

Proiect Modelare si Simulare

Pendulul Dublu

Dumitru Samuel Irinel - 331AB

December 31, 2023

Cuprins

- Cerinta 1
- Cerinta 2
- Cerinta 3
- Cerinta 4
- Cerinta 5 & 6
- Cerinta 7
- Cerinta 8
- Cerinta 9
- Cerinta 10
- Cerinta 11
- Cerinta 12
- Cerinta 13
- Cerinta 14
- Cerinta 15

Cerinta 1

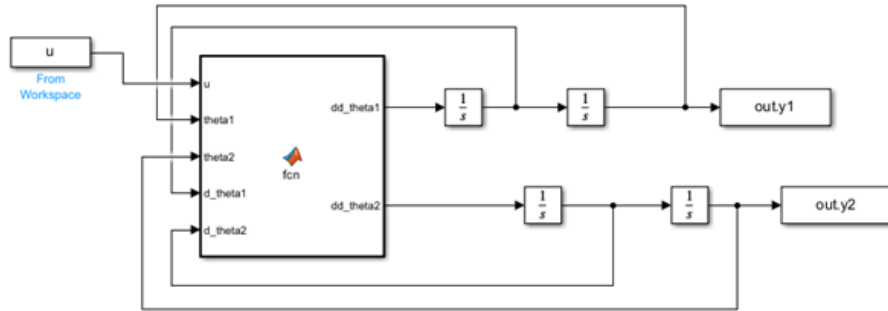


Figure 1: Matlab Function

```
function [dd_theta1,dd_theta2] = fcn(u, theta1,theta2,d_theta1,d_theta2)
```

```
zeta = 0.7;
```

```
g = 10;
```

```
m = 5;
```

```
l = 1;
```

```
A = - (d_theta2^2) * sin(theta1 - theta2) - 2 * g * sin(theta1) / l - zeta * d_theta1 + u / (m * l * l);
```

```
B = (d_theta1^2) * sin(theta1 - theta2) - g * sin(theta2) / l - zeta * d_theta2;
```

```
dd_theta1 = (B * cos(theta1 - theta2) - A) / (-cos(2 * (theta1 - theta2)));
```

```
dd_theta2 = (2 * B - A * cos(theta1 - theta2)) / (cos(2 * (theta1 - theta2)));
```

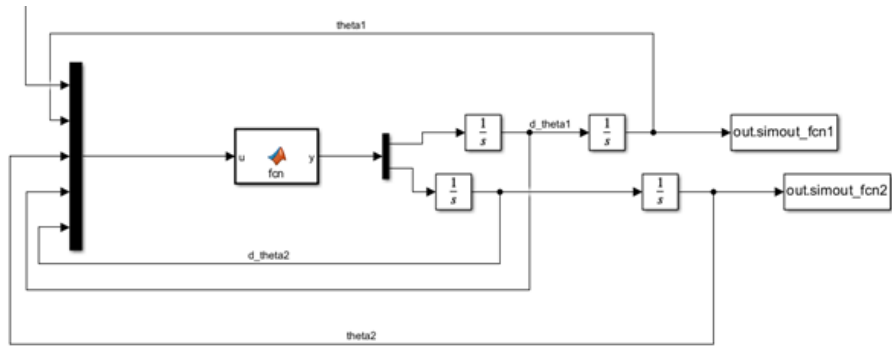


Figure 2: Bloc FCN SISO

```

function y = fcn(u)

zeta = 0.7;
g = 10;
m = 5;
l = 1;
ys = [0;0];
A = - (u(5)^2) * sin(u(2)- u(3))- 2 *g*sin(u(2))/1 - zeta*u(4)+ u(1)/(m*l*1);
B = (u(4)^2) * sin(u(2) - u(3)) - g*sin(u(3))/1 - zeta*u(5);

ys(1) = (B* cos( u(2) - u(3)) - A )/( - cos(2*(u(2) - u(3)))));
ys(2)= (2*B -A* cos( u(2) - u(3)) )/( cos(2*(u(2) - u(3))) );

y = ys;

```

Cerinta 2

Timpul de simulare l-am ales 45 secunde deoarece atunci ajunge modelul meu in regim permanent la intrare treapta*10

```

Tmax = 45;
t = linspace(0,Tmax,100);
u1 = 10.*double(t>=0);
usim = timeseries(u1,t);

