%%
transition rules
%%
auxiliary functions
```

The declarations section includes declarations of variables, *manifest constants* (identifiers declared to stand for a constant).

## 5 Finite Automata

We shall now discover how **Lex** turns its input program into a lexical analyzer. At the heart of the transition is the formalism known as *finite automata*. These are essentially graphs, like transition diagrams, with a few differences:

1. Finite automata are *recognizers*; they simply say "yes" or "no" about each possible input string.
2. Finite automata come in two flavors:
  - (a) *Nondeterministic finite automata* (NFA) have no restrictions on the labels of their edges.
  - (b) *Deterministic finite automata* (DFA) have, for each state, and for each symbol of its input alphabet exactly one edge with that symbol leaving that state.

Both deterministic and nondeterministic finite automata are capable of recognizing the same languages. In fact these languages are exactly the same languages, called the *regular languages*, the regular expressions can describe.<sup>1</sup>

### 5.1 Nondeterministic Finite Automata

A *nondeterministic finite automata* (NFA) consists of:

1. A finite set of state  $S$ .
2. A set of input symbols  $\Sigma$ , the *input alphabet*.

---

<sup>1</sup>There is a small lacuna: as we defined them, regular expressions cannot describe the empty language, since we would never want to use this pattern in practice. However, finite automata *can* define the empty language.

3. A *transition function* that gives, for each state, and for each symbol in  $\Sigma \cup \{\epsilon\}$  a set of *next states*.
4. A state  $s_0$  from  $S$  that is distinguished as the *start state* (or *initial state*).
5. A set of states  $F$ , a subset of  $S$ , that is distinguished as the *accepting states* (or *final states*).

We can represent either an NFA or DFA by a *transition graph*, where the nodes are states and the labeled edges represent the transition function.

## 5.2 Transition Tables

We can also represent an NFA by a *transition table*, whose rows correspond to states, and whose columns correspond to the input symbols and  $\epsilon$ .

## 5.3 Acceptance of Input Strings by Automata

An NFA *accepts* input string  $x$  if and only if there is some path in the transition graph from the start state to one of the accepting states, such that the symbols along the path spell out  $x$ .

The *language defined* (or *accepted*) by an NFA is the set of strings labeling some path from the start to an accepting state.

## 5.4 Deterministic Finite Automata

A *deterministic finite automata* (DFA) is a special case of an NFA where:

1. There are no moves on input  $\epsilon$ , and
2. For each state  $s$  and input symbol  $a$ , there is exactly one edge out of  $s$  labeled  $a$ .

**Algorithm:** Simulating a DFA.

**INPUT:** An input string  $x$  terminated by an end-of-file character **eof**. A DFA  $D$  with start state  $s_0$ , accepting states  $F$ , and transition function *move*.

**OUTPUT:** Answer "yes" if  $D$  accepts  $x$ ; "no" otherwise.

**METHOD:** Apply the algorithm in Fig. 3.1 to the input string  $x$ . The function *move*( $s, c$ ) gives the state to which there is an edge from state  $s$  on input  $c$ . The function *nextChar* returns the next character of the input string  $x$ . ■

```

s = s0;
c = nextChar();
while ( c != eof ) {
    s = move(s, c);
    c = nextChar();
}
if ( s is in F ) return "yes";
else return "no";

```



Figure 3.1: Simulating a DFA

## 6 From Regular Expressions to Automata

### 6.1 Conversion of an NFA to a DFA

**Algorithm:** The *subset construction* of a DFA from an NFA.

**INPUT:** An NFA  $N$ .

**OUTPUT:** A DFA  $D$  accepting the same language as  $N$ .

**METHOD:** Our algorithm constructs a transition table  $Dtran$  for  $D$ . Each state of  $D$  is a set of NFA states, and we construct  $Dtran$  so  $D$  will simulate "in parallel" all possible moves  $N$  can make on a given input string. Our first problem is to deal with  $\epsilon$ -transitions of  $N$  properly. In Fig. 3.2 we see the definitions of several functions that describe basic computations on the states of  $N$  that are needed in the algorithm. Note that  $s$  is a single state of  $N$ , while  $T$  is a set of states of  $N$ .

We must explore those sets of states that  $N$  can be in after seeing some input string. As a basis, before reading the first input symbol,  $N$  can be in any of the states of  $\epsilon$ -closure( $s_0$ ), where  $s_0$  is its start state. For the induction, suppose that  $N$  can be in set of states  $T$  after reading input string  $x$ . If it next reads input  $a$ , then  $N$  can immediately go to any of the states in  $move(T, a)$ . However, after reading  $a$ , it may also make several  $\epsilon$ -transitions; thus  $N$  could be in any state of  $\epsilon$ -closure( $move(T, a)$ ) after reading input  $xa$ . Following these ideas, the construction of the set of  $D$ 's states,  $Dstates$ , and its transition function  $Dtran$ , is shown in Fig. 3.3.

