

## 1. Adjacent numbers

### Description

Given a  $n*m$  matrix, please judging whether there exists two or more adjacent number with the same value in a same row or a same column.

### Input

The first line will be an integer  $T$  ( $1 \leq T \leq 20$ ), which is the number of test cases. For each test case, the first line will be two integer  $n$   $m$  ( $0 \leq n \leq 100$ ,  $0 \leq m \leq 100$ ) means the number of rows and columns in this two-dimensional array. The next  $n$  rows have  $m$  integers per row, which is the element in each row, and the size of each integer element is in a range  $[-2^{30}, 2^{30}]$ .

### Output

For each test case, if exists adjacent numbers, your program is expected to output "true", otherwise, "false".

### Sample Input

```
3
3 3
1 2 2
3 4 5
5 6 7
10 10
6 -6 -10 1 0 2 -9 -10 8 -4
8 9 -1 3 -1 -9 5 -9 -8 -2
7 -2 -9 -5 -3 3 -9 -7 -9 -5
-10 1 -9 -6 3 -10 -9 9 -8 -7
4 -1 -7 -2 -10 -7 9 -5 6 2
0 -3 -2 -5 0 2 -4 -9 -5 0
6 5 -3 -9 -3 3 -7 -6 -9 2
6 -5 8 2 9 -10 -10 -1 6 4
-4 0 -6 7 7 6 -7 -7 -6 -2
1 6 -8 4 -7 0 5 4 -1 -3
2 2
1 3
2 4
```

### Sample Output

```
true
true
false
```

## 2. Processing two-dimensional arrays

### Description:

There is a two-dimensional array that stores integers, and the number of elements in each row is not equal. We can do the following for the array:

**k r**: means to add k to all elements of the rth row (k is not equal to 0)

**0 r**: means to remove all 0 in the rth row

### Input:

The first line will be an integer T ( $1 \leq T \leq 10$ ), which is the number of test cases.

For each test case, the first line will be two integer n m ( $1 \leq n, m \leq 100$ ) means the number of rows in this two-dimensional array and the number of operations.

The next n rows are the two-dimensional array, and the first element of each row represents the number of elements in this row. The last m rows have two integers per row, which means the operation to be performed.

### Output:

For each test case, output the processed two-dimensional array, separated by a space.

### Sample Input:

```
2
3 3
3 1 2 3
3 2 -1 4
5 1 5 5 5 5
1 0
1 1
0 1
3 3
2 2 3
3 -1 -2 -3
3 -3 4 5
-2 0
3 2
0 0
```

### Sample Output:

```
2 3 4
3 5
1 5 5 5 5
1
-1 -2 -3
0 7 8
```

### 3. Center two-dimension array

**Description:**

Given a two-dimension array with different 2nd dimension lengths, center the two-dimension array based on the maximal 2nd dimension length and print it.

**Input:**

The first line will be an integer  $T$  ( $1 \leq T \leq 20$ ), which is the number of test cases.

For each test case:

- The first line will be an integer  $n$  ( $1 \leq n \leq 20$ ), which means the how many rows in the tow-dimensional array.
- The second line will be the  $n$  integers, for each integer, means the length of each row, and these  $n$  integers are all odd number or even number.
- The following  $n$  lines, for each line will be the data (from 0 to 9) in each row.

**Output:**

Print the centered two-dimension arrays from the first test case to the last the test case, and we use only '\n' to separate each test cases.

For each test case:

- There is only '\n' to separate each rows.
- We need to make sure that the intermediary number in all rows should be printed in a vertical line. (You can refer to the sample output)

For each rows, there is only a single space ' ' to separate each element.

