Lab II: Sets (Due on Check on Léa)

A set is a collection of distinct elements.

$$\{2,3,5,7\}$$
 $\{\text{'a','b','c'}\}$ $\{\text{"aardvark","aardwolf","albatross"}\}$

We will create a set data structure, but restrict ourselves to only sets whose elements can be ordered.

1 Sets

The sets you will represent here are similar to the sets you have studied in mathematics, but with one important difference: the set contains only elements of one type (ex: Integer), String, etc...).

1.1 Operations

Contains. The fundamental operation *contains* (a.k.a.: member, usually denoted by \in) on a set is to tell if an element is contained within it:

$$a \in \{a, b, c\}$$
 $c \notin \{a, b\}$

Contains all. Determine if every element of a set A is also in a second set B, that is, A is entirely in B (a.k.a. subset). This is usually written as $A \subseteq B$. For example:

$$\{a,c\} \subseteq \{a,b,c,d\}$$
 $\{b,d\} \not\subseteq \{a,b,c\}$

A more formal definition of subset is: for all x, if $x \in A$ then $x \in B$.

Add. Sorted sets are built using an operation for adding an element to an existing set. If we have a set $\{a,b\}$, then $\mathbf{add}(c)$ would yield $\{a,b,c\}$. Add should behave like the traditional set *union* operation \cup , in that adding a duplicate to a set would leave the set unchanged. Ex:

$$\{a, b, c\} \cup \{a\} = \{a, b, c\}$$

Remove. An element can be removed from a sorted set using the remove operation. If we have a set $\{a,b,c\}$, then $\mathbf{remove}(c)$ would yield $\{a,b\}$. Remove should be have like the traditional set *difference* operation —, in that removing an element not in the original set results in the set unchanged. Ex:

$${a,b,c} - {d} = {a,b,c}$$

Size. Number of elements of the set (a.k.a. cardinality). This is usually written as |A|.

Empty/Full. Determine if the set is empty $(\{\})$ or full. A set is full if there is insufficient space to store additional elements.

To String. Operations to get a string representation of a set (see API).

1.2 Set API

This specification uses a type parameter T.

Signature	boolean contains(T element)
Description	Determine if the set contains a specific element.
Pre-conditions	None.
Post-conditions	If the element is found in the set that equals element, then returns true, other-
	wise, the method returns false.

Signature	boolean containsAll(Set <t> rhs)</t>
Description	Determine if the set contains all the elements of the provided set, or, that the
	provided set is a subset of the current set.
Pre-conditions	None.
Post-conditions	Returns true if all the elements of rhs are in the current set, false otherwise. If
	the provided set is empty, return true.

Signature	boolean add(T element)
Description	Add an element into the set.
Pre-conditions	The set is not full.
Post-conditions	If there is no element in the set that equals element, then the element is inserted
	into the set, otherwise the set is unchanged. The method returns <code>true</code> if the ele-
	ment is added to the set, and false otherwise.

Signature	boolean remove(T element)
Description	Remove an element from the set.
Pre-conditions	None.
Post-conditions	If there is an element in the set equal to element, then it is removed from the
	set. Otherwise, the set is unchanged. The method returns <code>true</code> if the element is
	added to the set, and false otherwise.

Signature	int size()
Description	Determine the number of elements in the set.
Pre-conditions	None.
Post-conditions	Returns the number of elements in the set.

Signature	boolean isEmpty()
Description	Determine if the set is empty.
Pre-conditions	None.
Post-conditions	Returns true if the set is empty, false otherwise.

Signature	boolean isFull()
Description	Determines if the set is full.
Pre-conditions	None.
Post-conditions	Returns true if the set is full, false otherwise.

Signature	String toString()
Description	Get a (String) representation of the set.
Pre-conditions	None.
Post-conditions	Returns a (String) representation of the set, consisting of:
	• a {,
	• the String representations of the elements, comma-separated, and
	• a }.

2 Sorted Sets

A *sorted* set is a set that has a further restriction: the elements can be ordered, meaning that there must be operations <, >, =, etc...defined for any type used in a sorted set.

2.1 Operations

Minimum/Maximum. Since the elements of a set are ordered, it is possible to determine the smallest and largest element in the set.

Subset. Produce a subset of the current set containing all the elements between a lower bound (inclusive) and an upper bound (exclusive). For example, the **subset**(2,4) of the set $\{1,2,3,4,5\}$ is $\{2,3\}$.

2.2 Sorted Set API

Signature	T min()
Description	Retrieve the smallest element in the set.
Pre-conditions	The sorted set is not empty.
Post-conditions	Returns the smallest element in the set. The set is unchanged.

Signature	T max()
Description	Retrieve the largest element in the set.
Pre-conditions	The sorted set is not empty.
Post-conditions	Returns the largest element in the set. The set is unchanged.

Signature	SortedSet <t> subset(T low, T high)</t>
Description	Produce a subset of the current set containing all the elements between low (in-
	clusive) and high (exclusive)
Pre-conditions	The low must be less than or equal to high.
Post-conditions	Returns the subset.

3 Traversable Abstract Data Type and API

A traversal is a sequence of steps visiting each element in the data type.

