

CS & IT ENGINEERING

Data Structure

Stack and Queues Chapter- 4

Lec- 06



By- Pankaj Sharma sir



TOPICS TO BE
COVERED

Queue-II

Priority Queue

~ A priority is associated with each element.

Emergency (Rs 500)



Rs 200/-

Element with high priority processed first.

Same priority



Doc.

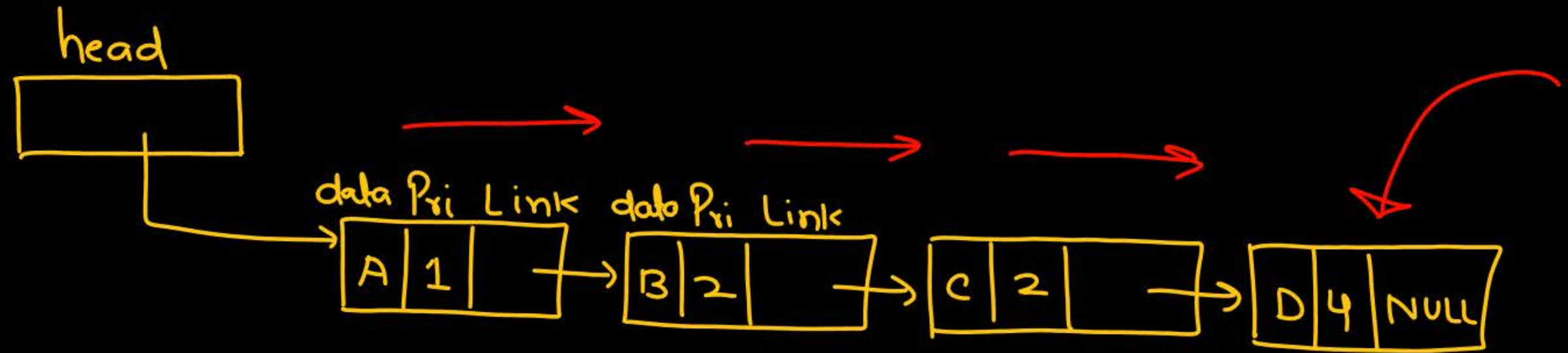


Elements with same priority are pro.
as per their arrival.

Small no \rightarrow High priority ✓

Large no \rightarrow High priority

(E, 2)



B पहले आता है।

✓ A Priority Queue Q is used to implement a stack S that stores characters. $\text{Push}(c)$ is implemented as $\text{Insert}(Q, c, k)$, where k is an app. integer key chosen by implementation.

Pop is implemented as $\text{DELETERMIN}(Q)$. For a seq. of operations the key chosen are in :

- A) Non-increasing order.
- B) Non-decreasing order.
- C) strictly-increasing order
- D) strictly-dec. order

1, 2, 3 \rightarrow inc. X

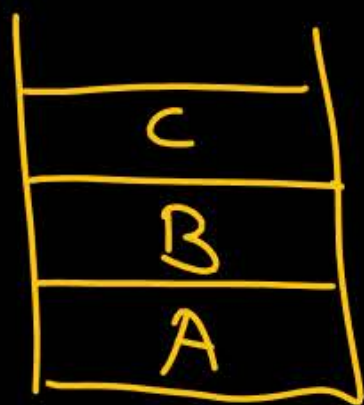
Stack \Rightarrow using a Priority Queue Q