The start state of  $D$  is  $\epsilon$ -closure( $s_0$ ), and the accepting states of  $D$  are all those sets of  $N$ 's states that include at least one accepting state of  $N$ . To complete our description of the subset construction, we need only to show how initially,  $\epsilon$ -closure( $s_0$ ) is the only state in  $Dstates$ , and it is unmarked;  $\epsilon$ -closure( $T$ ) is computed for any set of NFA states  $T$ . This process, shown in Fig. 3.4, is a straightforward search in graph from a set of states. In this case, imagine that only the  $\epsilon$ -labeled edges are available in the graph. ■

Operation	Description
$\epsilon$ -closure( $s$ )	Set of NFA states reachable from NFA state $s$ on $\epsilon$ -transitions alone.
$\epsilon$ -closure( $T$ )	Set of NFA states reachable from NFA state $s$ in set $T$ on $\epsilon$ -transitions alone; $= \cup_{s \text{ in } T} \epsilon$ -closure( $s$ ).
$move(T, a)$	Set of NFA states to which there is transition on input symbol $a$ from some state $s$ in $T$ .

Figure 3.2: Operations on NFA states

```

while ( there is an unmarked state  $T$  in  $Dstates$  ) {
    mark  $T$ ;
    for ( each input symbol  $a$  ) {
         $U = \epsilon\text{-closure}(\text{move}(T, a))$ ;
        if (  $U$  is not in  $Dstates$  )
            add  $U$  as an unmarked state to  $Dstates$ ;
         $Dtran[T, a] = U$ ;
    }
}

```

**Figure 3.3:** The subset construction

```

push all states of  $T$  onto  $stack$ ;
initialize  $\epsilon\text{-closure}(T)$  to  $T$ ;
while (  $stack$  is not empty ) {
    pop  $t$ , the top element, off  $stack$ ;
    for ( each state  $u$  with an edge from  $t$  to  $u$  labeled  $\epsilon$  )
        if (  $u$  is not in  $\epsilon\text{-closure}(T)$  ) {
            add  $u$  to  $\epsilon\text{-closure}(T)$ ;
            push  $u$  onto  $stack$ ;
        }
}

```

**Figure 3.4:** Computing  $\epsilon\text{-closure}(T)$

## 6.2 Simulation of an NFA

**Algorithm:** Simulating an NFA.

**INPUT:** An input string  $x$  terminated by an end-of-file character **eof**. An NFA  $N$  with start state  $s_0$ , accepting states  $F$ , and transition function  $move$ .

**OUTPUT:** Answer "yes" if  $M$  accepts  $x$ ; "no" otherwise.

**METHOD:** The algorithm keeps a set of current states  $S$ , those that are reached from  $s_0$  following a path labeled by the inputs read so far. If  $c$  is the next input character, read by function  $nextChar()$ , then we first compute  $move(S, c)$  and then close that set using  $\epsilon\text{-closure}()$ . The algorithm is sketched in Fig 3.5. ■

```

1)  $S = \epsilon\text{-closure}(s_0)$ ;
2)  $c = nextChar()$ ;
3) while (  $c \neq eof$  ) {
4)      $S = \epsilon\text{-closure}(move(S, c))$ ;
5)      $c = nextChar()$ ;
6) }
7) if (  $S \cap F \neq \emptyset$  ) return "yes";
8) else return "no";

```

Figure 3.5: Simulating an NFA

### 6.3 Efficiency of NFA Simulation

#### Big-Oh Notation

Technically, we say a function  $f(n)$ , perhaps the running time of some step of an algorithm, is  $O(g(n))$  if there are constants  $c$  and  $n_0$ , such that whenever  $n \geq n_0$ , it is true that  $f(n) \leq cg(n)$ . The use of this *big-oh notation* enables us to avoid getting too far into the details of what we count as a unit of execution time, yet lets us express the rate at which the running time of an algorithm grows.

### 6.4 Construction of an NFA from a Regular Expression

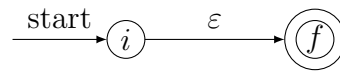
**Algorithm:** The McNaughton-Yamada-Thompson algorithm to convert a regular expression to an NFA.

**INPUT:** A regular expression  $r$  over alphabet  $\Sigma$ .

**OUTPUT:** An NFA  $N$  accepting  $L(r)$ .

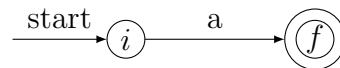
**METHOD:** Begin by parsing  $r$  into its constituent subexpressions. The rules for constructing an NFA consist of basic rules for handling subexpressions with no operators, and inductive rules for constructing larger NFA's from the NFA's for the immediate subexpressions of a given expression.

**BASIS:** For expression  $\epsilon$  construct the NFA



Here,  $i$  is a new state, the start state of this NFA, and  $f$  is another new state, the accepting state for the NFA.