```

Cerinta 3

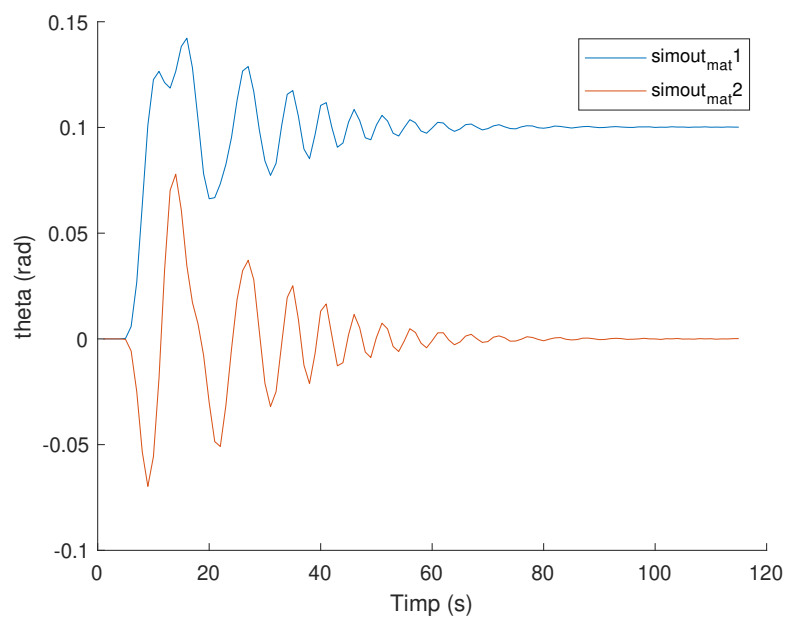


Figure 3: Sistemul MIMO

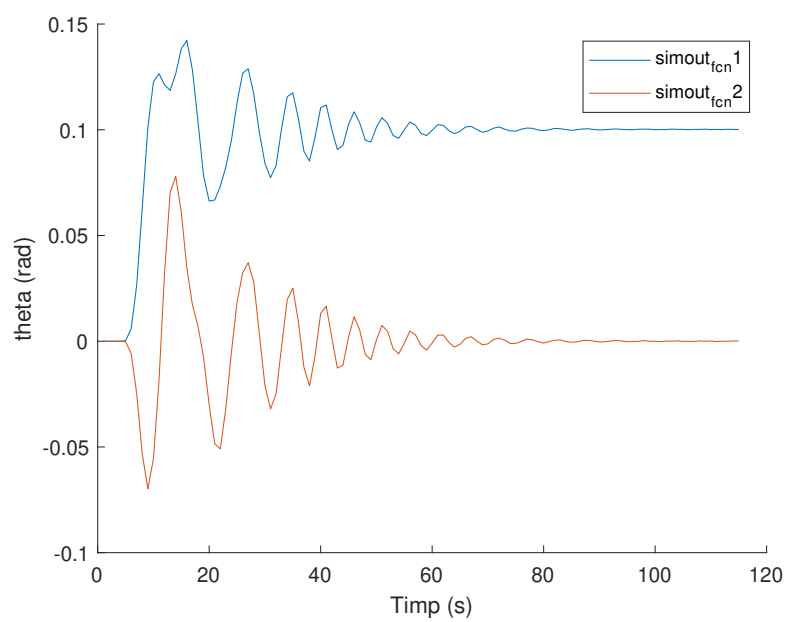


Figure 4: Sistemul SISO

Observam ca iesirile sunt identice chiar daca folosim blocul cu o intrare si o iesire in comparatie cu blocul ce accepta mai multe intrari si mai multe iesiri.

Cerinta 4

```
err1 = norm(simout_mat1 - squeeze(simout_fcn1),2 );  
err2 = norm(simout_mat2 - squeeze(simout_fcn2),2 );
```

Asteptarile mele erau sa fie cel putin o diferenta infima intre iesirile respective dar vad conform $err1 = 0$ si $err2 = 0$ ca nu exista nicio diferenta intre cele doua implementari. Cred ca acest lucru se intampla deoarece multiplexorul si demultiplexorul sunt ideale, astfel nu exista nici-o intarziere in a selecta canalul dorit si a citi valoarea de pe acel fir.