Push('A') \Rightarrow Insert(Q, 'A', 1) $\xrightarrow{\text{key}}$

Push('B') \Rightarrow Insert(Q, 'B', 2) $\xrightarrow{\text{key}}$

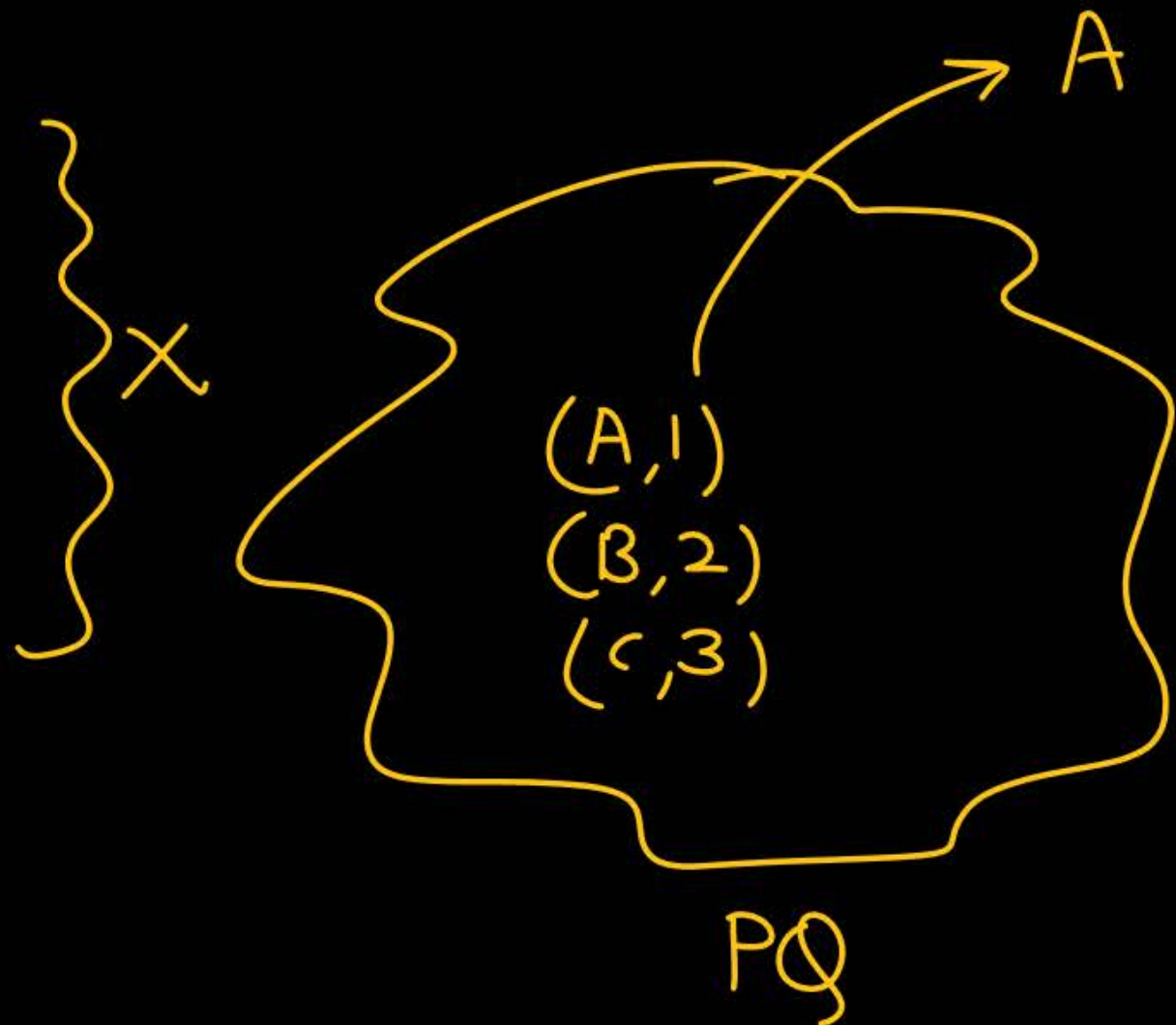
Push('C') \Rightarrow Insert(Q, 'C', 3) $\xrightarrow{\text{key}}$

Pop \Rightarrow DeleteMin(Q)



Pop()
 \Rightarrow C

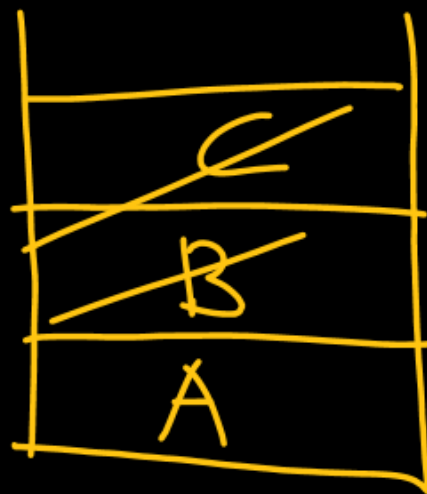
A, B, C \rightarrow



Push('A') \Rightarrow Insert(Q, 'A', 3)

Push('B') \Rightarrow Insert(Q, 'B', 2)