For any subexpression  $a$  in  $\Sigma$ , construct the NFA

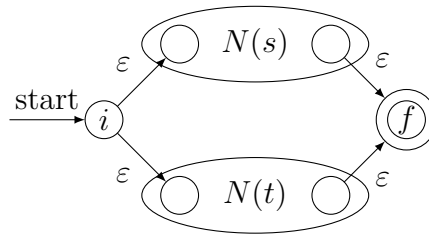


where again  $i$  and  $f$  are new states, the start and accepting states, respectively. Note that in both of the basis constructions, we construct a distinct NFA, with new states, for every occurrence of  $\epsilon$  or some  $a$  as a subexpression of  $r$ .

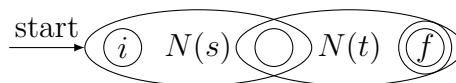
**INDUCTION:** Suppose  $N(s)$  and  $N(t)$  are NFA's for regular expression  $s$  and  $t$ , respectively.

- a) Suppose  $r = s|t$ . Then  $N(r)$ , the NFA for  $r$ , is constructed as in Fig. 3.6. Here,  $i$  and  $f$  are new states, the start and accepting states of  $N(r)$ , respectively. There are  $\epsilon$ -transitions from  $i$  to the start states of  $N(s)$  and  $N(t)$ , and each of their accepting states have  $\epsilon$ -transitions to the accepting state  $f$ . Note that the accepting states of  $N(s)$  and  $N(t)$  are not accepting in  $N(r)$ . Since any path from  $i$  to  $f$  must pass through either  $N(s)$  or  $N(t)$  exclusively, and since the label of that path is not changed by the  $\epsilon$ 's leaving  $i$  or entering  $f$ , we conclude that  $N(r)$  accepts  $L(s) \cup L(t)$ , which is the same as  $L(r)$ . That is, Fig. 3.6 is a correct construction for the union operator.

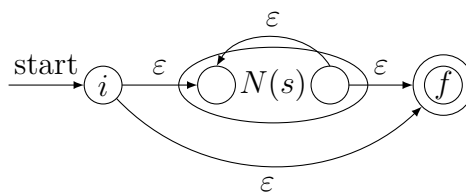
- b) Suppose  $r = st$ . Then construct  $N(r)$  as in Fig. 3.7. The start state of  $N(s)$  becomes the start state of  $N(r)$ , and the accepting state of  $N(t)$  is the only accepting state of  $N(r)$ . The accepting state of  $N(s)$  and the start state of  $N(t)$  are merged into a single state, with all the transitions in or out of either state. A path from  $i$  to  $f$  in Fig. 3.7 must go first through  $N(s)$ , and therefore its label will begin with some string in  $L(s)$ . The path then continues through  $N(t)$ , so the path's label finishes with a string in  $L(t)$ . Accepting states never have edges out and start states never have edges in, so it is not possible for a path to re-enter  $N(s)$  after leaving it. Thus  $N(r)$  accepts exactly  $L(s)L(t)$ , and it is a correct NFA for  $r = st$ .
- c) Suppose  $r = s^*$ . Then for  $r$  we construct the NFA  $N(r)$  shown in Fig. 3.8. Here,  $i$  and  $f$  are new states, the start state and lone accepting state of  $N(r)$ . To get from  $i$  to  $f$ , we can either follow the introduced path labeled  $\epsilon$ , which takes care of the one string in  $L(s)^0$ , or we can go to the start state of  $N(s)$ , through that NFA, then from its accepting state back to its start state zero or more times. These options allow  $N(r)$  to accept all the strings in  $L(s)^1$ ,  $L(s)^2$ , and so on, so the entire set of strings accepted by  $N(r)$  is  $L(s)^*$ .
- d) Finally, suppose  $r = (s)$ . Then  $L(r) = L(s)$ , and we can use the NFA  $N(s)$  as  $N(r)$ .



**Figure 3.6:** NFA for the union of two regular expressions



**Figure 3.7:** NFA for the concatenation of two regular expressions



**Figure 3.8:** NFA for the closure of a regular expression

## 7 Design of a Lexical-Analyzer Generator

### 7.1 DFA's for Lexical Analyzers

We simulate the DFA until at some point there is no next state (or strictly speaking, the next state is  $\emptyset$ , the *dead state* corresponding to the empty set of NFA states).

## 8 Optimization of DFA-Based Pattern Matchers

### 8.1 Important States of an NFA

We call a state of an NFA *important* if it has a non- $\epsilon$  out-transition.

By concatenating a unique right endmarker  $\#$  to a regular expression  $r$ , we give the accepting state for  $r$  a transition on  $\#$ , making it an important state of the NFA for  $(r)\#$ . In other words, by using the *augmented* regular expression  $(r)\#$ , we can forget about accepting states as the subset construction proceeds; when the construction is complete, any state with a transition on  $\#$  must be an accepting state.

