

CS & IT ENGINEERING

Discussion notes

Discrete Mathematics
Mathematical Logic



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TOPICS TO BE COVERED

01 Question

02 Discussion

Q.1

Let $R(x, y, z)$ denote the statement

$"x + y = z"$ $x + y = z$

[MSQ]



Which of the following proposition will evaluate truth value True?

A.

$R(1, +2, =3)$ (\top) ✓
 $x \quad y \quad z$

B.

$R(0, +0, =1)$ (\bot)

C.

$R(1, +1, =2)$ (\top) ✓

D.

$R(2, +3, =4)$ (\bot)

Q.2

Let $p(x)$, $q(x)$ denote the following open statements.

[MCQ]

$p(x): x \leq 3$ $q(x): x + 1$ is odd $D: \mathbb{Z}$.

If the universe consists of all integers, what are the truth values of the following statements?

$S_1: \sim(p(-4) \vee q(-3))$

$S_2: \sim(p(-4) \wedge \sim q(-3))$

$S_1: \text{True,}$

$S_2: \text{False}$

$S_1: \text{False,}$

$S_2: \text{True}$

$S_1: \text{True,}$

$S_2: \text{True}$

$S_1: \text{False,}$

$S_2: \text{False}$

$p(n): n \leq 3$ $q(n): n+1$ is odd.

$p(-4): -4 \leq 3$ $q(-3): -3+1$ is odd.

T.

F

-2 is odd.

Handwritten truth value analysis for S_1 and S_2 using a truth table approach. For $S_1: \sim(p(-4) \vee q(-3))$, $p(-4)$ is T, $q(-3)$ is F, so $p(-4) \vee q(-3)$ is T, and $\sim(p(-4) \vee q(-3))$ is F. For $S_2: \sim(p(-4) \wedge \sim q(-3))$, $p(-4)$ is T, $\sim q(-3)$ is T, so $p(-4) \wedge \sim q(-3)$ is T, and $\sim(p(-4) \wedge \sim q(-3))$ is F.

Q.3

Let $p(x)$, $q(x)$ denote the following open statements.

[NAT]



$$p(x): x+1 > x \quad q(x): x^2 > 0$$

$2+1 > 2$

How many expressions evaluate to True?

I. $\overset{\tau}{p}(3) \vee \overset{\vee}{[q(3) \vee \sim p(3)]} (\tau)$

II. $\overset{\tau}{p}(2) \rightarrow \overset{(\tau \rightarrow \tau) \equiv \tau}{[q(2) \rightarrow p(2)]}$

III. $[p(2) \rightarrow q(2)] \wedge \underline{p(-3)}$

$$(\tau \rightarrow \tau) \wedge \tau \equiv \tau$$

3

Q.4

[MSQ]



Consider the English sentence

"You can not ride the roller coaster ^{$\neg q$} if ^{R} you are under 4 feet tall unless ^{S} you are older than 16 years old". (q, c)

Which of the following correctly represent the logical expression for the sentence?

A.

$$q \rightarrow \sim(r \wedge \sim S)$$

B.

$$(r \vee \sim S) \rightarrow q$$

C.

$$(r \wedge \sim S) \rightarrow \sim q$$

D.

None of these

$$\neg S \rightarrow (\neg q \text{ if } R)$$

$$\neg S \rightarrow (R \rightarrow \neg q)$$

$$S \vee \neg R \vee \neg q$$

$$P \rightarrow q$$
$$q \text{ unless } \neg p$$

$$q \text{ if } p = p \rightarrow q$$

Q.5

[MCQ] 

Let $p(x)$ be the statement

$$"x + 1 > x"$$

Now, consider the truth value of quantification, where the domain consists of all real number.

$$L_1 = \forall x p(x) \quad (\text{F})$$

$$L_2 = \exists x p(x) \quad (\text{T})$$

Which of the following evaluate to True?

A.

L_1 only

B.

L_2 only

C.

Both L_1 and L_2 are True ✓

D.

Neither L_1 nor L_2

