



Worksheet

Course Name:

DIGITAL LOGIC DESIGN

Topic:

MINIMALISATION TECHNIQUE

Minimisation is the calculated process of breaking down or simplifying boolean expressions into simpler terms.

Laws such as annulment law, identity law, idempotent law, associative law, distributive law, and complement law will help to simplify these expressions to a minimum number of terms.

STEPS TO ACCURATE SIMPLIFICATION

- 1 Look for similar terms
- 2 Apply Boolean algebra rules
- 3 Ensure that the simplified expression is logically equivalent to the original expression by comparing their truth tables or applying boolean algebra rules.
- 4 Applying one simplification at a time to avoid complexities during simplification.

EXAMPLES

Simplify this expression

$$AB + BC(B+C)$$

$AB + BC.B + BC.C$ (Applying distributive law)

$$AB + BBC + BCC$$

Remember $B.B = B$ and $C.C = C$ using the idempotent law.

Simplifying, we have

$$AB + BC + BC$$

$$BC + BC = BC \text{ (Applying idempotent law)}$$

$$\text{FINAL RESULT} \\ = B(A+C)$$

EXAMPLES

Simplify the boolean expression below.

$$AB = A(B+C) + B(B+C)$$

Use distributive law to expand the terms in the bracket.

We have

$$AB + AB + AC + BB + BC$$

$$B.B = B \text{ (using idempotent law).}$$

$$AB + AB + AC + B + BC$$

$$B + BC = B \quad \text{(using absorption law)}$$

$$AB + AB + AC + B$$

Gather like terms

$$AB + AB + B + AC$$

$$AB + AB = AB \text{ (using idempotent law)}$$

We have

$$AB + B + AC$$

$$AB + B = B \text{ (Using absorption law)}$$

FINAL RESULT
B + AC

EXAMPLES

Simplify this expression

$$AB + BC(B+C)$$

$$AB' + A(B+C) + B(B+C) \quad (\text{Applying distributive law})$$

$$AB' + AB + AC + BB + BC$$

$$B.B = B \quad (\text{Using idempotent law})$$

$$B + BC = B \quad (\text{Using absorption law})$$

$$AB' + AB + B + AC$$

(Gather like terms)

$$AB' + B + AB + AC$$

$$B + BC = B \quad (\text{Using absorption law})$$

$$\text{FINAL RESULT} \\ AB' + B + AC$$

QUIZ 1

CHECK YOUR PROGRESS

Simplify the expression

$$X + Z(X + XZ') + XY + Y$$

HINT!

Compare original expression and your final result using truth tables. If they give same output then you are correct

QUIZ 2

Simplify this expression

$$XY' + X' + Y'X'$$