It is useful to present the regular expression by its *syntax tree*, where the leaves correspond to operands and the interior nodes correspond to operators. An interior node is called a *cat-node*, *or-node*, or *star-node* if it is labeled by the concatenation operator (dot), union operator  $|$ , or star operator  $*$ , respectively.

Leaves in a syntax tree are labeled by  $\epsilon$  or by an alphabet symbol. To each leaf not labeled  $\epsilon$ , we attach a unique integer. We refer to this integer as the *position* of the leaf and also as a position of its symbol.

### 8.2 Converting a Regular Expression Directly to a DFA

**Algorithm:** Construction of a DFA from a regular expression  $r$ .

**INPUT:** A regular expression  $r$ .

**OUTPUT:** A DFA  $D$  that recognizes  $L(r)$ .

**METHOD:**

1. Construct a syntax tree  $T$  from the augmented regular expression  $(r)\#$ .
2. Compute *nullable*, *firstpos*, *lastpos*, and *followpos* for  $T$ .
3. Construct  $Dstates$ , the set of states of DFA  $D$ , and  $Dtran$ , the transition function for  $D$ , by the procedure of Fig. 3.9. The states of  $D$  are sets of positions in  $T$ . Initially, each state is "unmarked," and a state becomes "marked" just before we consider its out-transitions. The start state of  $D$  is *firstpos*( $n_0$ ), where node  $n_0$  is the root of  $T$ . The accepting states are those containing the position for the endmarker symbol  $\#$ .

```

initialize  $Dstates$  to contain only the unmarked state  $firstpos(n_0)$ ,
  where  $n_0$  is the root of syntax tree  $T$  for  $(r)\#$ ;
while ( there is an unmarked state  $S$  in  $Dstates$  ) {
  mark  $S$ ;
  for ( each input symbol  $a$  ) {
    let  $U$  be the union of  $followpos(p)$  for all  $p$ 
      in  $S$  that correspond to  $a$ ;
    if (  $U$  is not in  $Dstates$  )
      add  $U$  as an unmarked state to  $Dstates$ ;
     $Dtran[S, a] = U$ ;
  }
}

```

**Figure 3.9:** Construction of a DFA directly from a regular expression

### 8.3 Minimizing the Number of States of a DFA

We shall say that two automata are *the same up to the state names* if one can be transformed into the other by doing nothing more than changing the names of states.

We say that string  $x$  *distinguishes* state  $s$  from state  $t$  if exactly one of the states reached from  $s$  and  $t$  by following the path with label  $x$  is an accepting state. State  $s$  is *distinguishable* from state  $t$  if there is some string that distinguishes them.

**Algorithm:** Minimizing the number of states of a DFA.

**INPUT:** A DFA  $D$  with set of states  $S$ , input alphabet  $\Sigma$ , start state  $s_0$ , and set of accepting states  $F$ .

**OUTPUT:** A DFA  $D'$  accepting the same language as  $D$  and having as few states as possible.

**METHOD:**

1. Start with an initial partition  $\Pi$  with two groups,  $F$  and  $S - F$ , the accepting and nonaccepting states of  $D$ .
2. Apply the procedure of Fig. 3.10 to construct a new partition  $\Pi_{\text{new}}$ .
3. If  $\Pi_{\text{new}} = \Pi$ , let  $\Pi_{\text{final}} = \Pi$  and continue with step (4). Otherwise, repeat step (2) with  $\Pi_{\text{new}}$  in place of  $\Pi$ .
4. Choose one state in each group of  $\Pi_{\text{final}}$  as the *representative* for that group. The representatives will be the states of the minimum-state DFA  $D'$ . The other components of  $D'$  are constructed as follows:
  - (a) The start state of  $D'$  is the representative of the group containing the start state of  $D$ .
  - (b) The accepting states of  $D'$  are the representatives of those groups that contain an accepting state of  $D$ . Note that each group contains either only accepting states, or only nonaccepting states, because we started by separating those two classes of states, and the procedure of Fig. 3.10 always forms new groups that are subgroups of previously constructed groups.

