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1 / $\forall x (\neg P(x) \rightarrow Q(x) \wedge R(x))$

premise $\rightarrow e$

2 / $\forall x (\neg Q(x) \vee \neg R(x)) \rightarrow P(x)$

1, MP, de Morgan

3 $\exists x (\neg Q(x) \vee \neg R(x)) \rightarrow P(x)$

$\forall e$

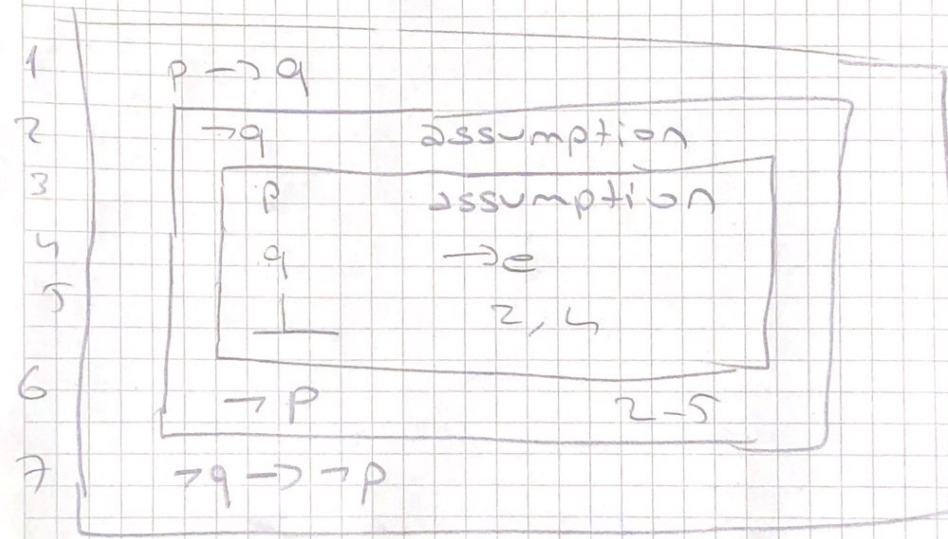
4 / $\exists y (\neg R(y) \vee \neg Q(y))$

premise

5 / $\exists z P(z)$

2, 3, $\rightarrow e$, $\exists i$

lemma MP:



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lemma De Morgan:

1 $\neg(p \wedge q)$

2 $\neg(\neg p \vee \neg q)$ assump

3 $\neg p$ assump

4 $\neg p \vee \neg q$ \vee_i

5 \perp

6 p 3-5

7 $\neg q$ assump

8 $\neg q \vee \neg p$ \vee_i

9 \perp 8, 2

10 q 7-9

11 $p \wedge q$ $\wedge_i, 2, 9$

12 \perp

13 $\neg p \vee \neg q$