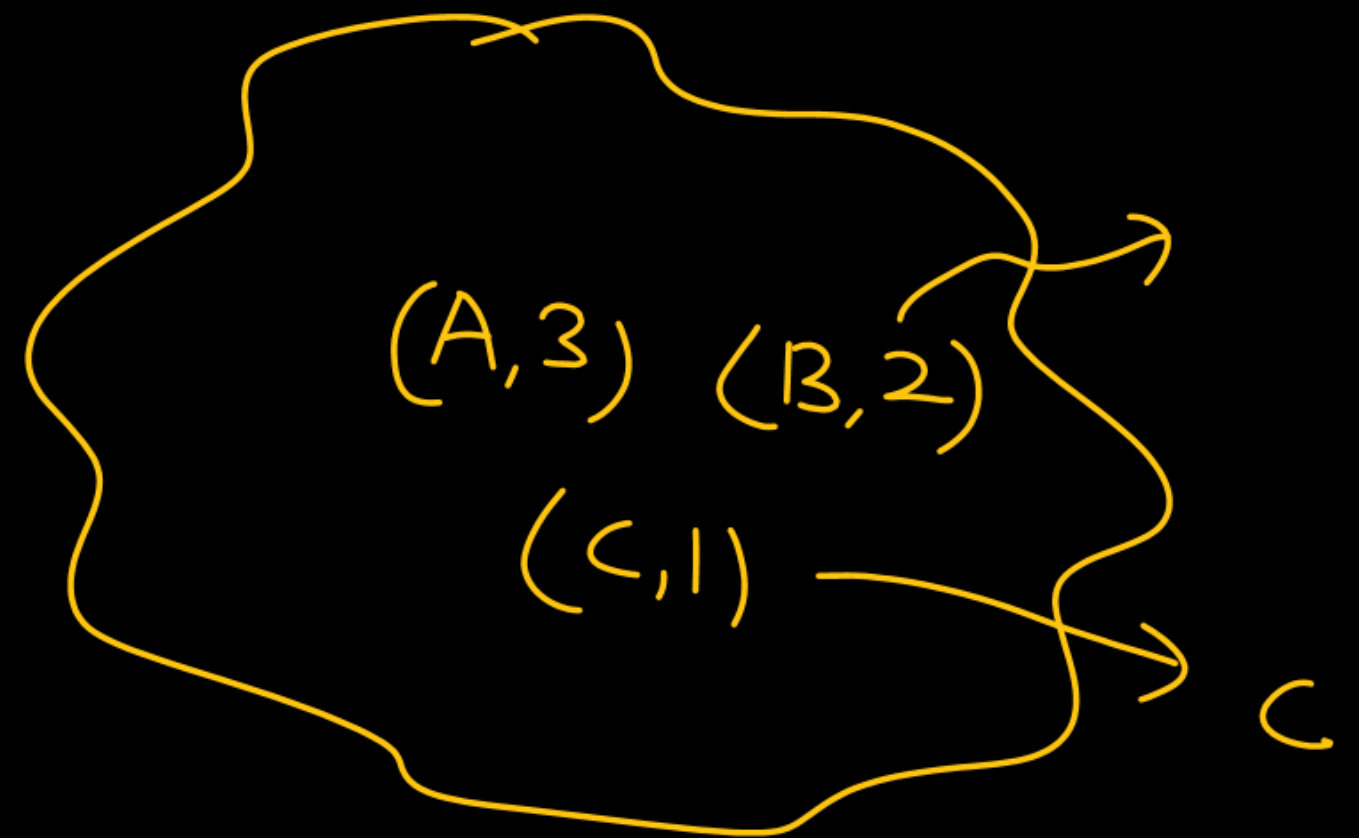
Push('C') \Rightarrow Insert(Q, 'C', 1)



Pop() \Rightarrow C

Pop() \Rightarrow B

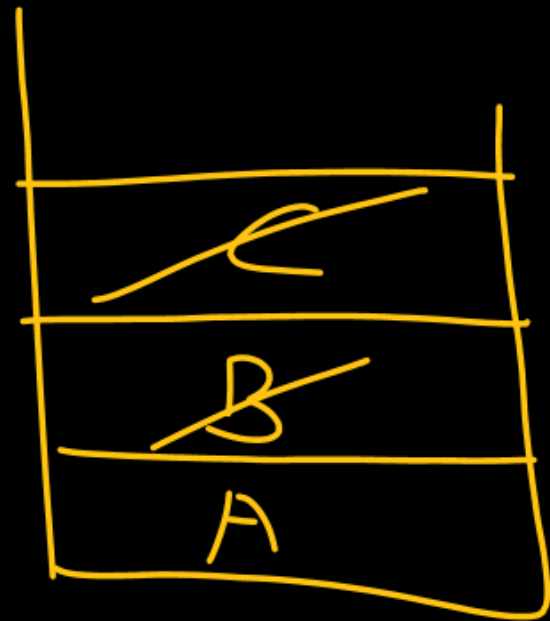
3, 2, 1 \rightarrow



Push('A') \Rightarrow Insert(Q, 'A', 3)