- (c) Let  $s$  be the representative of some group  $G$  of  $\Pi_{\text{final}}$ , and let the transition of  $D$  from  $s$  on input  $a$  be to state  $t$ . Let  $r$  be the representative of  $t$ 's group  $H$ . Then in  $D'$ , there is a transition from  $s$  to  $r$  on input  $a$ . Note that in  $D$ , every state in group  $G$  must go to some state of group  $H$  on input  $a$ , or else, group  $G$  would have been split according to Fig. 3.10. ■

initially, let  $\Pi_{\text{new}} = \Pi$ ;

**for** ( each group  $G$  of  $\Pi$  ) {

    partition  $G$  into subgroups such that two states  $s$  and  $t$

        are in the same subgroup if and only if for all input symbols  $a$ , states  $s$  and  $t$  have transition to states in the same group of  $\Pi$ ;

    /\* at worst, a state will be in a subgroup by itself \*/

    replace  $G$  in  $\Pi_{\text{new}}$  by the set of all subgroups formed;

}

**Figure 3.10:** Construction of  $\Pi_{\text{new}}$

---

---

# CHAPTER 4

---

## SYNTAX ANALYSIS

### 1 Introduction

#### 1.1 Representative Grammars

Associativity and precedence are captured in the following grammar.  $E$  represents expressions consisting of terms separated by  $+$  signs,  $T$  represents terms consisting of factors separated by  $*$  signs, and  $F$  represents factors that can be either parenthesized expressions or identifiers:

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow ( E ) \mid \text{id} \end{aligned} \tag{4.1}$$

The following non-left-recursive variant of the expression grammar (4.1) will be used for top-down parsing:

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \mid \epsilon \\ T &\rightarrow FT' \\ T' &\rightarrow *FT' \mid \epsilon \\ F &\rightarrow ( E ) \mid \text{id} \end{aligned} \tag{4.2}$$

The following grammar treats  $+$  and  $*$  alike, so it is useful for illustrating techniques for handling ambiguities during parsing:

$$E \rightarrow E + E \mid E * E \mid ( E ) \mid \text{id} \tag{4.3}$$

#### 1.2 Syntax Error Handling

Common programming errors can occur at many different levels.

- *Lexical* errors include misspelling of identifiers, keywords, or operators and missing quotes around text intended as a string.
- *Syntactic* errors include misplaced semicolons or extra missing braces; that is, "{" or "}".
- *Semantic* errors include type mismatches between operators and operands.
- *Logical* errors can be anything from incorrect reasoning on the part of the programmer to the use in a C program of the assignment operator  $=$  instead of the comparison operator  $==$ .



Several parsing methods detect an error as soon as possible; that is, when the stream of tokens from the lexical analyzer cannot be parsed further according to the grammar for the language. More precisely, they have the *viable-prefix property*, meaning that they detect that an error has occurred as soon as they see a prefix of the input that cannot be completed to form a string in the language.

### 1.3 Error-Recovery Strategies

#### Panic-Mode Recovery

With this method, on discovering an error, the parser discards input symbols one at a time until one of a designated set of *synchronizing tokens* is found.

## 2 Context-Free Grammars

Using a syntactic variable *stmt* to denote statements and variable *expr* to denote expressions, the production

$$stmt \rightarrow \text{if} ( expr ) stmt \text{ else } stmt \quad (4.4)$$

specifies the structure of this form of conditional statement.

### 2.1 The Formal Definition of a Context-Free Grammar

A context-free grammar (grammar for short) consists of terminals, nonterminals, a start symbol, and productions.

1. *Terminals* are the basic symbols from which strings are formed.
2. *Nonterminals* are syntactic variables that denote sets of strings.
3. In a grammar, one nonterminal is distinguished as the *start symbol*, and the set of strings it denotes is the language generated by the grammar.
4. Each *production* consists of:
  - (a) A nonterminal called the *head* or *left side* of the production; this production defines some of the strings denoted by the head.
  - (b) The symbol  $\rightarrow$ .
  - (c) A *body* or *right side* consisting of zero or more terminals and nonterminals.

### 2.2 Derivations

Bottom-up parsing is related to a class of derivations known as "rightmost" derivations, in which the rightmost nonterminal is rewritten at each step.

For example, consider the following grammar, with a single nonterminal *E*, which adds a production  $E \rightarrow -E$  to the grammar (4.3):

$$E \rightarrow E + E \mid E * E \mid - E \mid ( E ) \mid \text{id} \quad (4.5)$$

We can take a single  $E$  and repeatedly apply productions in any order to get a sequence of replacements. For example,

$$E \Rightarrow -E \Rightarrow -(E) \Rightarrow -(\mathbf{id})$$

We call such a sequence of replacements a *derivation* of  $-(\mathbf{id})$  from  $E$ .

When a sequence of derivation steps  $\alpha_1 \Rightarrow \alpha_2 \Rightarrow \cdots \Rightarrow \alpha_n$  rewrites  $\alpha_1$  to  $\alpha_n$ , we say  $\alpha_1$  *derives*  $\alpha_n$ .

If  $S \xRightarrow{*} \alpha$ , where  $S$  is the start symbol of a grammar  $G$ , we say that  $\alpha$  is a *sentential form* of  $G$ . A *sentence* of  $G$  is a sentential form with no nonterminals. The *language generated by* a grammar is its set of sentences. A language that can be generated by a grammar is said to be a *context-free language*. If two grammars generate the same language, the grammars are said to be *equivalent*.

