

Module - 4

Anomaly

- Db anomaly v normally the flow in db which occurs because of poor planning and storing everything in a flat db.
- Generally this is removed by the process of normalization which performed by splitting joining of table
- Type of Anomalies
 - 1) Insert
 - 2) Delete
 - 3) Update.

Insert Anomaly

- An insert Anomaly occurs when certain attributes cannot be inserted into the db without the presence of other attribute

(cannot be added one attribute being absent of other attribute)

- If a tuple is inserted in referencing relation & referencing attribute values not present in referenced attribute, it will not allow inserting in referencing relation.

StudentID	Error no	Roll no	Name	Address	City	Dept ID
1	Rx001	1-BSCS-218	John	House 1	Lahore	3
2	Rx002	2 " "	Faiz	house 2	Karachi	4
3.	Rx003	3 " "	Nonnumm	house 3	Faisalabad	5
4	Rx004	4 " "	Jerry	house 29	M&B	6.

Dept ID	Name	Phone Extension
3	CS	398974
4	Botany	988784
5	English	898418

Jerry is a

There is no
Hence, the
should be
only then

Delete anomaly

- It happens
information
be deleted
- So to say
comes deletion
anomaly.

StudentID
2
3
4.

Jerry is a new student with department 6

There is no department with this dept id 6.
Hence, the anomaly. The usual behavior
should be new department id with 6 and
only then student could have it.

Delete anomaly

- It happens when the deletion of unwanted information causes desired information to be deleted as well.
- So to say deletion of some attribute which causes deletion of other attributes is deletion anomaly.

Student Id	Enroll No	Roll No	Name	Dept ID
2	Ax002	2 -	Faiz	4
3	" 3	3	Mominam	5
4	" 4	4	Jerry	6.

dep id	name	phone
4	Botany	988-184
8	English	898418

- Now if some one decides to delete CS department, he may end up deleting all student's data who had the department of CS.

Update anomaly

- This occurs in case of data redundancy and partial update.
- When duplicated data is updated at one instance and not across all instances where it was duplicated. That's an update anomaly.
- See below English department has now dept 108, but unfortunate

Unfortunately it was not updated in student

table.

Functional dependency

Consider the schema: Following Schema stores current student data in college hostels. (college has more than 1 hostel buildings)

Student - Hostel					
adm no	student name	sex	dept	hostel name	room no

- Since adm no is a key

adm no \longrightarrow { student name, sex, dept, hostel name, room no }

adm no \longrightarrow student name

adm no \longrightarrow sex

adm no \longrightarrow dept

adm no \longrightarrow hostel name

adm no \longrightarrow room no.

Student - Hostel

admno	Student name	Sex	dept	hostelname	roomno
A2003	Arun	m	CS	nila	101
A2033	Remya	F	EC	Yamuna	101
A2019	Sonmya	F	CS	Gangga	102
A2025	Aneesh	m	CE	nila	102
A2044	Rakesh	m	CE	Yamuna	102

→ hostel no , room no → adm no .

- FDs are additional constraints that can be specified by designers.

→ Functional dependency is trivial

$$X \rightarrow Y$$

$$\& Y \subseteq X$$

$$\text{eg} - A \rightarrow A$$

$$\text{SSN , PNO} \rightarrow \text{P number}$$

$$\text{hostel name , room no} \rightarrow \text{room no}$$

- The set of all dependencies that can be referred from the set of given functional dependencies, say F^* is called closure of F , (F^*)
- These FDS can be deduced using some inference rules.

Rule 1: Reflexivity

"A, B, C are set of 1 or more attributes"

IF B is subset of A
 A determines B .

$$A \rightarrow B$$

eg. Last name \subseteq Firstname, Last name

Firstname, Last name \rightarrow Lastname

Rule 2 : Augmentation

IF $A \rightarrow B$ and C is a set of attributes,
then AC determines BC

$$\{AC \rightarrow BC\}$$

Eg :

Roll

Re

Ro

Rule 3

IF

2

Rule 3 : Transitivity

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Ex: If $A \rightarrow B$ & $B \rightarrow C$ then $A \rightarrow C$

is also true.

