Subject: Engineering Mathematics Chapter: Probability

DPP-08

Topic: Mean, Median & Mode

- 1. The standard deviation for the data 7, 9, 11, 13, 15 is
 - (a) 2.4
- (b) 2.5
- (c) 2.7
- (d) 2.8
- **2.** Consider the continuous random variable with probability density function

$$f(t) = 1 + t \text{ for } -1 \le t \le 0$$

$$= 1 - t$$
 for $0 \le t < 1$

The standard deviation of the random variable is

- (a) $\frac{1}{\sqrt{3}}$
- (b) $\frac{1}{\sqrt{6}}$
- (c) $\frac{1}{3}$
- (d) $\frac{1}{6}$
- **3.** Let X and Y be two independent random variables. Which one of the relations between expectation (E), variance (Var) and covariance (Cov) given below is FALSE?
 - (a) E(XY) = E(X) E(Y)
 - (b) Cov(X, Y) = 0
 - (c) Var(X + Y) = Var(X) + Var(Y)
 - (d) $E(X^2Y^2) = (E(X))^2 (E(Y))^2$
- **4.** In the following table, x is a discrete random variable and p(x) is the probability density. The standard deviation of x is

X	1	2	3
p(x)	0.3	0.6	0.1

- (a) 0.18
- (b) 0.36
- (c) 0.54
- (d) 0.6
- **5.** The probability density function of evaporation E on any day during a year in watershed is given by

$$f(E) = \begin{cases} \frac{1}{5} & 0 \le E \le 5 \text{ mm/day} \\ 0 & \text{otherwise} \end{cases}$$

The probability that E lies in between 2 and 4 mm/day in a day in watershed is (in decimal) _____

6. Let X be a random variable with probability density function

$$f(x) = \begin{cases} 0.2, & \text{for } |x| \le 1 \\ 0.1, & \text{for } 1 < |x| \le 4 \\ 0, & \text{otherwise} \end{cases}$$

The probability P(0.5 < X < 5) is _____.

7. Mark obtained by 100 students in an examination are given in the table

SI. No.	Marks obtained	Number of students
1 /	25	20
2	30	20
3	35	40
4	40	20

What would be the mean, median and mode of the marks obtained by the students?

- (a) Mean 33; Median 35; Mode 40
- (b) Mean 35; Median 32; Mode 40
- (c) Mean 33; Median 35; Mode 35
- (d) Mean 35; Median 32; Mode 35
- **8.** Two random variable x and y are distributed according to

$$f_{x,y}(x,y) = \begin{cases} (x+y), & 0 \le x \le 1, 0 \le y \le 1 \\ 0, & \text{otherwise} \end{cases}$$

The probability $P(x + y \le 1)$ is _____.

Common data question 9-10

Suppose the probability density function of a continuous random variable x is $f(x) = 3x^2$, 0 < x < 1.

9. Find 'a' satisfying the following condition

(A)
$$P[x \le a] = P[x \ge a]$$

10. Find 'b' satisfying the following condition (A) P[x > b] = 0.05



Answer Key

1. (d)

2. (b)

3. (d)

4. (d)

5. (0.4)

6. (0.4)

7. (c)

8. (0.33)

9. (0.795)

10. (0.983)







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