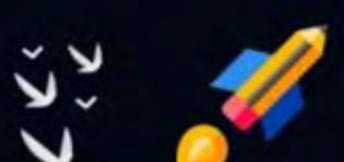
# CS & IT ENGINEERING Algorithms

Analysis of Algorithms



## Recap of Previous Lecture







## **Topics to be Covered**











**Topics** 

**Asymptotic Notations** 

Little Oh, Little Omega

**Properties of ASN** 

**Problem Solving** 





$$\text{NB}$$
) Big-oh:  $f(n)$  is  $O(g(n)) \Longrightarrow f(n) \leq C \cdot g(n)$  whenever  $n \geq n_0$ ;

13 2) Big-omega (-2): 
$$f(n)$$
 is  $-22(5(n))$  if  $f(n) \ge -5(n)$ .

Tight 3) Theta (0):  $f(n)$  is  $O(5(n))$  if  $n \ge n$ .

Sound

(m) (m) f (m) f





=> 3maller functions are in the order of Bosser function

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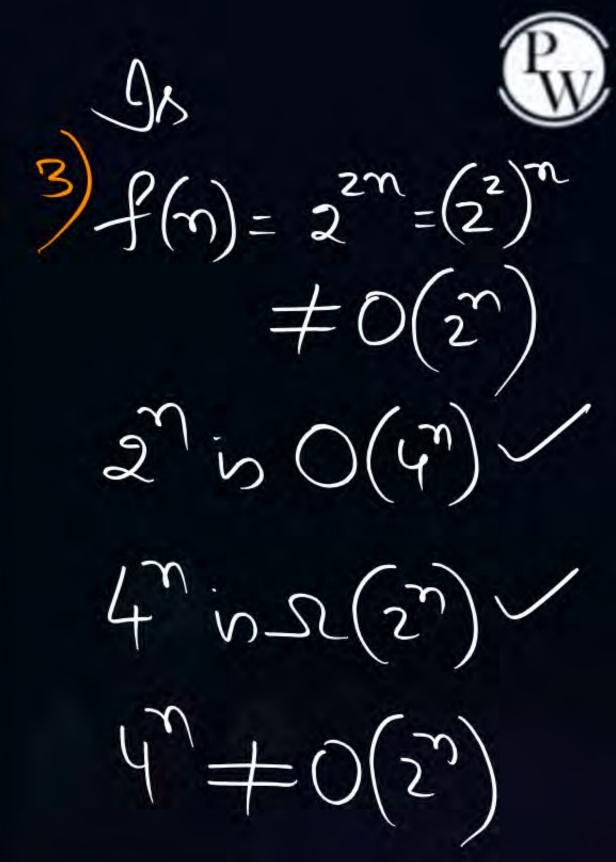
En: 2 < 23

=> If the rate of Growth of 138th the functions are equal, then they are that of each other;



1) 
$$f(n) = 2 \log_{z}^{n} = 0 (m)$$
  
=  $n \log_{z}^{2} = n =$ 

$$\frac{1}{2} \int_{-\infty}^{\infty} f(x) = \frac{1}{2} \int_{-\infty}^{\infty} \frac{1}$$





$$95 = 0(2^{n})$$
 $2^{n+1} = 0(2^{n})$ 
 $2^{n} = 0(2^{n})$ 

$$m = 2$$

$$f(n) = n = (value)$$

$$= \left(\frac{\log n}{2}\right) \frac{1}{\log n}$$

$$= 2 = 2 (c)$$

$$= 0 (1)$$

$$-\int (m) = \frac{1}{2} \sqrt{6} \sqrt{n} = x$$

$$= \frac{1}{2} \sqrt{6} \sqrt{6} \sqrt{n} = x$$

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$$= \frac{1$$







$$C = b$$

$$C = b$$

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f(m) = Logn < 5	(m)= Jm
	Log In
	Log m/2
Log Log	1. Cos(m)





