

10/29/24

Neural Network - HW6

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1) a) Given:

$$f_i = \frac{e^{z_i}}{\sum_j e^{z_j}}$$

$$l(y, f) = \sum_i y_i \log \frac{1}{f_i} \quad \text{--- (1)}$$

where y is non negative, $\sum y_i = 1$

Computing the gradient wrt f_i in (1)

$$\frac{\partial l}{\partial f_i} = -\frac{y_i}{f_i} \quad \text{--- (2)}$$

b) Backpropagation equation from $\nabla_1 l$ to $\nabla_2 l$.

Since we know that $f_i = \frac{e^{z_i}}{\sum_j e^{z_j}}$

using chainrule we can derive that

$$\frac{\partial l}{\partial z_i} = \sum_j \frac{\partial l}{\partial f_j} \cdot \frac{\partial f_j}{\partial z_i} \quad \text{--- (3)}$$

c) Subs. ② + ③.

$$\nabla_{21} = \frac{\partial \ell}{\partial z_1} = \beta_i - y_i$$

$$\frac{\partial \ell}{\partial \beta_i} = \frac{1}{n} \sum_{i=1}^n (y_i - \beta_i)$$

①) $\frac{\partial \ell}{\partial \beta_i} = 0$ for all i

②) $\frac{\partial \ell}{\partial \beta_i} = 0$ for all i

$$\frac{\partial \ell}{\partial \beta_i} = \frac{1}{n} \sum_{i=1}^n (y_i - \beta_i)$$

③) $\frac{\partial \ell}{\partial \beta_i} = 0$ for all i

$$\frac{\partial \ell}{\partial \beta_i} = \frac{1}{n} \sum_{i=1}^n (y_i - \beta_i)$$

④) $\frac{\partial \ell}{\partial \beta_i} = 0$ for all i

$$\frac{\partial \ell}{\partial \beta_i} = \frac{1}{n} \sum_{i=1}^n (y_i - \beta_i)$$

2. b)

```
➡ Using cpu device
NeuralNetwork(
  (fc1): Linear(in_features=784, out_features=200, bias=True)
  (fc2): Linear(in_features=200, out_features=200, bias=True)
  (fc3): Linear(in_features=200, out_features=10, bias=True)
)
```

Epoch 1

```
-----
loss: 2.317232 [ 64/60000]
loss: 2.295797 [ 6464/60000]
loss: 2.292961 [12864/60000]
loss: 2.300758 [19264/60000]
loss: 2.283749 [25664/60000]
loss: 2.296002 [32064/60000]
loss: 2.274789 [38464/60000]
loss: 2.277119 [44864/60000]
loss: 2.272804 [51264/60000]
loss: 2.266154 [57664/60000]
Test Error:
Accuracy: 43.7%, Avg loss: 2.269623
```

Epoch 2

```
-----
loss: 2.263774 [ 64/60000]
loss: 2.267873 [ 6464/60000]
loss: 2.256180 [12864/60000]
loss: 2.260281 [19264/60000]
loss: 2.258021 [25664/60000]
loss: 2.262865 [32064/60000]
loss: 2.255936 [38464/60000]
loss: 2.252871 [44864/60000]
loss: 2.236404 [51264/60000]
loss: 2.230034 [57664/60000]
Test Error:
Accuracy: 59.7%, Avg loss: 2.226548
```

Epoch 3

```
-----
loss: 2.222221 [ 64/60000]
loss: 2.230322 [ 6464/60000]
loss: 2.216831 [12864/60000]
loss: 2.211512 [19264/60000]
loss: 2.207336 [25664/60000]
loss: 2.187446 [32064/60000]
loss: 2.185654 [38464/60000]
loss: 2.163105 [44864/60000]
loss: 2.167564 [51264/60000]
loss: 2.178476 [57664/60000]
Test Error:
Accuracy: 63.2%, Avg loss: 2.153835
```