Eg.

Roll no. \rightarrow address & Adm.

address \rightarrow Pincode

Roll no \rightarrow Pincode.

Rule 6

IF

Rule 4: Union

IF $\{A \rightarrow B\}$ & $\{A \rightarrow C\}$ hold

$A \rightarrow BC$ true.

Rule 7

gives

Eg :-

Roll no \rightarrow name

Roll no \rightarrow address

Roll no \rightarrow , name & address.

Rule 5 : composition

IF $\{ A \rightarrow B \}$ $\{ A \times C \rightarrow B \times C \}$ is
 $\{ X \rightarrow Y \}$ true.

Roll no \rightarrow name

Adm no \rightarrow address

Roll no, adm no \rightarrow

name, address

Rule 6 : Decomposition

IF $A \rightarrow BC$ then

$A \rightarrow B$

$A \rightarrow C$ is true.

Rule 7 : Pseudo transitivity

given $A \rightarrow B$

$BC \rightarrow D$

$\{ A \rightarrow C \rightarrow D \}$

Eg:

Roll no \rightarrow Name.

Name \rightarrow Roll no.

Name, marks \rightarrow Percentage

Rollno, marks \rightarrow percentage.

ii) Armstrong's Axioms

- This shows

Armstrong's Axioms as a inference
rules like

Reflexivity

Augmentation

Transitivity

? Consider relation $R = \{P_1, Q, R_{CD}, T, U\}$

having set of functional dependencies
(FD).

$\{P \rightarrow Q, P \rightarrow R, QR \rightarrow S, Q \rightarrow T$
 $QR \rightarrow U, PR \rightarrow V\}$

Show Using inference rules that the
 Following dependencies can be inferred
 From the above set.

$$1) P \rightarrow T$$

$$2) PR \rightarrow SU$$

$$3) QR \rightarrow SU$$

$$4) PR \rightarrow SU$$

$$- P \rightarrow T$$

Given $P \rightarrow Q$
 $Q \rightarrow T$.

$P \rightarrow T$ (1, 2, Transitivity rule)

Hence proved

(Ans)

$T \rightarrow P, Q, R$, $P \rightarrow Q, R$

$\rightarrow PR \rightarrow S$ Given

$\text{Qo} \rightarrow PR, P \rightarrow Q \rightarrow R$

$PR \rightarrow S$

benefit of using ~~inferred~~ ~~inferred~~ work
of ~~inferred~~ ~~inferred~~ ~~inferred~~ ~~inferred~~ ~~inferred~~
 $PR \rightarrow S$ (pseudo
transitivity)

Hence proved ~~inferred~~

$P \rightarrow Q$

$\rightarrow PR \rightarrow SU$ Given

$P \rightarrow Q$

$QR \rightarrow S$

$PR \rightarrow S$ (pseudo transitivity)

$PR \rightarrow U$

$\text{P} \rightarrow Q$
 $PR \rightarrow SU$ (union rule)

$P \rightarrow Q$

$\rightarrow QR \rightarrow SU$

(~~inferred~~) Given

$QR \rightarrow S$

$QR \rightarrow U$

$QR \rightarrow SU$ (union rule)

Normalization

The process of organizing the data in db to avoid the redundancy and anomalies.

Normal Forms (rules)

1NF

2NF

3NF

BCNF

1NF

Relation should not contain any multivalued

Attribute

product

ProductID	Color	Price
1	red, green	20
2	yellow	25
3	green	10
4	red, blue	25

INF =>

db in web app

Product id	color	price
1	red	20
1	green	20
2	yellow	25
3	green	10
4	red	10
4	blue	25

↓

Product id	color 1	color 2	price
1	red	green	20
2	yellow	null	25
3	green	null	10
4	red	blue	25

1NF Decompose

productID	color

productID	price

2NF

Relation R is in 2nd normal form

- R should be in 1NF
- R should not contain any partial functional dependency.