$$f(n) = \frac{1}{m}$$

$$f(n)$$





$$f(n) = n^{2} < g(n) = n^{3}$$

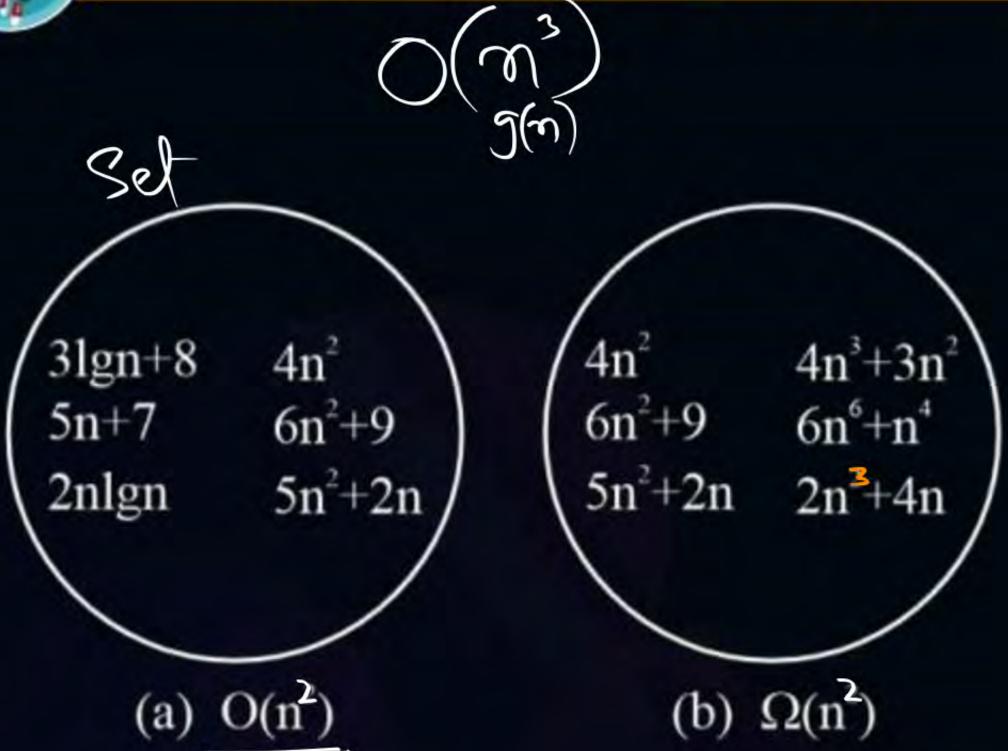
$$2 \log n$$

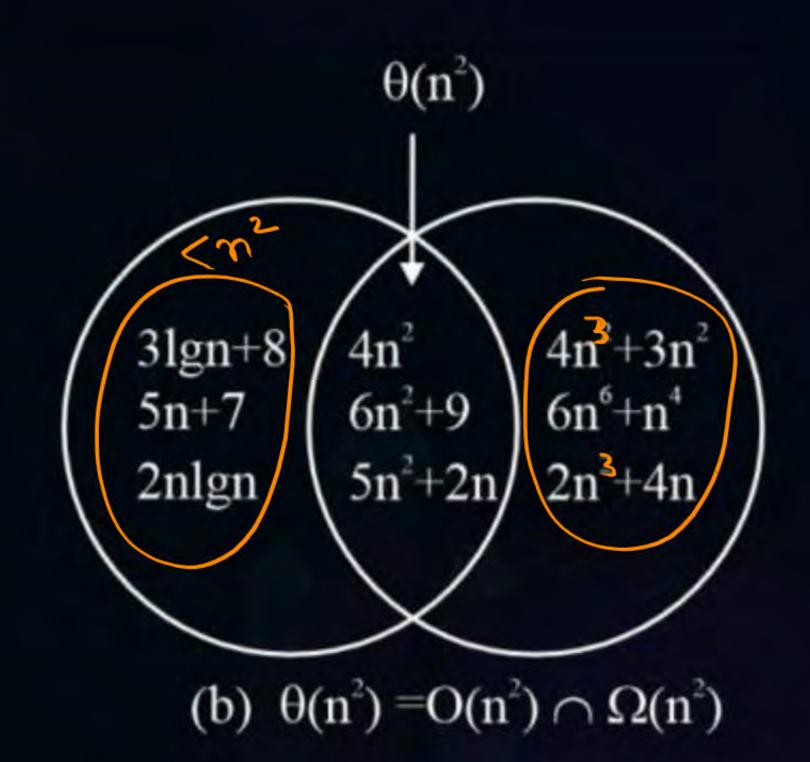
$$\sqrt{2 \log n}$$



#### **Topic: Time Complexity**







Note:- The set  $O(n^2)$ ,  $\Omega(n^2)$ ,  $\Theta(n^2)$ . Some exemplary member are shown.



