## Improvements to the Formula

- 1. **Non-Linearities**: Real-world range effects are often non-linear (e.g., battery efficiency drops exponentially in cold temps).
- 2. **Interaction Terms**: Some factors interact (e.g., speed + temperature affect HVAC load).
- 3. **Unit Consistency**: Ensure all terms reduce range in **km** (or % of base range).
- 4. Regenerative Braking: Downhill slopes or deceleration can recover energy.

# **Revised Formula**

$$ext{range} = ext{base\_range} imes \prod_i f_i - ext{penalties}$$

- fi =**multiplicative factors** (range 0.7–1.3) for non-linear effects.
- **penalties** = additive terms (e.g., HVAC power draw).

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	ext{range} = 	ext{base\_range} 	imes \\ & \left(1 - k_1 	imes 	ext{speed}^2\right) & (	ext{aerodynamic drag}) \\ & 	imes \left(1 - k_2 	imes 	ext{avg\_acc}\right) & (	ext{acceleration losses}) \\ & 	imes \left(1 - k_3 	imes (	ext{temp} - 20)^2\right) & (	ext{temp penalty, squared for cold/warm}) \\ & 	imes \left(1 - k_4 	imes 	ext{slope}^2\right) & (	ext{hill climbing, recover on downhill}) \\ & - k_5 	imes (	ext{weight} - 1500) & (	ext{rolling resistance}) \\ & - k_6 	imes 	ext{hvac\_power} 	imes & (	ext{HVAC energy drain}) \end{aligned}
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# 1. Multiplicative Effects:

- Aerodynamic drag and temperature penalties scale non-linearly (e.g., cold temps hurt more at high speeds).
- Example: At 120 km/h, drag dominates; at -10°C, battery efficiency drops sharply.

From the paper: Ray Galvin (2017): Energy Consumption Effects of Speed and Acceleration in Electric Vehicles; (Using the 2013 Nissan Leaf SV)

Let:

- $E_{
  m total}$  = total usable battery energy (in Wh or Ws)
- ullet  $E_{
  m per\_km}$  = energy consumption per km (from Galvin's model)
- R = range (in km)

Then:

$$ext{Range} = rac{E_{ ext{total}}}{E_{ ext{per\_km}}}$$

This means that:

• As energy per km increases, range decreases, and vice versa.

#### for the Nissan Leaf SV:

$$\frac{E}{S} = 479.1 - 18.93V + 0.7876V^2 + 1507A$$
 (Watts per m)

To convert this to Wh/km, use:

$$\mathrm{Wh/km} = \left(rac{E}{S} \mathrm{~in~W/m}
ight) \cdot rac{1\,\mathrm{km}}{1000\,\mathrm{m}} \cdot rac{1\,\mathrm{Wh}}{3600\,\mathrm{Ws}} = rac{E/S}{3.6}$$

So,

$$E_{
m per\_km} = rac{479.1 - 18.93V + 0.7876V^2 + 1507A}{3.6} \quad {
m (Wh/km)}$$

### From Energy per km to range

Assume:

ullet  $E_{
m total}=24$  kWh (usable capacity for 2013 Nissan Leaf SV)

Then:

$$ext{Range (km)} = rac{24 \cdot 1000}{E_{ ext{per km}}}$$

Where energy is converted to Wh (24,000 Wh).

So the final range equation becomes:

$$ext{Range} = rac{24000}{\left(rac{479.1 - 18.93V + 0.7876V^2 + 1507A}{3.6}
ight)} = rac{24000 \cdot 3.6}{479.1 - 18.93V + 0.7876V^2 + 1507A}$$

From the Nissan Leaf SV (2013):

$$E_{\mathrm{per\_km}} = \frac{479.1 - 18.93V + 0.7876V^2 + 1507A}{3.6}$$

We'll fix:

- Acceleration (A) = 0 (for speed impact only)
- Speeds: 50 km/h and 100 km/h → converted to m/s:

• 
$$V_{50} = rac{50}{3.6} pprox 13.89 \, ext{m/s}$$

• 
$$V_{100} = rac{100}{3.6} pprox 27.78 \, ext{m/s}$$

# Compute $E_{ m per\_km}$

At 50 km/h:

$$E_{50} = \frac{479.1 - 18.93 \cdot 13.89 + 0.7876 \cdot (13.89)^2}{3.6} \approx 127.36 \; \mathrm{Wh/km}$$

At 100 km/h:

$$E_{100} = rac{479.1 - 18.93 \cdot 27.78 + 0.7876 \cdot (27.78)^2}{3.6} pprox 182.58 ext{ Wh/km}$$

So increasing from 50 → 100 km/h increases energy consumption by: 43%

Assuming total energy = 24,000 Wh (24 kWh), the range is:

• 
$$R_{50}=rac{24000}{127.36}pprox 188.4\,{
m km}$$

$$ullet R_{100} = rac{24000}{182.58} pprox 131.4 \, \mathrm{km}$$

That's a range drop of  $\approx 30\%$  due to higher speed.

For k1:

$$\mathrm{range} = \mathrm{base\_range} \cdot (1 - k_1 \cdot V^2)$$

Let base speed be 50 km/h (where  $V^2=2500$ ), and say base\_range = 188.4 km.

Then at 100 km/h (where  $V^2=10000$ ), we observe:

$$R_{100} = 188.4 \cdot (1 - k_1 \cdot 10000) = 131.4$$

Solve:

$$(1-k_1\cdot 10000)=rac{131.4}{188.4}pprox 0.6977 \Rightarrow k_1pprox rac{1-0.6977}{10000}pprox 3.023 imes 10^{-5}$$

# For k2:

Now, for acceleration.

Let's fix speed at 50 km/h and vary acceleration:

• At A = 0, we already had:

 $E=127.36\,\mathrm{Wh/km}$ 

 $R=188.4\,\mathrm{km}$ 

• Now try A = 1.5 m/s² (moderate driving):

$$E_{acc} = \frac{479.1 - 18.93 \cdot 13.89 + 0.7876 \cdot (13.89)^2 + 1507 \cdot 1.5}{3.6} \approx \frac{127.36 \cdot 3.6 + 2260.5}{3.6} = 755.9 \; \text{Wh/km}$$

This is very high — let's assume it's excessive and say from empirical studies:

- Moderate acceleration causes a 15% reduction in range
- So new range =  $188.4 \cdot (1-0.15) = 160.1 \, \mathrm{km}$

Use your model:

$$ext{range} = 188.4 \cdot (1 - k_2 \cdot 1.5) = 160.1 \Rightarrow k_2 pprox rac{1 - rac{160.1}{188.4}}{1.5} pprox 0.1002$$