**Sample Input:**

```
2
4
10 10 10 14
3 3 3 3 3 3 3 3
2 2 2 2 2 2 2 2
1 1 1 1 1 1 1 1
0 0 0 0 0 0 0 0 0 0
8
1 3 3 3 3 5 1
0
0 0 0
0 0 0
0 0 0
0 0 0
0 0 0
0 0 0 0
0
```

**Sample Output:**

333333333  
222222222  
111111111  
000000000000000  
0  
000  
000  
000  
000  
000  
00000  
0

#### 4. Pascal's triangle

**Description:**

In mathematics, Pascal's triangle is a triangular array of the binomial coefficients. The entry in the  $n$ th row and  $k$ th column of Pascal's triangle is denoted as  $(n, k)$ . For example, the unique nonzero entry in the topmost row is  $(0, 0) = 1$ . With this notation, the construction of the pascal's triangle paragraph may be written as:  $(n, k) = (n - 1, k - 1) + (n - 1, k)$  for any non-negative integer  $n$  and any integer  $k$  between 0 and  $n$ , inclusive.

Pascal's triangle determines the coefficients which arise in binomial expansions. For an example, consider the expansion:

$$(x + y)^2 = 1 \cdot x^2 \cdot y^0 + 2 \cdot x^1 \cdot y^1 + 1 \cdot x^0 \cdot y^2$$

The  $n$ th row of Pascal's triangle is the binomial coefficients of  $(x + y)^n$ .

$$(x + y)^n = a_0 \cdot x^n + a_1 \cdot x^{n-1} \cdot y + \dots + a_{n-1} \cdot x \cdot y^{n-1} + a_n \cdot y^n$$

The entry is  $a_i = (n, i)$

You need to print the  $n$ th row of Pascal's triangle.

**Input:**

The first line will be an integer  $T$  ( $1 \leq T \leq 150$ ), which is the number of test cases. For each test case, there will be one line of an integer  $n$  ( $1 \leq n \leq 33$ ) means the  $n$ th row needed to print.

**Output:**

For each test case, output entries of  $n$ th row of Pascal's triangle, separated by a space.

**Sample Input:**

```
4
4
3
2
1
```

**Sample Output:**

```
1 3 3 1
1 2 1
1 1
1
```

## 5. Sudoku

### Description

Sudoku is a famous mathematical game in which players fill numbers 1-9 in a 9 by 9 square. The square satisfies that every row and every column contain 1-9 only once, for example, a column contains [2 3 6 4 9 8 1 5 7] is valid but a column contains [1 1 3 6 8 4 2 9 7] is invalid. Specially, the square is divided into 9 “small squares”, that every small square has size 3 by 3. Of course, every “small square” also contains 1-9 only once. The picture is a valid sudoku (Notation that small squares are divided by red line).

2	9	3	7	1	5	4	8	6
8	6	1	2	4	9	5	3	7
7	4	5	8	6	3	1	9	2
6	7	8	9	2	1	3	4	5
1	3	9	5	7	4	2	6	8
4	5	2	6	3	8	7	1	9
9	2	4	3	8	7	6	5	1
3	8	6	1	5	2	9	7	4
5	1	7	4	9	6	8	2	3

After the player fills all the blanks in the sudoku, he wants to know whether he has finished it correct. So, the player turns to you to design a program to verify the correction of sudoku.

### Input

The question will contain several test cases, the integer T ( $1 \leq T \leq 20$ ) in the first line indicates the number of test cases.

For each test cases:

There will be 9 lines and every line has 9 integers, all the integers are from 1 to 9, split by a space character.

### Output

Each test cases have only one line for output. If the sudoku is valid, output “YES”, if not output “NO”.

### Sample input

```
2
9 7 8 3 1 2 6 4 5
3 1 2 6 4 5 9 7 8
6 4 5 9 7 8 3 1 2
7 8 9 1 2 3 4 5 6
1 2 3 4 5 6 7 8 9
4 5 6 7 8 9 1 2 3
8 9 7 2 3 1 5 6 4
```

2 3 1 5 6 4 8 9 7  
5 6 4 8 9 7 2 3 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1  
1 1 1 1 1 1 1 1 1

### **Sample output**

YES  
NO

## 6. Spiral Matrix [bonus]

### Description:

Given a matrix of  $m \times n$  elements ( $m$  rows,  $n$  columns), output an array that contains all elements of the matrix in clockwise spiral order, starting from the given position.

