

ASSIGNMENT - 4Simple Linear Regression

Sample(i)	x_i^a	y_i^a
1	7.6	157
2	7.1	174

Step-1: Read dataset $\eta=0.1$, epochs=1, $m=1$, $c=-1$

Step-2: Set iteration = 1

Step-3: Set Sample $i=1$

Step-4: $y = mx + c$

$$= 1(7.6) - 1$$

$$= 6.6$$

Step-5: $E = \frac{1}{2} (y_i^a - mx_i^a - c)^2$

$$= \frac{1}{2} [157 - 1(7.6) - (-1)]^2$$

$$= \frac{22620.16}{2} \Rightarrow 11310.08$$

Step-6: $\frac{\partial E}{\partial m} = -(y_i^a - mx_i^a - c)x_i^a$

$$= -[157 - 6.6]7.6 \Rightarrow -1143.04$$

$$\frac{\partial E}{\partial c} = -(y_i^a - mx_i^a - c)$$

$$= -[157 - 6.6] \Rightarrow -150.4$$

Step-7: $\Delta m = -\eta \frac{\partial E}{\partial m}$

$$= - (0.1) (-1143.04)$$

$$= 114.304$$

$$\Delta c = -\eta \frac{\partial E}{\partial c}$$

$$= - (0.1) (-150.4)$$

$$= 15.04$$

Step-8: $m = m + \Delta m$

$$= 1 + 114.304 = 115.304$$

$$c = c + \Delta c$$

$$= -1 + 15.04 = 14.04$$

Step-9: Sample $i = i + 1 = 2$ & $i \leq n$ $T \rightarrow$ Step (4)

\rightarrow Step-4:

$$y = (115.304) 7.1 + 14.04$$

$$= 832.69$$

Step-5:

$$E = \frac{1}{2} (174 - 832.69)^2$$

$$= \frac{433872.5}{2}$$

$$\Rightarrow 216936.25$$

Step-6:

$$\frac{\partial E}{\partial m} = - [174 - (115.304) 7.1 - 14.04] 7.1$$

$$= - [174 - 832.69] (7.1)$$

$$= (658.69) 7.1 \Rightarrow 4676.69$$

$$\frac{\partial E}{\partial c} = -(174 - 832.69) = 658.69$$

$$\begin{aligned}\text{Step-7: } \Delta m &= -\eta \frac{\partial E}{\partial m} \\ &= -(0.1)(4676.69) \\ &= -467.669\end{aligned}$$

$$\begin{aligned}\Delta c &= -\eta \frac{\partial E}{\partial c} \\ &= -(0.1)(658.69) \\ &= -65.869\end{aligned}$$

$$\begin{aligned}\text{Step-8: } m &= 115.304 + (-467.669) \\ &= -352.36 \\ c &= 14.04 + (-65.869) \\ &= -51.829\end{aligned}$$

$$\text{Step-9: Sample } i = i+1 = 2+1=3 \quad \begin{matrix} i \leq n_s & \rightarrow & \text{next} \\ 3 & 2 & \text{step} \end{matrix}$$

$$\text{Step-10: } \text{iter} = \text{iter}+1 = 1+1=2, \quad \text{iter} > \text{epochs} \quad \rightarrow \text{next step}$$

Step-11: Stop.