Traversal. A *traversal* is a series of operations that enable a visiting of each of the elements in the collection. For example the traversal of $\{1, 2, 3\}$ will be:

$$1 \longrightarrow 2 \longrightarrow 3$$

The traversal operation is broken down into 3 sub-operations: **reset**, **hasNext** and **next**. Resetting restarts the traversal, say after a previous traversal. Next gives the next element in the traversal and **hasNext** indicates the end.

3.1 Traversable API

Traversals are used to "loop" over the data type. For example, if data is a traversable collection of integers, then we can write the following:

```
data.reset();
while(data.hasNext()) {
   int x = data.next();
   // code to run for each element
}
```

Signature	void reset()
Description	Initialize a traversal.
Pre-conditions	
Post-conditions	If there are elements, the traversal cursor is positioned on the first element. Oth-
	erwise, the traversal is complete (trivially).

Signature	boolean hasNext()
Description	Determine if a traversal can continue.
Pre-conditions	The traversal has been initialized and no modifications (ex: add or remove operations) have been performed since the initialization.
Post-conditions	Returns true is there are elements left in the traversal, false otherwise.

Signature	T next()
Description	Return the current element in the traversal, and then advance the traversal cur-
	sor to the next element.
Pre-conditions	The traversal has been initialized and no modifications (add or remove opera-
	tions) have been performed since the initialization. The traversal still has at least
	one element left.
Post-conditions	If there is a next element, the traversal cursor has advanced to it and it is returned.
	At the end of the traversal cursor is <i>undefined</i> , meaning that is no longer refers to
	an element.

4 Sorted Set Data Structure

Implement the above APIs as a SortedSet data structure. Your implementation must use an array to store the elements and keep them is a sorted order. The Set and Traversable APIs are included as Java interfaces to be implemented by your data structure.

The implementation will be a generic class, i.e.: <u>SortedSet<T></u>. In order to sort the set elements, we must put an constraint on the type arguments that can be supplied for T. We will allow only classes that implement the method compareTo(), by declaring the class as follows:

```
public class SortedSet<T extends Comparable<T>> implements \dots { \dots }
```

Start from the supplied Java file, SortedSet.java, which contains the declaration of the (SortedSet<T>) class, as well as the constructor and an implementation of contains(). You may add/remove private members of the class, but the public methods should remain the same.

5 Unit Testing

Instead of testing your data structure using a main() method, use JUnit test cases to verify your implementation. Appendix A has a list of tests provided in the starter that your class should pass.

6 Efficiency

For each (Set) and (SortedSet) API method, use the fact that the elements are be stored in sorted order to optimize the efficiency of your code. Hint: many methods can benefit from binary search, for example the contains() can use binary search instead of linear search.

7 Requirements

Your program *must* meet the following requirements:

- 1. Your program should be clear and well commented. It must follow the "420-406 Style Guidelines" (on Léa).
- 2. The SortedSet<T> class implements the API methods from Sections 1, 2 and 3.
- 3. The set elements must be stored in an array in sorted order (either ascending or descending). Do not use a list to store the data.
- 4. Use the fact that the elements can be stored in sorted order to optimize the efficiency of your code (Section 6).
- 5. Do not do a complete sort of the array of elements. For example, no sorting using Arrays.sort(..). Storing the elements in a list, even temporarily is prohibited, since it is likely less efficient than working with the array directly.
- 6. Your data structure should pass all tests in the (SortedSetTest) class.
- 7. Submit using Git by following the instructions (on Léa).

A Appendix: Provided JUnit test cases

Set API Tests.

Test Name	Test Description
testConstructorMakesEmptySet()	The set is initialized to the empty set.
testContains()	The operation contains works for the set.
testContainsAll()	Test that the containsAll operation works.
testAdd()	The operation add works for the set.
testNoDuplicates()	Adding a duplicate elements to the set does not modify the set.
testFullSet()	The operation isFull works for the set.
testFullSetException()	Adding to a full set will cause an error.
testRemove()	The operation remove works for the set.
testRemoveNonElement()	The operation remove fails to remove a non-element of the set.
testEmptySet()	The operation isEmpty works for the set.
testRemoveOnEmptySet()	Removing from the empty set fails, but does not cause an error.
testToString()	Converting the set into its String representation gives expected results.

Sorted Set API Tests.

	50100 50111 1 1050			
Test Name	Test Description			
testMin()	The operation min returns the minimum element in the set.			
testMax()	The operation min returns the minimum element in the set.			
testMinMaxInSingletonSet()	In a set with one element, the minimum and the maximum are the same.			
testMinOnEmptySet()	Calling min on an empty set gives an error.			
testMaxOnEmptySet()	Calling max on an empty set gives an error.			
testSubset()	Test that the subset method generates proper subsets.			
testSubsetOnEmptySet()	Test that the subset operation on an empty set returns an empty set			
testSubsetIllegalArguments()	Test that when subset is called with low > high an error is thrown.			

Traversal API Tests.

Test Name	Test Description
testTraversal()	Test that a traversal visits each element in the set in turn.
testTraversalWithoutError()	Test that a proper traversal does not cause an error.
<pre>testTraversalEmptySet()</pre>	Test that an empty set has no elements in its traversal.
testAddDuringTraversal()	Test that adding during a traversal causes an error.
<pre>testNextOnCompletedTraversal()</pre>	Test that asking for more elements at the end of the traversal causes an error.