### Input:

The first line will be an integer  $T$  ( $1 \leq T \leq 10$ ), which is the number of test cases. For each test case, the first line will be two integers  $m$  and  $n$  ( $0 < m, n \leq 20$ ). Then there will be  $m$  lines, each line contains  $n$  integers, representing the matrix. After the matrix, the next line will be two integers  $x$  and  $y$  ( $0 \leq x < m, 0 \leq y < n$ ), which is the initial row and column position that the spiral path begins from.

### Output:

For each test case, output the array that contains all elements of the spiral path and there is only a single space ' ' to separate each element.

### Sample Input:

```
3
3 4
1 2 3 4
4 5 6 7
7 8 9 0
1 2
3 3
1 2 3
4 5 6
7 8 9
1 1
3 3
1 2 3
4 5 6
7 8 9
0 0
```

### Sample Output:

```
6 7 0 9 8 5 2 3 4 7 4 1
5 6 9 8 7 4 1 2 3
1 2 5 4 3 6 9 8 7
```



## 7. Spatial Convolution [bonus]

### Description

Convolution is a widely-used signal processing operation, and nowadays convolutional neural network is becoming a tremendously popular research interest. In this problem, you are asked to convolve some images with given kernels.

A greyscale digital image  $x$  consists of many pixels organized in rows and columns. The brightness of a pixel  $x[i][j]$  is discretized and usually represented by an integer ranging from 0 to 255. A two-dimensional kernel, or filter, is a small matrix indicating how to combine a pixel with its neighbors in the image to get a processed value. (Mathematically, a kernel is defined on an infinitely extended plane. When a kernel is given as a matrix with finite entries, you should consider any undefined value as 0.)

The discrete convolution of an image  $x$  and a kernel  $h$  can be calculated using the following formula:

$$(x \star h)[i, j] = \sum_{u=-\infty}^{\infty} \sum_{v=-\infty}^{\infty} x[u, v] h[i - u, j - v]$$

We may think about the formula in this way: To calculate the convolution sum at  $[i, j]$ , we first flip the kernel  $h$  in both dimensions, i.e. rotate it  $180^\circ$ . Then, place the flipped kernel  $h'$  on the original image such that the center of  $h'$  covers  $x[i, j]$ , do pointwise multiplication on the overlapped area, and sum up the products.

The sum would be the convolution sum at  $[i, j]$ .

To blur images, people usually use Gaussian kernels. Figure 1 may help you understand how a 2D Gaussian kernel looks like. Figure 2 depicts how  $(x \star h)[2, 3]$  is calculated. In figure 2, the overlapped area is surrounded by the red rectangle. To obtain a blurred image, we need to calculate every  $(x \star h)[i, j]$  in an analogous manner, and thus the rectangle should be shifted many times to cover every  $x[i, j]$ . In this problem, when  $h'$  is placed on the borders or at the corners of  $x$ , covering an area where some values of  $x$  is undefined, you should substitute them with their nearest defined values respectively.