Epoch 4

```
-----
loss: 2.146271 [ 64/60000]
loss: 2.153185 [ 6464/60000]
loss: 2.146166 [12864/60000]
loss: 2.097913 [19264/60000]
loss: 2.122499 [25664/60000]
loss: 2.101561 [32064/60000]
loss: 2.067542 [38464/60000]
loss: 2.042393 [44864/60000]
loss: 2.051870 [51264/60000]
loss: 2.043984 [57664/60000]
Test Error:
Accuracy: 64.5%, Avg loss: 2.022980
```

Epoch 5

```
-----
loss: 1.998259 [ 64/60000]
loss: 2.049722 [ 6464/60000]
loss: 2.032401 [12864/60000]
loss: 1.978890 [19264/60000]
loss: 1.938801 [25664/60000]
loss: 1.916338 [32064/60000]
loss: 1.951066 [38464/60000]
loss: 1.862448 [44864/60000]
loss: 1.840247 [51264/60000]
loss: 1.793576 [57664/60000]
Test Error:
Accuracy: 66.9%, Avg loss: 1.803158
```

Epoch 6

```
-----
loss: 1.818758 [ 64/60000]
loss: 1.826935 [ 6464/60000]
loss: 1.838849 [12864/60000]
loss: 1.749794 [19264/60000]
loss: 1.651051 [25664/60000]
loss: 1.706330 [32064/60000]
loss: 1.711715 [38464/60000]
loss: 1.646418 [44864/60000]
loss: 1.590284 [51264/60000]
loss: 1.495407 [57664/60000]
Test Error:
Accuracy: 71.8%, Avg loss: 1.498418
```

Epoch 7

```
loss: 1.552967 [ 64/60000]
loss: 1.398770 [ 6464/60000]
loss: 1.411034 [12864/60000]
loss: 1.337801 [19264/60000]
loss: 1.374751 [25664/60000]
loss: 1.323522 [32064/60000]
loss: 1.320986 [38464/60000]
loss: 1.378839 [44864/60000]
loss: 1.221678 [51264/60000]
loss: 1.243457 [57664/60000]
```

Test Error:

Accuracy: 76.6%, Avg loss: 1.189543

Epoch 8

```
loss: 1.084921 [ 64/60000]
loss: 1.119827 [ 6464/60000]
loss: 1.181804 [12864/60000]
loss: 1.258242 [19264/60000]
loss: 1.169763 [25664/60000]
loss: 1.136437 [32064/60000]
loss: 1.066760 [38464/60000]
loss: 1.084299 [44864/60000]
loss: 0.900540 [51264/60000]
loss: 0.983532 [57664/60000]
```

Test Error:

Accuracy: 79.7%, Avg loss: 0.959550

Epoch 9

```
loss: 0.907628 [ 64/60000]
loss: 0.949432 [ 6464/60000]
loss: 0.939754 [12864/60000]
loss: 0.817330 [19264/60000]
loss: 0.873873 [25664/60000]
loss: 1.100950 [32064/60000]
loss: 0.817576 [38464/60000]
loss: 0.812407 [44864/60000]
loss: 0.938766 [51264/60000]
loss: 0.785961 [57664/60000]
```

Test Error:

Accuracy: 81.7%, Avg loss: 0.807746

Epoch 10

```
loss: 0.903691 [ 64/60000]
loss: 0.740208 [ 6464/60000]
loss: 0.851091 [12864/60000]
loss: 0.811425 [19264/60000]
loss: 0.809761 [25664/60000]
loss: 0.895571 [32064/60000]
loss: 0.779057 [38464/60000]
loss: 0.603100 [44864/60000]
loss: 0.799368 [51264/60000]
loss: 0.910713 [57664/60000]
```

Test Error:

Accuracy: 83.1%, Avg loss: 0.705340

Hyperparameters:

Learning Rate: 0.001, Batch Size: 64, Epochs: 10

3. a)

```
Using cpu device
CNNModel(
  (conv1): Conv2d(1, 20, kernel_size=(4, 4), stride=(1, 1))
  (relu1): ReLU()
  (conv2): Conv2d(20, 20, kernel_size=(4, 4), stride=(2, 2))
  (relu2): ReLU()
  (pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (fc1): Linear(in_features=500, out_features=250, bias=True)
  (relu3): ReLU()
  (fc2): Linear(in_features=250, out_features=10, bias=True)
)
```

```
class CNNModel(nn.Module):
    def __init__(self):
        super(CNNModel, self).__init__()
        self.conv1 = nn.Conv2d(in_channels=1, out_channels=20, kernel_size=4, stride=1)
        self.relu1 = nn.ReLU()
        self.conv2 = nn.Conv2d(in_channels=20, out_channels=20, kernel_size=4, stride=2)
        self.relu2 = nn.ReLU()
        self.pool = nn.MaxPool2d(kernel_size=2, stride=2)
        self.fc1 = nn.Linear(20 * 5 * 5, 250)
        self.relu3 = nn.ReLU()
        self.fc2 = nn.Linear(250, 10)

    def forward(self, x):
        x = self.relu1(self.conv1(x))
        x = self.relu2(self.conv2(x))
        x = self.pool(x)
        x = x.view(x.size(0), -1)
        x = self.relu3(self.fc1(x))
        x = self.fc2(x)
        return x

model = CNNModel()
```

b)

<div>Epoch 1</div> <div>loss: 2.305104 [64/60000]</div> <div>loss: 2.303448 [6464/60000]</div> <div>loss: 2.294596 [12864/60000]</div> <div>loss: 2.296383 [19264/60000]</div> <div>loss: 2.295296 [25664/60000]</div> <div>loss: 2.289412 [32064/60000]</div> <div>loss: 2.298305 [38464/60000]</div> <div>loss: 2.298476 [44864/60000]</div> <div>loss: 2.296193 [51264/60000]</div> <div>loss: 2.296289 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 14.2%, Avg loss: 2.294679</div>	<div>Epoch 4</div> <div>loss: 2.246596 [64/60000]</div> <div>loss: 2.242231 [6464/60000]</div> <div>loss: 2.245816 [12864/60000]</div> <div>loss: 2.212727 [19264/60000]</div> <div>loss: 2.238058 [25664/60000]</div> <div>loss: 2.226318 [32064/60000]</div> <div>loss: 2.204172 [38464/60000]</div> <div>loss: 2.168584 [44864/60000]</div> <div>loss: 2.176803 [51264/60000]</div> <div>loss: 2.154619 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 61.0%, Avg loss: 2.137171</div>
<div>Epoch 2</div> <div>loss: 2.289654 [64/60000]</div> <div>loss: 2.293405 [6464/60000]</div> <div>loss: 2.290475 [12864/60000]</div> <div>loss: 2.296170 [19264/60000]</div> <div>loss: 2.292363 [25664/60000]</div> <div>loss: 2.291523 [32064/60000]</div> <div>loss: 2.294999 [38464/60000]</div> <div>loss: 2.283917 [44864/60000]</div> <div>loss: 2.282780 [51264/60000]</div> <div>loss: 2.285823 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 21.6%, Avg loss: 2.282664</div>	<div>Epoch 5</div> <div>loss: 2.149927 [64/60000]</div> <div>loss: 2.123748 [6464/60000]</div> <div>loss: 2.032661 [12864/60000]</div> <div>loss: 2.024104 [19264/60000]</div> <div>loss: 1.963973 [25664/60000]</div> <div>loss: 1.885181 [32064/60000]</div> <div>loss: 1.745482 [38464/60000]</div> <div>loss: 1.614492 [44864/60000]</div> <div>loss: 1.469387 [51264/60000]</div> <div>loss: 1.528122 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 75.0%, Avg loss: 1.299685</div>
<div>Epoch 3</div> <div>loss: 2.279245 [64/60000]</div> <div>loss: 2.278999 [6464/60000]</div> <div>loss: 2.273145 [12864/60000]</div> <div>loss: 2.267029 [19264/60000]</div> <div>loss: 2.273639 [25664/60000]</div> <div>loss: 2.275116 [32064/60000]</div> <div>loss: 2.276027 [38464/60000]</div> <div>loss: 2.260669 [44864/60000]</div> <div>loss: 2.266533 [51264/60000]</div> <div>loss: 2.253453 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 44.4%, Avg loss: 2.253181</div>	<div>Epoch 6</div> <div>loss: 1.394576 [64/60000]</div> <div>loss: 1.158404 [6464/60000]</div> <div>loss: 1.032260 [12864/60000]</div> <div>loss: 1.086673 [19264/60000]</div> <div>loss: 1.030844 [25664/60000]</div> <div>loss: 0.925704 [32064/60000]</div> <div>loss: 0.888781 [38464/60000]</div> <div>loss: 0.667631 [44864/60000]</div> <div>loss: 0.709151 [51264/60000]</div> <div>loss: 0.518154 [57664/60000]</div> <div>Test Error:</div> <div>Accuracy: 83.4%, Avg loss: 0.603303</div>