#### **Topic: Exponentials**



For all real a > 0, m, n

$$a^{-1} = 1/a$$

$$(a^m)^n = a^{mn}$$

$$(a^{m})^{n} = (a^{n})^{m}$$

$$a^m \cdot a^n = a^{m+n}$$



#### **Topic: Analysis of Algorithms**

$$\log x^y = y \log x$$

$$\log xy = \log x + \log y$$

$$\log \log n = \log(\log n)$$

$$a^{\log_b^x} = x^{\log_b^a}$$

$$\log n = \log_{10}^{n}$$

$$\log^{k} n = (\log n)^{k}$$

$$\log \frac{x}{y} = \log x - \log y$$

$$\log_b^x = \frac{\log_a^x}{\log_a^b} = \frac{\log_a^x}{\log_a^b}$$





$$a = b^{\log_b a} \qquad a^{\log_b b} = a^{\log_b a}$$

$$\log_c (ab) = \log_c a + \log_c b$$

$$\log_b a^n = n \cdot \log_b a$$

$$\log_b a = \frac{\log_c a}{\log_c b}$$

$$\log_b^{1/a} = -\log_b a \qquad \log_b a$$

$$\log_b a = \frac{1}{\log_a b}$$

$$a^{\log_b c} = \log_b a$$



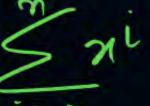
#### Topic: Geometric Sum Formula



1. The geometric sum formula for finite terms is given as:

if 
$$r = 1$$
,

$$S_n = n*a$$



if 
$$|r| < 1$$
,  $S_n = \frac{a(1-r^n)}{1-r}$ 

if 
$$|r| > 1$$
,  $S_n = \frac{a(r^{n-1})}{r-1}$ 

$$\frac{2}{5} \frac{1}{2^{i}} = \frac{1}{2^{i}} \frac{1}{2^{i}} = \frac{1}{2^{i}}$$

$$= \frac{1}{2^{i}}$$

$$= \frac{1}{2^{i}}$$

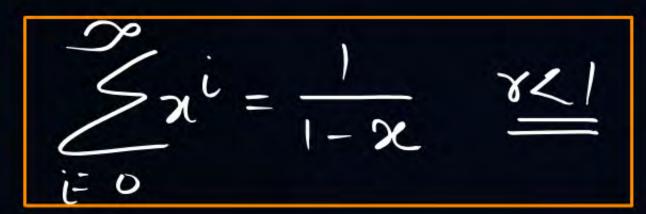
Where

- a is the first term
- r is the common ratio
- n is the number of terms

$$\sum_{i=1}^{n} \frac{1}{2^{i}} = 2(\frac{n}{2^{i}-1}) = \frac{n+1}{2^{i}-2}$$



#### **Topic: Geometric Sum Formula**





2. The geometric sum formula for infinite terms is given as:

if 
$$|r| < 1$$
,  $S_{\infty} = \frac{a}{1-r}$ 

If |r| > 1, the series does not converge and it has no sum.



