

MATH 487 Deterministic Operations Research

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Contents

| | |
|-----------------------------|----------|
| 1 Linear Programming | 2 |
|-----------------------------|----------|

1 Linear Programming

Definition 1.1. Linear programming: The optimization of a linear function subject to linear constraints.

Example. Suppose a starving artist is trying to plan a food budget. He is health conscious and wants a healthy diet that includes the following: at least 70 g of protein per day, at least 100 g of carbohydrates per day, exactly 15 mg of vitamin D per day, but no more than 75 g of fat per day.

Five foods to choose from (fix formatting later):

| Food | Protein | Carbohydrates | Vitamin D | Fat | Cost |
|-----------|---------|---------------|-----------|---------|------------|
| Hamburger | 10g/oz | 2g/oz | .5mg/oz | 8g/oz | \$0.20/oz |
| Milk | 2g/oz | 3 g/oz | 4mg/oz | 2g/oz | \$0.02/oz |
| Cereal | 3g/oz | 23g/oz | 2mg/oz | 1g/oz | \$0.10/oz |
| Ch. N S | 2g/oz | 2g/oz | 0 mg/oz | 0.5g/oz | \$0.03/oz |
| Eggs | 6g/egg | 4g/egg | 1mg/egg | 5g/egg | \$0.10/egg |

Question: How can he meet dietary goals while minimizing cost?

Answer. Set up **decision variables**:

H, M, C, CNS, and E are oz (or number) per day

Constraints:

$$\text{Protein: } p = 10H + 2M + 3C + 2CNS + 6E \geq 70$$

$$\text{Carbs: } c = 2H + 3M + 23C + 2CNS + 4E \geq 100$$

$$\text{Vitamin D: } 0.5H + 4M + 2C + E = 15$$

$$\text{Fat: } f = 8H + 2M + 1C + 0.5CNS + 5E \leq 75$$

$$\text{Nonnegativity: } H, M, C, CNS, E \geq 0$$

Subject to these requirements, we wish to minimize cost:

$$\text{cost} = 20H + 2M + 10C + 3CNS + 10E$$

(*)

Definition 1.2. Let $f : \mathbb{R}^n \rightarrow \mathbb{R}$ be a function of n variables, then f is called linear $\iff f$ is of the form

$$f(x_1, x_2, \dots, x_n) = a_1x_1 + a_2x_2 + \dots + a_nx_n + b_0$$

for some constraints

$$a_1, a_2, \dots, a_n \text{ and } b_0$$

Definition 1.3. A linear equation is an equation of the form $f(x_1, \dots, x_n) = a$ constant.

Definition 1.4. A linear inequality is an inequality of the form $f(x_1, \dots, x_n) \leq$ a constant, or $f(x_1, \dots, x_n) \geq$ a constant.

Definition 1.5. A linear constraint is either a linear equation or a linear inequality.

Definition 1.6. A linear program is the optimization of a linear function subject to linear constraints.