Epoch 7

```
-----  
loss: 0.604298 [ 64/60000]  
loss: 0.586471 [ 6464/60000]  
loss: 0.709707 [12864/60000]  
loss: 0.577819 [19264/60000]  
loss: 0.585110 [25664/60000]  
loss: 0.519224 [32064/60000]  
loss: 0.423448 [38464/60000]  
loss: 0.369643 [44864/60000]  
loss: 0.522212 [51264/60000]  
loss: 0.205503 [57664/60000]
```

Test Error:

Accuracy: 86.6%, Avg loss: 0.466286

Epoch 8

```
-----  
loss: 0.281309 [ 64/60000]  
loss: 0.550678 [ 6464/60000]  
loss: 0.409051 [12864/60000]  
loss: 0.467448 [19264/60000]  
loss: 0.511992 [25664/60000]  
loss: 0.444320 [32064/60000]  
loss: 0.589170 [38464/60000]  
loss: 0.462137 [44864/60000]  
loss: 0.507723 [51264/60000]  
loss: 0.377445 [57664/60000]
```

Test Error:

Accuracy: 87.8%, Avg loss: 0.413807

Epoch 9

```
-----  
loss: 0.620323 [ 64/60000]  
loss: 0.474886 [ 6464/60000]  
loss: 0.407568 [12864/60000]  
loss: 0.329935 [19264/60000]  
loss: 0.299089 [25664/60000]  
loss: 0.427519 [32064/60000]  
loss: 0.350101 [38464/60000]  
loss: 0.432922 [44864/60000]  
loss: 0.532287 [51264/60000]  
loss: 0.454067 [57664/60000]
```

Test Error:

Accuracy: 88.7%, Avg loss: 0.383164

Epoch 10

```
-----  
loss: 0.496418 [ 64/60000]  
loss: 0.425211 [ 6464/60000]  
loss: 0.543954 [12864/60000]  
loss: 0.313636 [19264/60000]  
loss: 0.253047 [25664/60000]  
loss: 0.545872 [32064/60000]  
loss: 0.545942 [38464/60000]  
loss: 0.461102 [44864/60000]  
loss: 0.281568 [51264/60000]  
loss: 0.297356 [57664/60000]
```

Test Error:

Accuracy: 89.3%, Avg loss: 0.360136

Hyperparameters:

Learning Rate: 0.001, Batch Size: 64, Epochs: 10

c)

```
CNNModelWithDropout(
  (conv1): Conv2d(1, 20, kernel_size=(4, 4), stride=(1, 1))
  (relu1): ReLU()
  (conv2): Conv2d(20, 20, kernel_size=(4, 4), stride=(2, 2))
  (relu2): ReLU()
  (pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)
  (dropout): Dropout(p=0.5, inplace=False)
  (fc1): Linear(in_features=500, out_features=250, bias=True)
  (relu3): ReLU()
  (fc2): Linear(in_features=250, out_features=10, bias=True)
)
```

