Subject: Engineering Mathematics Chapter: Numerical Methods

Topic : Numerical Solution of Algebraic & Transcendental equations

- 1. In the interval $[0, \pi]$ the equation $x = \cos x$ has
 - (a) No solution
 - (b) Exactly one solution
 - (c) Exactly Two solution
 - (d) An infinite number of solution
- 2. The Newton-Raphson method is used to find the root of the equation $x^2 2$. If the iterations are started from -1, then the iteration will-
 - (a) converge to -1
 - (b) converge to $\sqrt{2}$
 - (c) converge to $-\sqrt{2}$
 - (d) not converge
- 3. The equation $x^3 x^2 + 4x 4 = 0$ is to be solved using the Newton-Raphson method. If x = 2 is taken as the initial approximation of the solution, the next approximation using this method will be-
 - (a) $\frac{2}{3}$
- (b) $\frac{4}{3}$
- (c) 1
- (d) $\frac{3}{2}$
- **4.** Consider the series $X_{n+1} = \frac{x_n}{2} + \frac{9}{8x_n}$, $x_0 = 0.5$ obtained

from the Newton-Raphson method. The series converges to-

- (a) 1.5
- (b) $\sqrt{2}$
- (c) 1.6
- (d) 1.4
- **5.** Equation $e^x-1 = 0$ is required to be solved using Newton's method with an initial guess $x_0 = -1$. Then, after one step of Newton's method, estimate x_1 of the solution will be given by
 - (a) 0.71828
- (b) 0.36784
- (c) 0.20587
- (d) 0.00000

- **6.** The real root of the equation $xe^x = 2$ is evaluated using Newton-Raphson's method. If the first approximation of the value of x is 0.8676, the 2^{nd} approximation of the value of x correct to three decimal places is-
 - (a) 0.865
- (b) 0.853
- (c) 0.849
- (d) 0.838
- 7. The square root of a number N is to be obtained by applying the Newton-Raphson iterations to the equation $X^2 N = 0$. If i denotes the iteration index the correct iterative scheme will be-

(a)
$$X_{i+1} = \frac{1}{2} \left(X_i + \frac{N}{X_i} \right)$$

(b)
$$X_{i+1} = \frac{1}{2} \left(X_i^2 + \frac{N}{X_i^2} \right)$$

(c)
$$X_{i+1} = \frac{1}{2} \left(X_i^2 + \frac{N^2}{X_i} \right)$$

(d)
$$X_{i+1} = \frac{1}{2} \left(X_i - \frac{N}{X_i} \right)$$

- **8.** How many distinct values of x satisfy the equation sin(x) = x/2, where x is in radians?
 - (a) 1
- (b) 2
- (c) 3
- (d) 4 or more
- **9.** Only one of the real roots of $f(x) = x^6 x 1$ lies in the interval $1 \le x \le 2$ and bisection method is used to find its value. For achieving an accuracy of 0.001, the required minimum number of iterations is _____.
- 10. What is value of $(1525)^{0.2}$ to 2 decimal places?
 - (a) 4.33
- (b) 4.36
- (c) 4.38
- (d) 4.30

Answer Key

1. (b)

2. (c)

3. (b)

4. (a)

5. (a)

6. (b)

7. (a)

8. (c)

9. (10)

10. (a)







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