To understand how parsers work, we shall consider derivations in which the nonterminal to be replaced at each step is chosen as follows:

1. In *leftmost* derivations, the leftmost nonterminal in each sentential is always chosen.
2. In *rightmost* derivations, the rightmost nonterminal is always chosen; we write  $\alpha \Rightarrow_{rm} \beta$  in this case.

If  $S \xRightarrow{*}_{lm} \alpha$ , then we say that  $\alpha$  is a *left-sentential form* of the grammar at hand.

Rightmost derivations are sometimes called *canonical* derivations.

## 2.3 Parse Trees and Derivations

The leaves of a parse tree are labeled by nonterminals or terminals and, read from left to right, constitute a sentential form, called the *yield* or *frontier* of the tree.

## 2.4 Ambiguity

A grammar that produces more than one parse tree for some sentence is said to be *ambiguous*.

For most parsers, it is desirable that the grammar be made unambiguous, for if it is not, we cannot uniquely determine which parse tree to select for a sentence. In other cases, it is convenient to use carefully chosen ambiguous grammars, together with *disambiguating rules* that "throw away" undesirable parse trees, leaving only one tree for each sentence.

# 3 Writing a Grammar

## 3.1 Eliminating Ambiguity

Sometimes an ambiguous grammar can be rewritten to eliminate the ambiguity. As an example, we shall eliminate the ambiguity from the following "dangling-else" grammar:

$$\begin{array}{ll} stmt & \rightarrow \text{if } expr \text{ then } stmt \\ & | \text{if } expr \text{ then } stmt \text{ else } stmt \\ & | \text{other} \end{array} \quad (4.6)$$

Grammar (4.6) is ambiguous since the string

$$\text{if } E_1 \text{ then if } E_2 \text{ then } S_1 \text{ else } S_2 \quad (4.7)$$

has the two parse trees shown in Fig. 4.1.

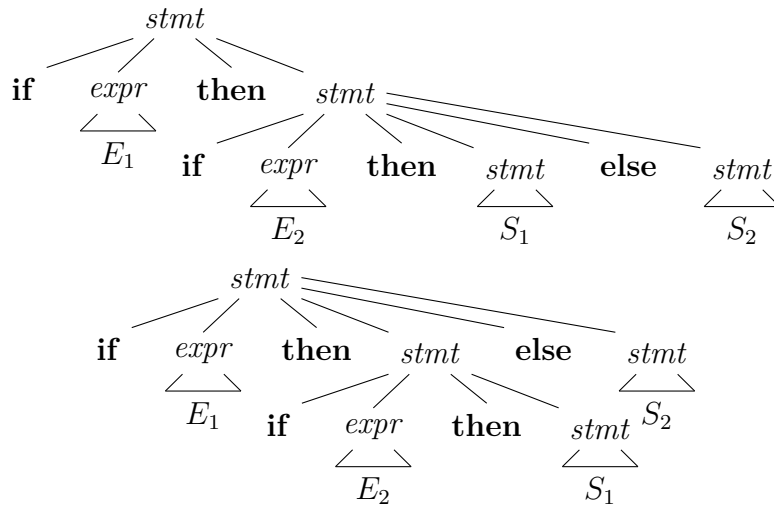


Figure 4.1: Two parse trees for an ambiguous sentence

### 3.2 Elimination of Left Recursion

A grammar is *left recursive* if it has a nonterminal  $A$  such that there is a derivation  $A \xRightarrow{+} A\alpha$  for some string  $\alpha$ .

**Algorithm:** Eliminating left recursion.

**INPUT:** Grammar  $G$  with no cycles or  $\epsilon$ -productions.

**OUTPUT:** An equivalent grammar with no left recursion.

**METHOD:** Apply the algorithm in Fig. 4.2 to  $G$ . Note that the resulting non-left-recursive grammar may have  $\epsilon$ -productions. ■

- 1) arrange the nonterminals in some order  $A_1, A_2, \dots, A_n$ .
- 2) **for** ( each  $i$  from 1 to  $n$  ) {
- 3)     **for** ( each  $j$  from 1 to  $i - 1$  ) {
- 4)         replace each production of the form  $A_i \rightarrow A_j\gamma$  by the  
             production  $A_i \rightarrow \delta_1\gamma|\delta_2\gamma|\dots|\delta_k\gamma$ , where  
              $A_j \rightarrow \delta_1|\delta_2|\dots|\delta_k$  are all current  $A_j$ -productions
- 5)     }
- 6)     eliminate the immediate left recursion among the  $A_i$ -productions
- 7) }

Figure 4.2: Algorithm to eliminate left recursion from a grammar

### 3.3 Left Factoring

**Algorithm:** Left factoring a grammar.

**INPUT:** Grammar  $G$ .