Epoch 1

```
loss: 2.283238 [ 64/60000]
loss: 2.314235 [ 6464/60000]
loss: 2.279460 [12864/60000]
loss: 2.289670 [19264/60000]
loss: 2.274018 [25664/60000]
loss: 2.235802 [32064/60000]
loss: 2.247103 [38464/60000]
loss: 2.247018 [44864/60000]
loss: 2.177578 [51264/60000]
loss: 2.188517 [57664/60000]
Test Error:
```

Accuracy: 55.0%, Avg loss: 2.206920

Epoch 2

```
loss: 2.192111 [ 64/60000]
loss: 2.137678 [ 6464/60000]
loss: 2.114167 [12864/60000]
loss: 1.979584 [19264/60000]
loss: 1.835543 [25664/60000]
loss: 1.834327 [32064/60000]
loss: 1.641800 [38464/60000]
loss: 1.509361 [44864/60000]
loss: 1.345453 [51264/60000]
loss: 1.167914 [57664/60000]
Test Error:
```

Accuracy: 76.7%, Avg loss: 1.420294

Epoch 3

```
loss: 1.405715 [ 64/60000]
loss: 1.216583 [ 6464/60000]
loss: 1.132421 [12864/60000]
loss: 1.155114 [19264/60000]
loss: 1.081555 [25664/60000]
loss: 0.865617 [32064/60000]
loss: 0.754709 [38464/60000]
loss: 1.066637 [44864/60000]
loss: 0.835639 [51264/60000]
loss: 0.499551 [57664/60000]
Test Error:
```

Accuracy: 84.7%, Avg loss: 0.864635

Epoch 4

```
loss: 0.763842 [ 64/60000]
loss: 0.610005 [ 6464/60000]
loss: 0.880354 [12864/60000]
loss: 0.588702 [19264/60000]
loss: 0.734527 [25664/60000]
loss: 0.614807 [32064/60000]
loss: 0.685144 [38464/60000]
loss: 0.654472 [44864/60000]
loss: 0.714165 [51264/60000]
loss: 0.635322 [57664/60000]
Test Error:
```

Accuracy: 86.7%, Avg loss: 0.703424

Epoch 5

```
loss: 1.059462 [ 64/60000]
loss: 0.627940 [ 6464/60000]
loss: 0.752802 [12864/60000]
loss: 0.642829 [19264/60000]
loss: 0.573602 [25664/60000]
loss: 0.515676 [32064/60000]
loss: 0.783810 [38464/60000]
loss: 0.414306 [44864/60000]
loss: 0.540178 [51264/60000]
loss: 0.583219 [57664/60000]
Test Error:
```

Accuracy: 87.9%, Avg loss: 0.616760

Epoch 6

```
loss: 0.685004 [ 64/60000]
loss: 0.636888 [ 6464/60000]
loss: 0.876887 [12864/60000]
loss: 0.476076 [19264/60000]
loss: 0.649369 [25664/60000]
loss: 0.507159 [32064/60000]
loss: 0.750487 [38464/60000]
loss: 0.651003 [44864/60000]
loss: 0.615696 [51264/60000]
loss: 0.542635 [57664/60000]
Test Error:
```