Eg: R(A B C D)

$F_D : (A \rightarrow B, C \rightarrow D)$

L.H.S candidate key (BD) (AC)

$A C^+ = A C B D$

~~L.H.S~~ prime attribute = AC (candidate key)

non prime attribute = BD.

Functional dependency

$$A \rightarrow B$$

$$C \rightarrow D$$

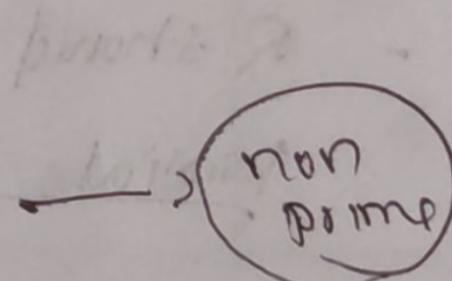
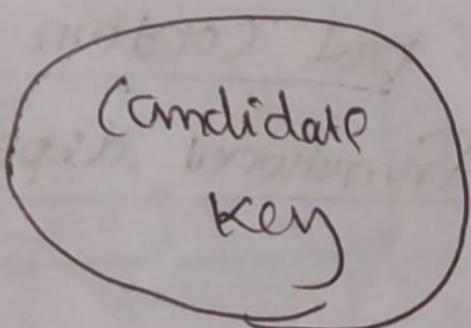
$$A \rightarrow B$$

Candidate
key part

non prime

partial functional
dependency

\Leftrightarrow not 2NF



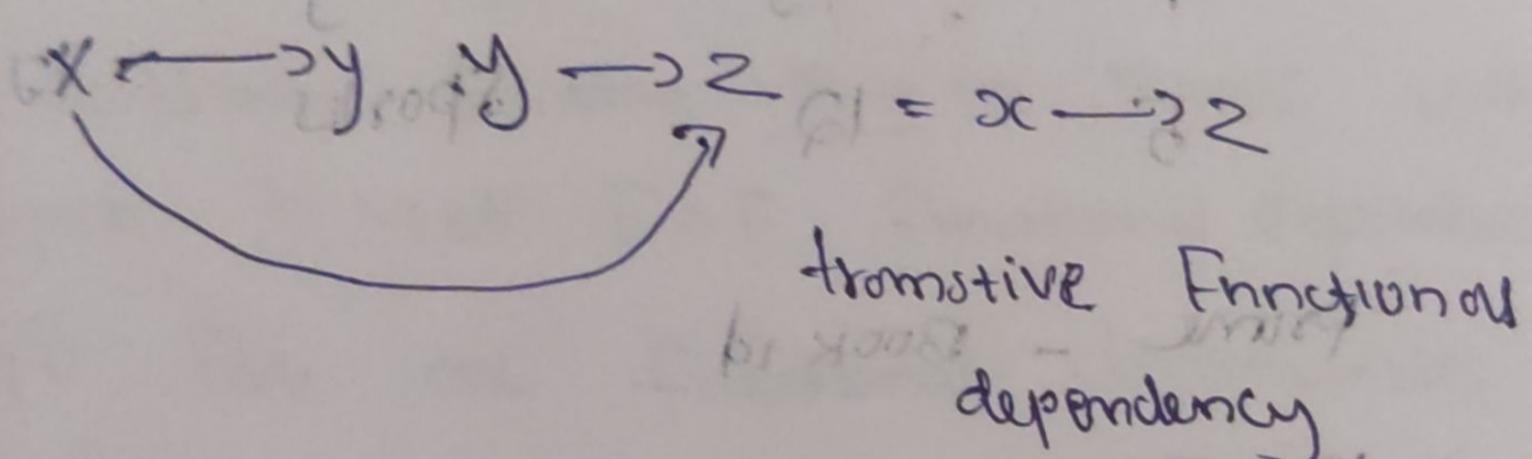
\Rightarrow partial
functional
dependency

3NF

3NF

A table U is in 3NF IF it satisfy the following conditions

- It is in second normal form.
- There is no transitive functional dependency.