**OUTPUT:** An equivalent left-factored grammar.

**METHOD:** For each nonterminal  $A$ , find the longest prefix  $\alpha$  common to two or more of its alternatives. If  $\alpha \neq \epsilon$  – i.e., there is a nontrivial common prefix – replace all of the  $A$ -productions  $A \rightarrow \alpha\beta_1|\alpha\beta_2|\dots|\alpha\beta_n|\gamma$ , where  $\gamma$  represents all alternatives that do

not begin with  $\alpha$ , by

$$\begin{aligned} A &\rightarrow \alpha A' \mid \gamma \\ A' &\rightarrow \beta_1 \mid \beta_2 \mid \cdots \mid \beta_n \end{aligned}$$

Here  $A'$  is a new nonterminal. Repeatedly apply this transformation until no two alternatives for a nonterminal have a common prefix. ■

### 3.4 LL(1) Grammars

**Algorithm:** Construction of a predictive parsing table.

**INPUT:** Grammar  $G$ .

**OUTPUT:** Parsing table  $M$ .

**METHOD:** For each production  $A \rightarrow \alpha$  of the grammar, do the following:

1. For each terminal  $a$  in  $\text{FIRST}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, a]$ .
2. If  $\epsilon$  is in  $\text{FIRST}(\alpha)$ , then for each terminal  $b$  in  $\text{FOLLOW}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, b]$ . If  $\epsilon$  is in  $\text{FIRST}(\alpha)$  and  $\$$  is in  $\text{FOLLOW}(A)$ , add  $A \rightarrow \alpha$  to  $M[A, \$]$  as well.

If, after performing the above, there is no production at all in  $M[A, a]$ , then set  $M[A, a]$  to **error** (which we normally represent by an empty entry in the table). ■

### 3.5 Nonrecursive Predictive Parsing

The behavior of the parser can be described in terms of its *configurations*, which give the stack contents and the remaining input. The next algorithm describes how configurations are manipulated.

**Algorithm:** Table-driven predictive parsing.

**INPUT:** A string  $w$  and a parsing table  $M$  for grammar  $G$ .

**OUTPUT:** If  $w$  is in  $L(G)$ , a leftmost derivation of  $w$ ; otherwise, an error indication.

**METHOD:** Initially, the parser is in a configuration with  $w\$$  in the input buffer and the start symbol  $S$  of  $G$  on top of the stack, above  $\$$ . The program in Fig. 4.3 uses the predictive parsing table  $M$  to produce a predictive parse for the input. ■

```

set  $ip$  to point to the first symbol of  $w$ ;
set  $X$  to the top stack symbol;
while (  $X \neq \$$  ) { /* stack is not empty */
    if (  $X$  is  $a$  ) pop the stack and advance  $ip$ ;
    else if (  $X$  is a terminal )  $error()$ ;
    else if (  $M[X, a]$  is an error entry )  $error()$ ;
    else if (  $M[X, a] = X \rightarrow Y_1 Y_2 \cdots Y_k$  ) {
        output the production  $X \rightarrow Y_1 Y_2 \cdots Y_k$ ;
        pop the stack;
        push  $Y_k, Y_{k-1}, \dots, Y_1$  onto the stack, with  $Y_1$  on top;
    }
    set  $X$  to the top stack symbol;
}

```

Figure 4.3: Predictive parsing algorithm

## 4 Bottom-Up Parsing

### 4.1 Reductions

At each *reduction* step, a specific substring matching the body of a production is replaced by the nonterminal at the head of that production.

Formally, if  $S \xRightarrow{*}_{rm} \alpha Aw \xRightarrow{rm} \alpha \beta w$ , then production  $A \rightarrow \beta$  in the position following  $\alpha$  is a *handle* of  $\alpha \beta w$ .

### 4.2 Shift-Reduce Parsing

While the primary operations are shift and reduce, there are actually four possible actions a shift-reduce parser can make: (1) shift, (2) reduce, (3) accept, and (4) error.

1. *Shift*. Shift the next input symbol onto the top of the stack.
2. *Reduce*. The right end of the string to be reduced must be at the top of the stack. Locate the left end of the string within the stack and decide with what nonterminal to replace the string.
3. *Accept*. Announce successful completion of parsing.
4. *Error*. Discover a syntax error and call an error recovery routine.

### 4.3 Conflicts During Shift-Reduce Parsing

There are context-free grammars for which shift-reduce parsing cannot be used. Every shift-reduce parser for such a grammar can reach a configuration in which the parser, knowing the entire stack contents and the next input symbol, cannot decide whether to shift or to reduce (a *shift/reduce conflict*), or cannot decide which of several reductions to make (a *reduce/reduce conflict*).

## 5 Introduction to LR Parsing: Simple LR

### 5.1 Items and the LR(0) Automaton

An *LR(0) item* (*item* for short) of a grammar  $G$  is a production of  $G$  with a dot at some position of the body.