Accuracy: 88.9%, Avg loss: 0.576922


```
Epoch 7
-----
loss: 0.595698 [ 64/60000]
loss: 0.694466 [ 6464/60000]
loss: 0.421711 [12864/60000]
loss: 0.582856 [19264/60000]
loss: 0.553170 [25664/60000]
loss: 0.669336 [32064/60000]
loss: 0.512973 [38464/60000]
loss: 0.436768 [44864/60000]
loss: 0.421563 [51264/60000]
loss: 0.492979 [57664/60000]
Test Error:
Accuracy: 89.6%, Avg loss: 0.538222
```

```
Epoch 8
-----
loss: 0.630278 [ 64/60000]
loss: 0.440131 [ 6464/60000]
loss: 0.638388 [12864/60000]
loss: 0.658343 [19264/60000]
loss: 0.509535 [25664/60000]
loss: 0.480949 [32064/60000]
loss: 0.260180 [38464/60000]
loss: 0.600495 [44864/60000]
loss: 0.470967 [51264/60000]
loss: 0.587227 [57664/60000]
Test Error:
Accuracy: 90.4%, Avg loss: 0.515293
```

```
Epoch 9
-----
loss: 0.393578 [ 64/60000]
loss: 0.393482 [ 6464/60000]
loss: 0.389347 [12864/60000]
loss: 0.400769 [19264/60000]
loss: 0.319928 [25664/60000]
loss: 0.456398 [32064/60000]
loss: 0.588937 [38464/60000]
loss: 0.355831 [44864/60000]
loss: 0.334114 [51264/60000]
loss: 0.442764 [57664/60000]
Test Error:
Accuracy: 90.6%, Avg loss: 0.490666
```

```
Epoch 10
-----
loss: 0.308005 [ 64/60000]
loss: 0.450437 [ 6464/60000]
loss: 0.455028 [12864/60000]
loss: 0.504925 [19264/60000]
loss: 0.274534 [25664/60000]
loss: 0.416096 [32064/60000]
loss: 0.503397 [38464/60000]
loss: 0.271194 [44864/60000]
loss: 0.436766 [51264/60000]
loss: 0.480191 [57664/60000]
Test Error:
Accuracy: 91.1%, Avg loss: 0.461365
```

Hyperparameters:

Learning Rate: 0.001, Batch Size: 64, Epochs: 10, Weight Decay: 0.0005

d)

```
CNNModelWithBatchNorm(  
  (conv1): Conv2d(1, 20, kernel_size=(4, 4), stride=(1, 1))  
  (bn1): BatchNorm2d(20, eps=1e-05, momentum=0.1, affine=True, track_running_stats=True)  
  (relu1): ReLU()  
  (conv2): Conv2d(20, 20, kernel_size=(4, 4), stride=(2, 2))  
  (bn2): BatchNorm2d(20, eps=1e-05, momentum=0.1, affine=True, track_running_stats=True)  
  (relu2): ReLU()  
  (pool): MaxPool2d(kernel_size=2, stride=2, padding=0, dilation=1, ceil_mode=False)  
  (fc1): Linear(in_features=500, out_features=250, bias=True)  
  (bn3): BatchNorm1d(250, eps=1e-05, momentum=0.1, affine=True, track_running_stats=True)  
  (relu3): ReLU()  
  (fc2): Linear(in_features=250, out_features=10, bias=True)  
)
```

Epoch 1

```
loss: 2.324754 [ 64/60000]  
loss: 1.759311 [ 6464/60000]  
loss: 1.369600 [12864/60000]  
loss: 1.224094 [19264/60000]  
loss: 1.140897 [25664/60000]  
loss: 0.936820 [32064/60000]  
loss: 0.984665 [38464/60000]  
loss: 0.768954 [44864/60000]  
loss: 0.770214 [51264/60000]  
loss: 0.660641 [57664/60000]  
Test Error:  
Accuracy: 89.8%, Avg loss: 0.611704
```

Epoch 2

```
loss: 0.573018 [ 64/60000]  
loss: 0.616314 [ 6464/60000]  
loss: 0.607676 [12864/60000]  
loss: 0.596551 [19264/60000]  
loss: 0.594288 [25664/60000]  
loss: 0.577056 [32064/60000]  
loss: 0.339757 [44864/60000]  
loss: 0.544697 [51264/60000]  
loss: 0.359833 [57664/60000]  
Test Error:  
Accuracy: 93.2%, Avg loss: 0.368206
```

Epoch 3

```
loss: 0.467123 [ 64/60000]  
loss: 0.392933 [ 6464/60000]  
loss: 0.373965 [12864/60000]  
loss: 0.292960 [19264/60000]  
loss: 0.304315 [25664/60000]  
loss: 0.406189 [32064/60000]  
loss: 0.261403 [38464/60000]  
loss: 0.274273 [44864/60000]  
loss: 0.295395 [51264/60000]  
loss: 0.314184 [57664/60000]  
Test Error:  
Accuracy: 94.7%, Avg loss: 0.269849
```