- X is a candidate key or prime key \Rightarrow not correct

$$X \rightarrow Y$$

Candidate Key
Super Key

or Prime

Eg : Books

Book ID	General ID	General Type	Price
1	11	Physics	25
2	12	Sports	14
3	11	Physics	10
4	13	Botany	12
5	12	Sports	15

prime - Book id

non prime - general ID

general type

price

Functional dependency

Book ID \rightarrow General ID

General ID \rightarrow General Type

prime

Book ID \rightarrow General ID (Satisfying)

General ID \rightarrow General Type \Rightarrow non satisfying

↓
decomposition

Book 1		
Book ID	general ID	price
1001	1001	1001

Book 2.

elements	general type
1001	1001

functionally
BCNF

1001	1001
1001	1001

A relational Schema R in BCNF with respect to a set F of functional dependency

If for all functional dependencies that are in the form of $\alpha \rightarrow B$ where,

$\alpha, B \subseteq R$ at least one of the following holds true.

- $\alpha \rightarrow B$ is a trivial functional dependency

($\alpha \rightarrow \alpha$)

- α is the superkey for all the schema R .

($\alpha \rightarrow \alpha$)

R

α	B
1001	1001

Functional dependencies

trivial $B \subseteq \alpha$

non-trivial $\alpha \rightarrow \beta$

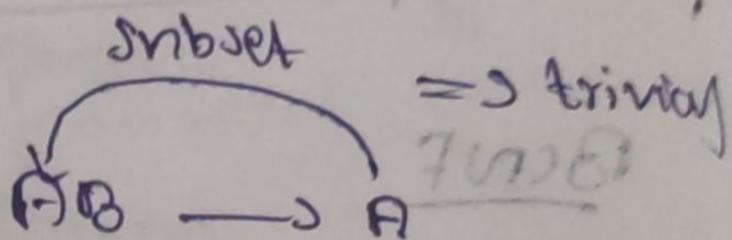
β is not subset
of α .

student no.	course id
70001	CS1001

student no.	course id
70002	CS1002

Eg

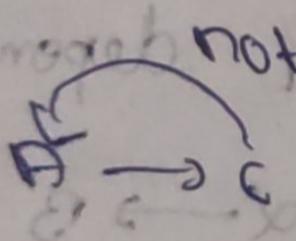
A	B	C
1	1	1
1	1	0



AB is subset of A \Rightarrow trivial

AB is not subset of B \Rightarrow non-trivial

$AB \rightarrow AB$ } trivial



$AB \rightarrow AC$ } not trivial

AB is not subset of AC \Rightarrow not trivial

→ A relation is in BCNF if every

determinant is a candidate key

candidate key is a determinant

$A \rightarrow B$

No. of mappings \downarrow with A determinant

dependent

(candidate key)

? Eg: - S1
S2

Student - no

Instructor.

1NF

Student

Student

Instr

2NF

1NF
partial
dependent
(candidate key)

com

com

Eg.: Student - Grade Report

Student no	name	major	course no	course name
------------	------	-------	-----------	-------------

instructor no	instructor name	instructor locat	grade
---------------	-----------------	------------------	-------

1NF

student no	student name	major
------------	--------------	-------

student no	course no	course name	instructor no
------------	-----------	-------------	---------------

instructor name	instructor location	grade
-----------------	---------------------	-------

2NF

student

student no	student name	major
------------	--------------	-------

course grade

student no	course no	grade
------------	-----------	-------

course instructor

course no	course name	instructor no	instructor name
-----------	-------------	---------------	-----------------

instructor location

name

3NF \rightarrow first formative
 $x \rightarrow y \rightarrow z$
 $y \rightarrow z \Rightarrow x \rightarrow z$

student student report award

Student

student no	name	major
------------	------	-------

course grade

student no	course no	grade
100001	10101	A

course

course no	course name	instructor no
10101	DBMS	100001

instructor

instructor no	instructor name	instructor location
100001	John Smith	New York

row

row	row value	row value
1	100001	10101

table

table	table value	table value
student	100001	10101

Dependency Preserving decomposition

- If we decompose a relation R into other relations R_1 and R_2 ,
relations R_1 and R_2 must be a part of R .
- All dependences of R either
 - must be a part of R_1 and R_2
 - or must be derivable from combination of FD's of R_1 and R_2 .