One collection of sets of LR(0) items, called the *canonical* LR(0) collection, provides the basis for constructing a deterministic finite automaton that is used to make parsing decisions. Such an automaton is called an *LR(0) automaton*.

If  $G$  is a grammar with start symbol  $S$ , then  $G'$ , the *augmented grammar* for  $G$ , is  $G$  with a new start symbol  $S'$  and production  $S' \rightarrow S$ .

### Closure of Item Sets

We divide all the sets of items of interest into two classes:

1. *Kernel items*: the initial term,  $S' \rightarrow \cdot S$ , and all items whose dots are not at the left end.
2. *Nonkernel items*: all items with their dots at the left end, except for  $S' \rightarrow \cdot S$ .

## 5.2 The LR-Parsing Algorithm

Where a shift-reduce parser would shift a symbol, an LR parser shifts a *state*.

### LR-Parser Configurations

A *configuration* of an LR parser is a pair:

$$(s_0 s_1 \cdots s_m, a_i a_{i+1} \cdots a_n \$)$$

where the first component is the stack contents (top on the right), and the second component is the remaining input.

### Behavior of the LR Parser

**Algorithm:** LR-parsing algorithm

**INPUT:** An input string  $w$  and an LR-parsing table with functions ACTION and GOTO for a grammar  $G$ .

**OUTPUT:** If  $w$  is in  $L(G)$ , the reduction steps of a bottom-up parse for  $w$ ; otherwise, an error indication.

**METHOD:** Initially, the parser has  $s_0$  on its stack, where  $s_0$  is the initial state, and  $w\$$  in the input buffer. The parser then executes the program in Fig. 4.4. ■

```

let  $a$  be the first symbol of  $w\$$ ;
while (1) { /* repeat forever */
    let  $s$  be the state on top of the stack;
    if ( ACTION[ $s, a$ ] = shift  $t$  ) {
        push  $t$  onto the stack;
        let  $a$  be the next input symbol;
    } else if ( ACTION[ $s, a$ ] = reduce  $A \rightarrow \beta$  ) {
        pop  $|\beta|$  symbols off the stack;
        let state  $t$  now be on top of the stack;
        push GOTO[ $t, A$ ] onto the stack;
        output the production  $A \rightarrow \beta$ ;
    } else if ( ACTION[ $s, a$ ] = accept ) break; /* parsing is done */
    else call error-recovery routine;
}

```

Figure 4.4: LR-parsing program

## 5.3 Constructing SLR-Parsing Tables

**Algorithm:** Constructing an SLR-parsing table.

**INPUT:** An augmented grammar  $G'$ .

**OUTPUT:** The SLR-parsing table functions ACTION and GOTO for  $G'$ .

**METHOD:**

1. Construct  $C = \{I_0, I_1, \dots, I_n\}$ , the collection of sets of LR(0) items for  $G'$ .
2. State  $i$  is constructed from  $I_i$ . The parsing actions for state  $i$  are determined as follows:
  - (a) If  $[A \rightarrow \alpha \cdot a\beta]$  is in  $I_i$  and  $\text{GOTO}(I_i, a) = I_j$ , then set  $\text{ACTION}[i, a]$  to "shift  $j$ ." Here  $a$  must be a terminal.
  - (b) If  $[A \rightarrow \alpha \cdot]$  is in  $I_i$ , then set  $\text{ACTION}[i, a]$  to "reduce  $A \rightarrow \alpha$ " for all  $a$  in  $\text{FOLLOW}(A)$ ; here  $A$  may not be  $S'$ .
  - (c) If  $[S' \rightarrow S \cdot]$  is in  $I_i$ , then set  $\text{ACTION}[i, \$]$  to "accept."

If any conflicting actions result from the above rules, we say the grammar is not SLR(1). The algorithm fails to produce a parser in this case.

3. The goto transitions for state  $i$  are constructed for all nonterminals  $A$  using the rule: If  $\text{GOTO}(I_i, A) = I_j$ , then  $\text{GOTO}[i, A] = j$ .
4. All entries not defined by rules (2) and (3) are made "error."
5. The initial state of the parser is the one constructed from the set of items containing  $[S' \rightarrow \cdot S]$ .

The parsing table consisting of the ACTION and GOTO functions determined by Algorithm 5.3 is called the *SLR(1) table for  $G$* . An LR parser using the SLR(1) table for  $G$  is called the SLR(1) parser for  $G$ , and a grammar having an SLR(1) parsing table is said to be *SLR(1)*.

## 5.4 Viable Prefixes

The prefixes of right sentential forms that can appear on the stack of a shift-reduce parser are called *viable prefixes*.

We say item  $A \rightarrow \beta_1 \cdot \beta_2$  is *valid* for a viable prefix  $\alpha\beta_1$  if there is a derivation  $S' \xRightarrow{*}_{rm} \alpha a w \Rightarrow_{rm} \alpha\beta_1\beta_2 w$ .