#### **Topic: Analysis of Algorithms**



#### Airthmetic series

$$\sum_{k=1}^{n} k = 1 + 2 + ... + n = \frac{n(n+1)}{2}$$

#### Geometric series

$$\sum_{k=0}^{n} x^{k} = 1 + x + x^{2} \dots + x^{n} = \frac{x^{n+1} - 1}{x - 1} (x \neq 1)$$

#### Harmonic series

$$\sum_{k=1}^{n} \frac{1}{k} = 1 + \frac{1}{2} + \dots + \frac{1}{n} \approx \log n$$

Harmonic series
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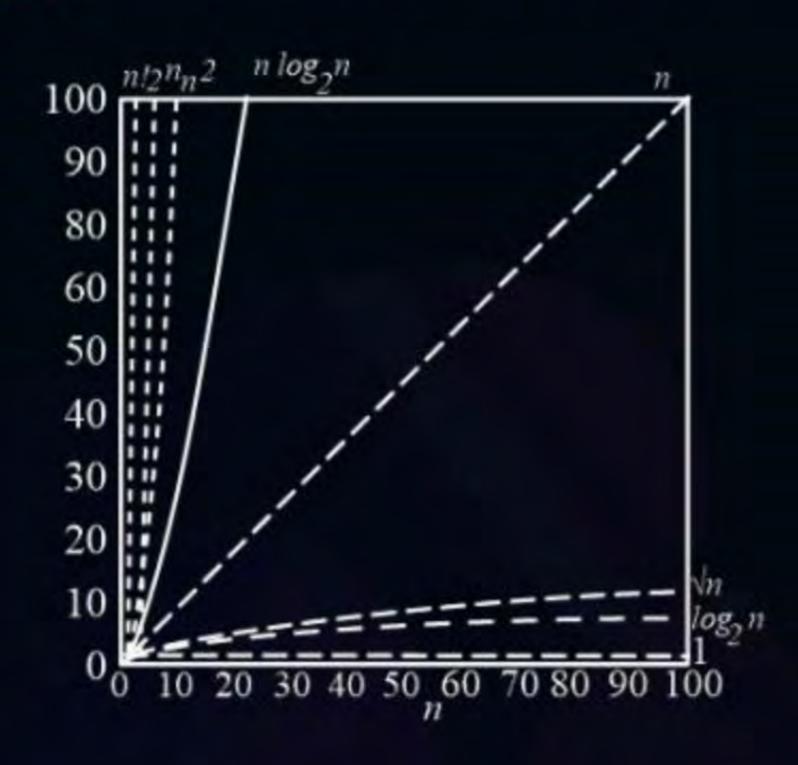
Dominance Relation
Constants < Logarithms < Poly < Preponential