Ex:

Relation $R (A B C D)$

FD's $A \rightarrow B$, $A \rightarrow C$, $A \rightarrow D$
decomposed into $R_1 (ABC)$ and $R_2 (AD)$

This is dependency preserving decomposition

① $A \rightarrow B$ and $A \rightarrow C$ one a point

and form a part of $R_1 (ABC)$ and

② $A \rightarrow D$ v part of $R_2 (AD)$

(A) + (B) = (A) + (C) + (D)

Lossless join

If we decompose a relation R into Relations R_1 and R_2

- Decomposition is lossless iff.

$R_1 \Delta R_2 \subseteq R$

\downarrow
(Natural join)

- Decomposition is lossy iff

$R_1 \Delta R_2 \supset R$.

To check for lossless join decomposition

Using FDs following conditions must hold

① Union of attributes of R_1 and R_2 must be equal to attribute R .

Each attribute of R must be either

common in R_1 or in R_2

$$\text{Att}(R) \cup \text{Att}(R_2) = \text{Att}(R)$$

② Intersection of attributes of R_1 and R_2
must not be null

$$\text{Att}(R_1) \cap \text{Att}(R_2) \neq \emptyset$$

③ common attribute must be a key for at
least one relation (R_1 or R_2)

$$\checkmark \text{Att}(R_1) \cap \text{Att}(R_2) \longrightarrow \text{Att}(R_1)$$

$$\checkmark \text{Att}(R_1) \cap \text{Att}(R_2) \longrightarrow \text{Att}(R_2)$$

Eg:

A relation $R(A, B, C, D)$ with FD set

$\{A \rightarrow BC, A \rightarrow D\}$ is decomposed into

$R_1(ABC)$ and $R_2(AD)$

① First condition holds true as

$$\begin{aligned} \text{Att}(R_1) \cup \text{Att}(R_2) &= (\text{ABC}) \cup (\text{AD}) \\ &= (\text{ABCD}) = \text{Att}(R) \end{aligned}$$

② second condition holds true.

$$\text{Att}(R_1) \cap \text{Att}(R_2) = (\text{ABC}) \cap (\text{AD}) = A \neq \emptyset$$

- Third condition

$AH(R_1) \cap AH(R_2) = D$ is key

$R_1(AB)$, $R_2(AD)$ is given

and key of $R_2(AD)$ is D .

Eg: 1 $\{A, B, C\} \rightarrow \{C, D, E\}$

let $R = ABCDE$

$R_1 = AD$, $R_2 = AB$, $R_3 = BE$, $R_4 = CD$

and $R_5 = AC$

Let the Functional dependencies

$A \rightarrow C$

$B \rightarrow C$

$C \rightarrow D$

$DE \rightarrow C$

$CE \rightarrow B$

Apply Standard algorithm to test

IF the decomposition of R into

$\{R_1, \dots, R_5\}$ is lossless join

decomposition or not.

$$R = ABCD, R_1 = AD, R_2 = AB, R_3 = BE$$

$$R_4 = CDE \text{ and } R_5 = AE$$

$$\{A \rightarrow C, B \rightarrow C, C \rightarrow D, DE \rightarrow C, CE \rightarrow A\}$$