Cerinta 5 & 6

```
ustar = [0.1 ;0.5;0.82; 1;1.5; 1.8; 2 ; 2.8; 3.1;3.6;4;4.5;10];% luam puncte random  
p1 = polyfit(ustar,y1star,1); % polinomul ce trece cel mai aproape de punctele mele cele ma  
p2 = polyfit(ustar,y2star,2);  
alfa = 3;  
beta = 7;  
gamma = 11;  
p1alfa = polyval(p1,alfa);  
p2alfa = polyval(p2,alfa);
```

Valorile pentru scalari si a raspunsurilor lor sunt:

```
alfa = 3; p1alfa = 0.150621811592054 p2alfa = -9.362544382551802e-05  
beta = 7; p1beta = 0.356268146304325 p2beta = 0.002418763033055  
gamma = 11; p1gamma = 0.571731077316811 p3gamma = 0.015312791334766
```

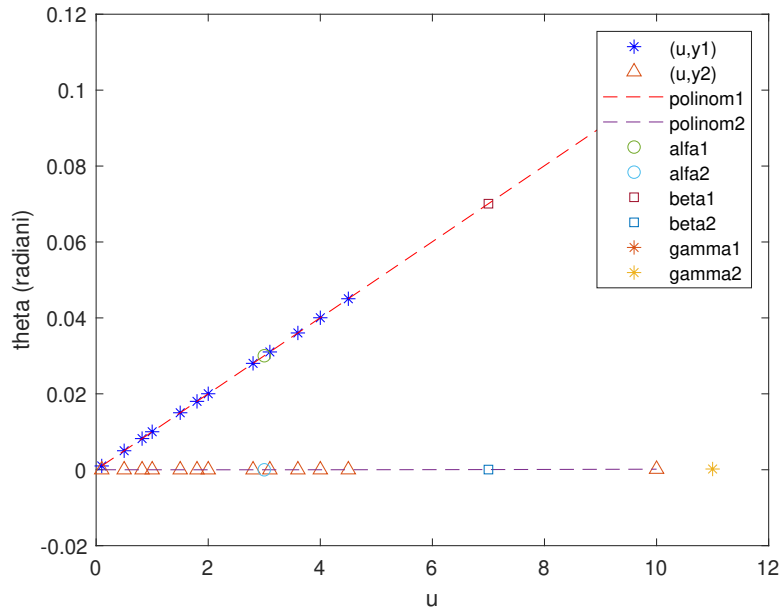


Figure 5: Caracteristica statica

Cerinta 7

Am construit un model separat

```
mdl_pin = 'penduldublu_pin';
```

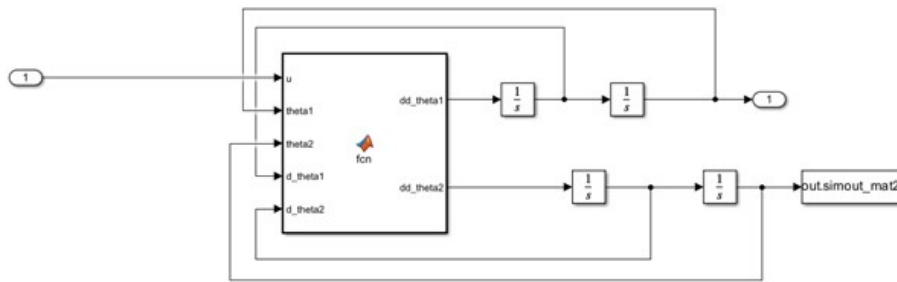


Figure 6: Schema model cu pini IN & OUT

Cerinta 8

```
u0 = 17;  
iu = length(u0);  
  
[xstar,ustar,y2star,~] = trim mdl_pin,[],u0,[],[],iu,[];  
  
erru = abs(ustar-u0);
```

Cerinta 9

```
[A_lin,B_lin,C_lin,D_lin] = linmod mdl_pin, xstar, ustar);
```

Cerinta 10

```
vp = eig(A_lin);% este stabil deoarece are 2 perechi de valori proprii complex conjugate in  
stabil = -1;  
for i = 1:size(vp)  
    if (real(vp(i)) > 0)  
        stabil = 0;  
        disp("sistem instabil");  
        break;  
    else  
        stabil = 1;  
    end  
end  
if(stabil == 1)  
    disp("Sistem STABIL");  
end
```

Sistem STABIL

Cerinta 11

```
mdl_liniarizat = 'penduldublu_liniarizat';  
r1 = 1.5.*double(t>=0);  
usim = timeseries(r1,t);  
set_param(mdl_liniarizat,'StopTime',num2str(Tmax));
```