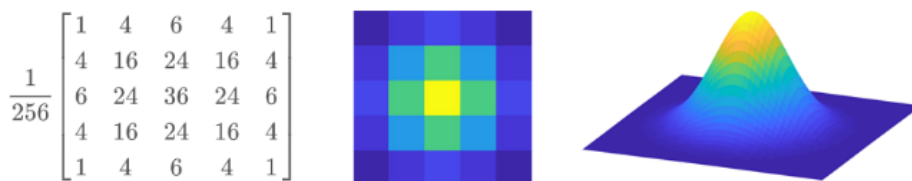


Fig.1 Two-dimensional gaussian kernels

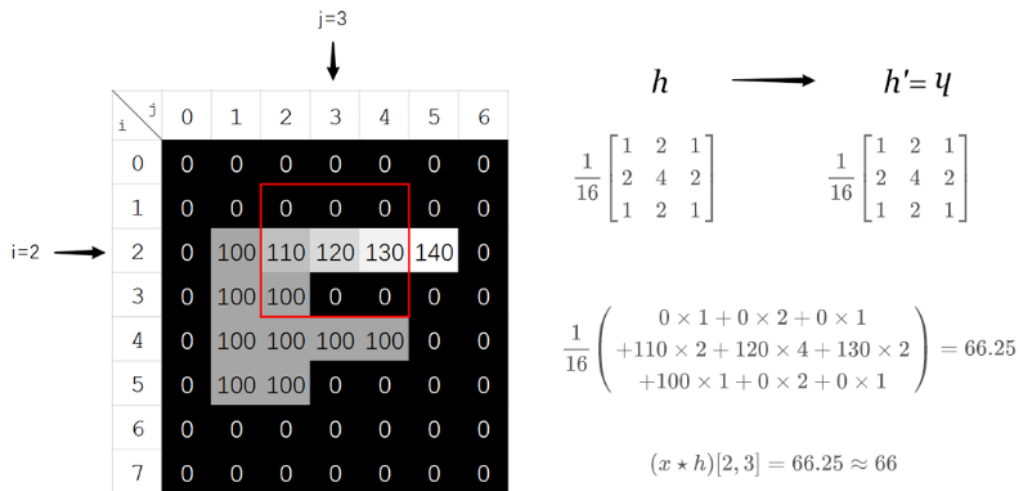


Fig.2 Calculating  $(x \star h)[2,3]$

Different convolution kernels lead to different processing effects. You are encouraged to visit [https://en.wikipedia.org/wiki/Kernel\\_\(image\\_processing\)](https://en.wikipedia.org/wiki/Kernel_(image_processing)) to see more convolution kernels. If you want to learn more about filtering operators for image processing, you can refer to Section 3.2 of *Computer Vision: Algorithms and Applications* by R. Szeliski. (Available on Springer: [https://link.springer.com/content/pdf/10.1007%2F978-1-84882-935-0\\_3.pdf](https://link.springer.com/content/pdf/10.1007%2F978-1-84882-935-0_3.pdf))

### Input

The first line of the input will be an integer  $T$  ( $1 \leq T \leq 10$ ), indicating the number of test cases.

For each test case:

The first line is an odd integer  $M$  ( $1 \leq M \leq 9$ ), followed by an  $M \times M$  matrix in the next  $M$  lines, which is the convolution kernel. Every entry of the convolution kernel has at most four decimal places. (A convolution kernel can contain negative values.)

Then come two integers  $H$  and  $W$  ( $1 \leq H, W \leq 100$ ), the height and width of the image. Each of the next  $H$  lines consists of  $W$  integers ranging from 0 to 255, representing the pixel values of the grayscale image to process.

### Output

For every test case, output the calculated spatial convolution in  $H$  lines, each of which contains  $W$  integers. You should round your results to the nearest integers. Pick a closest boundary value for a result that is smaller than 0 or greater than 255. You are supposed to right-align your output as the output example does. (Hint: use "%3d" as format string and add one more space between numbers.)

### Sample Input

```
3
3
0.0625 0.1250 0.0625
0.1250 0.2500 0.1250
0.0625 0.1250 0.0625
8 7
0 0 0 0 0 0 0
0 0 0 0 0 0 0
```

0	100	110	120	130	140	0
0	100	100	0	0	0	0
0	100	100	100	100	0	0
0	100	100	0	0	0	0
0	0	0	0	0	0	0
0	0	0	0	0	0	0

5

0.04	0.04	0.04	0.04	0.04
0.04	0.04	0.04	0.04	0.04
0.04	0.04	0.04	0.04	0.04
0.04	0.04	0.04	0.04	0.04
0.04	0.04	0.04	0.04	0.04

1 1

100

3

-1 0 1

-2 0 2

-1 0 1

3 3

9 8 7

0 1 0

7 9 8

### Sample Output

0	0	0	0	0	0	0
6	19	28	30	33	26	9
19	58	74	66	65	51	18
25	76	90	68	51	32	9
25	75	88	63	38	13	0
19	56	63	38	19	6	0
6	19	19	6	0	0	0
0	0	0	0	0	0	0

100

2	6	4
0	1	4
0	0	4