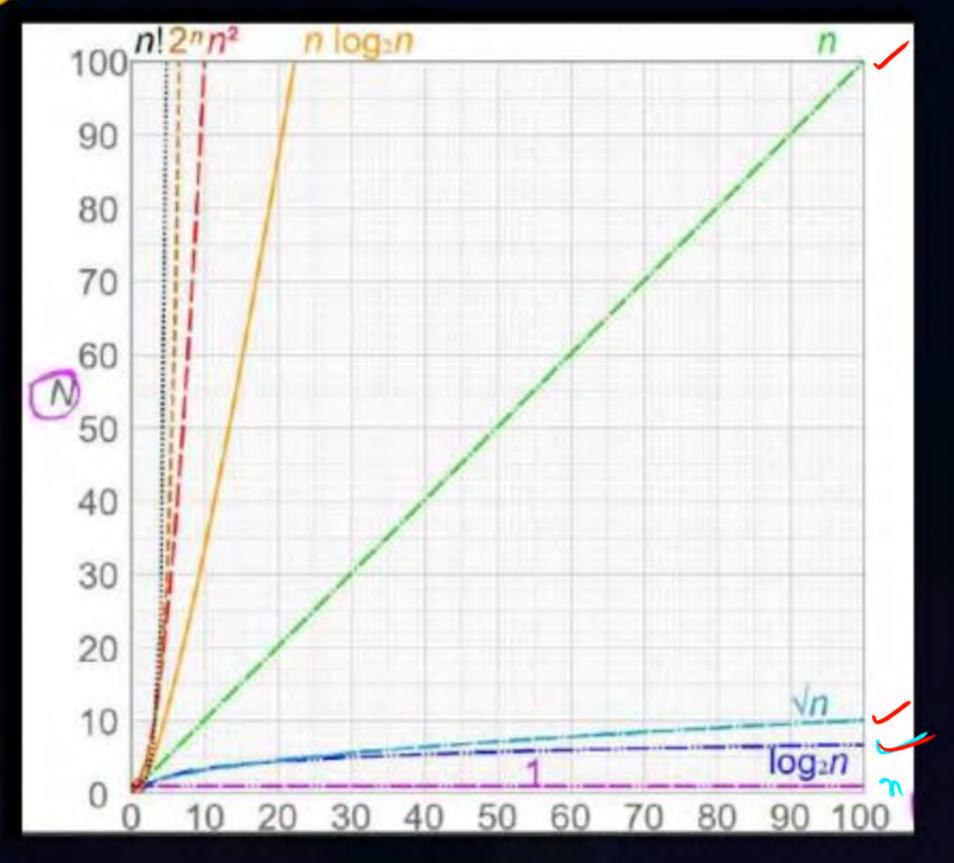
C < fogn < In < m < m fogn < m < m > m



#### **Topic: Analysis of Algorithms**







1) 
$$f(m) = \sum_{i=1}^{\infty} 1 = m = O(m) /$$

2) 
$$f(n) = \sum_{i=1}^{\infty} n = n \cdot \sum_{i=1}^{\infty} 1 = n \cdot n = O(n^2)$$

3) 
$$f(\eta) = \sum_{i=1}^{\infty} = \frac{\eta(\eta + i)}{2} = O(\eta^2)$$

4) 
$$f(n) = \sum_{i=1}^{2} \frac{1}{2} = \frac{O(u_{i})(u_{i})(u_{i})}{6}$$

5) 
$$f(n) = \sum_{i=1}^{3} = \left(\frac{n(n+i)}{2}\right)^{2} = O(n^{4})$$

2) 
$$f(n) = \sum_{i=1}^{\infty} n = n \cdot \sum_{i=1}^{\infty} 1 = m \cdot n = O(n^2)$$
 6)  $f(n) = \sum_{i=1}^{\infty} i = (2^{n+1}z) = O(2^n)$ 

$$f(n) = \frac{1}{2} \frac{1}{2} = (-\frac{1}{2}) = O(1)$$

8) 
$$f(n) = \frac{3}{5}i_{2}i_{2}i_{2} = (n-1)\cdot 2^{n+1} + 2$$

$$(n.2^{-1})$$
  $(n.2^{-1})$   $(n.2^{-1})$ 

9) 
$$f(m) = \tilde{f}_{i=1} = O(1)$$

$$| (n) - (n) = \frac{\pi}{n} i = (1.2.3. \quad m) = m! = m \cdot (m-1)(m-2) \cdot \dots \cdot 1$$

$$f(n) = \sum_{i=1}^{n} bogi$$

$$n = n(n-1)(n-2) \cdot A \times n \cdot n \cdot n$$

$$m : \langle m \rangle O(n)$$
 Boxes

$$\int_{\mathcal{S}} u = \mathcal{L}(u)$$

$$mi + Cr(w)$$

$$rac{1}{2}$$
  $rac{1}{2}$   $rac{1}{2}$   $rac{1}{2}$ 

$$f(n) = \sum_{i=1}^{\infty} \log i = \log 1 + \log 2 + \dots + \log n = \log (12.3..n)$$

$$= \log (n!)$$

$$= \log$$

2) 
$$\log n! = \sum_{i=1}^{\infty} \log_{i} n$$

3)  $\sum_{i=1}^{\infty} \log_{i} = \log_{i} + \log_{i} 2 + \dots + \log_{i} n$ 

1)  $\log_{i} + \log_{i} - 1 + \log_{i} n - 2 + \dots + \log_{i} n$ 
 $\leq (\log_{i} + \log_{i} n + \log_{i} n)$ 
 $\leq n \cdot \log_{i} n + \log_{i} n - 2 + \dots + \log_{i} n + \log_{i}$ 

$$\int_{1}^{\infty} \log x \cdot dx = \left[x(\log x - 1) + c\right]^{n}$$

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$$n! < m^n = 0 (m)$$

$$Losn! = 0 (m) Losn)$$

$$f(m) = \frac{\pi}{5i^{1/2}} = 0($$



# THANK - YOU