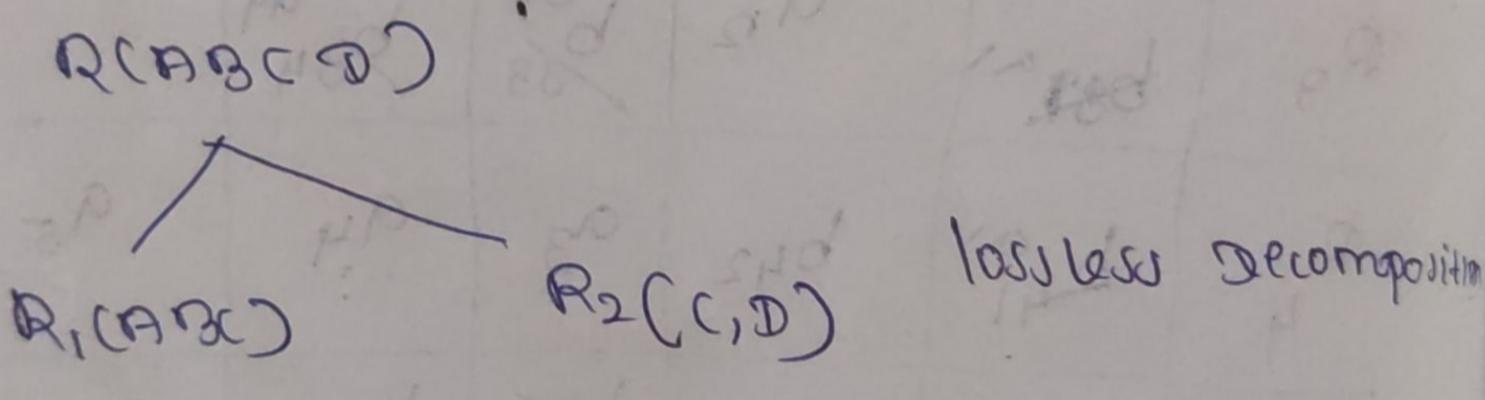
	A(1)	B(2)	C(3)	D(4)	E(5)
R_1	a_1	b_{12}	b_{13}	a_4	b_{15}
R_2	a_1	a_2	$\cancel{b_{23}}$	$b_{24} a_4$	b_{25}
R_3	$\cancel{b_{32} a_1}$	a_{12}	$\cancel{b_{33}}$	$b_{34} a_4$	a_5
R_4	$b_{41} a_1$	b_{42}	a_3	a_4	a_5
R_5	a_1	b_{52}	$\cancel{b_{53}} \\ b_{13}$	b_{54}	a_5

Unknown
value
b

Ansatz $R_3 = a_1 a_2 a_3 a_4 \rightarrow \text{lossless point}$

Decomposition in DBMS removes redundancy, anomalies and inconsistencies from a database by dividing the table into multiple tables.

- There are mainly two types.
 - lossless decomposition
 - lossy decomposition. (Not good)



Eg: given $R(ABCD)$

fd $\{AB \rightarrow CD, D \rightarrow BC\}$ is decomposed

to $R_1(AC)$ & $R_2(BCD)$ check

whether it is lossless join or not

n) Given $R(A, B, C, D, E)$
 Decomposed to $R_1(A, B, C)$, $R_2(C, D)$, $R_3(C, D, E)$

$f_D = \{AB \rightarrow CD, A \rightarrow DE, C \rightarrow D\}$?

① initial value
 $S_{ij} =$

	A	B	C	D	E		C_{bij}
R_1	b_{11} a_1	b_{12} a_2	b_{13} a_3	b_{14} a_4 ^{act on row 1}		b_{15}	
R_2	b_{21}	b_{22} a_2	b_{23} a_3	b_{24} a_4		b_{25}	
R_3	b_{31}	b_{32}	b_{33} a_3	b_{34} a_4		b_{35} a_5	

① $F_2 : \{AB \rightarrow CD\} \Rightarrow$ left side is not side.

$\{A \rightarrow E\} \Rightarrow$ not take any action.

$\{C \rightarrow D\} \Rightarrow$ some value a_3
 D value change
 a_4

Now look for any row with all a value.

Here there is no such row so we can't continue. This is a lossy join.