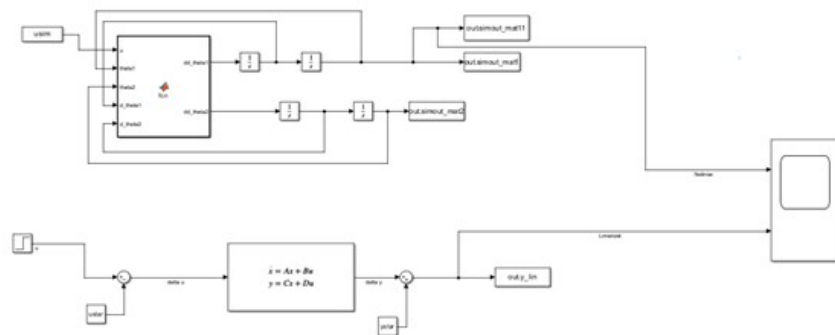


Figure 7: Schema pentru Liniarizare

Cerinta 12

```
y_nl = out1.simout_mat11; %116 linii
err5 = norm(y_nl.Data - y_lin.Data, 'inf')
```

err5 =

0.0032

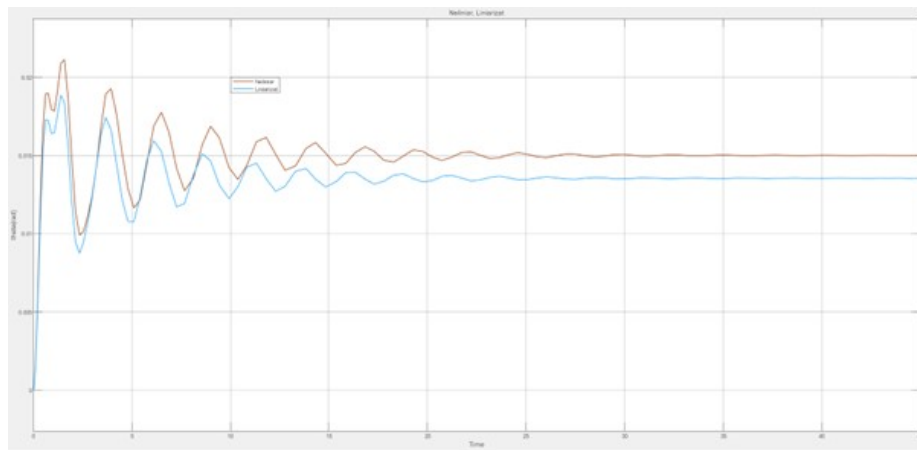


Figure 8: Grafic raspuns neliniar vs liniar

Cerinta 13

```
lin_model = ss(A_lin,B_lin,C_lin,D_lin);
```



```

Te = 0.07;
model_discretizat = c2d(lin_model,Te,'tustin');
isstable(model_discretizat)

```

cu tustin stabilitatea se pastreaza dar planul stabil se muta in discul unitate

Cerinta 14

Ecuatiile cu diferente sunt:

$$\begin{aligned}
 y_k = & 3.669302429617090*y_{k1} - 5.211069534922971*y_{k2} + \dots \\
 & 3.397234082780038*y_{k3} - 0.860313236420063*y_{k4} + \dots \\
 & 0.000238988402665551*uk + 0.000024589213779549*uk1 - \dots \\
 & 0.000441092984659992*uk2 + 3.609e-15*uk3 + 0.000226693795777581*uk4;
 \end{aligned}$$

Cerinta 15

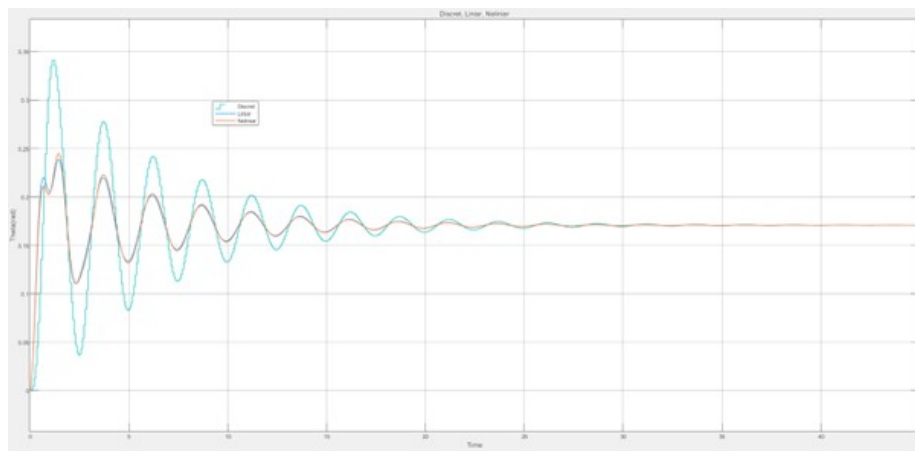


Figure 9: Discret vs neliniar vs liniar