Epoch 4

```
loss: 0.218656 [ 64/60000]  
loss: 0.318545 [ 6464/60000]  
loss: 0.235798 [12864/60000]  
loss: 0.301782 [19264/60000]  
loss: 0.202407 [25664/60000]  
loss: 0.390220 [32064/60000]  
loss: 0.190847 [38464/60000]  
loss: 0.223202 [44864/60000]  
loss: 0.232732 [51264/60000]  
loss: 0.226401 [57664/60000]  
Test Error:  
Accuracy: 95.5%, Avg loss: 0.218361
```

Epoch 5

```
loss: 0.157900 [ 64/60000]  
loss: 0.257836 [ 6464/60000]  
loss: 0.190923 [12864/60000]  
loss: 0.139174 [19264/60000]  
loss: 0.329085 [25664/60000]  
loss: 0.215989 [32064/60000]  
loss: 0.214765 [38464/60000]  
loss: 0.267469 [44864/60000]  
loss: 0.284139 [51264/60000]  
loss: 0.164501 [57664/60000]  
Test Error:  
Accuracy: 96.2%, Avg loss: 0.182517
```

Epoch 6

```
loss: 0.231232 [ 64/60000]  
loss: 0.126510 [ 6464/60000]  
loss: 0.248154 [12864/60000]  
loss: 0.235646 [19264/60000]  
loss: 0.155312 [25664/60000]  
loss: 0.121266 [32064/60000]  
loss: 0.174179 [38464/60000]  
loss: 0.283515 [44864/60000]  
loss: 0.270045 [51264/60000]  
loss: 0.261434 [57664/60000]  
Test Error:  
Accuracy: 96.5%, Avg loss: 0.160153
```

```
Epoch 7
-----
loss: 0.152310 [ 64/60000]
loss: 0.175591 [ 6464/60000]
loss: 0.194813 [12864/60000]
loss: 0.135895 [19264/60000]
loss: 0.136818 [25664/60000]
loss: 0.138605 [32064/60000]
loss: 0.205606 [38464/60000]
loss: 0.261998 [44864/60000]
loss: 0.192953 [51264/60000]
loss: 0.078076 [57664/60000]
Test Error:
Accuracy: 96.9%, Avg loss: 0.142399
```

```
Epoch 8
-----
loss: 0.099534 [ 64/60000]
loss: 0.218057 [ 6464/60000]
loss: 0.130247 [12864/60000]
loss: 0.168080 [19264/60000]
loss: 0.115223 [25664/60000]
loss: 0.158313 [32064/60000]
loss: 0.171455 [38464/60000]
loss: 0.143945 [44864/60000]
loss: 0.205392 [51264/60000]
loss: 0.179394 [57664/60000]
Test Error:
Accuracy: 97.1%, Avg loss: 0.128072
```

```
Epoch 9
-----
loss: 0.158578 [ 64/60000]
loss: 0.111646 [ 6464/60000]
loss: 0.143449 [12864/60000]
loss: 0.080239 [19264/60000]
loss: 0.095026 [25664/60000]
loss: 0.200723 [32064/60000]
loss: 0.174261 [38464/60000]
loss: 0.114019 [44864/60000]
loss: 0.175731 [51264/60000]
loss: 0.117175 [57664/60000]
Test Error:
Accuracy: 97.3%, Avg loss: 0.118689
```

```
Epoch 10
-----
loss: 0.190206 [ 64/60000]
loss: 0.139715 [ 6464/60000]
loss: 0.111545 [12864/60000]
loss: 0.147483 [19264/60000]
loss: 0.208482 [25664/60000]
loss: 0.075030 [32064/60000]
loss: 0.150385 [38464/60000]
loss: 0.194499 [44864/60000]
loss: 0.096000 [51264/60000]
loss: 0.114713 [57664/60000]
Test Error:
Accuracy: 97.4%, Avg loss: 0.109613
```

Hyperparameters:

Learning Rate: 0.001, Batch Size: 64, Epochs: 10, Weight Decay: 0.0005