Push('B') \Rightarrow Insert(Q, 'B', 3)

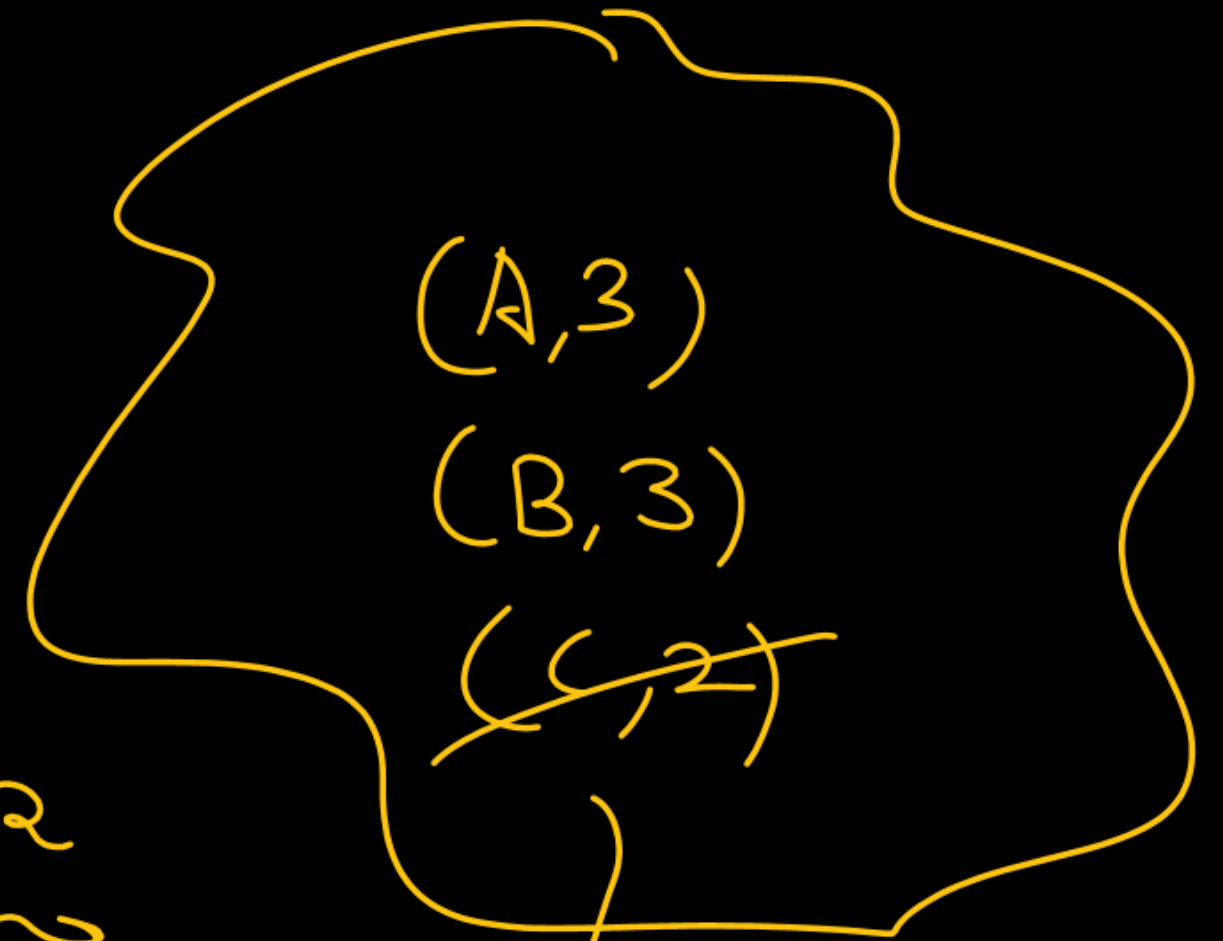
Push('C') \Rightarrow Insert(Q, 'C', 2)



Pop()

Pop()

3, 3, 2



C ✓

Q Gate-2001

What is the min. no. of $\left\{ \begin{array}{c} \text{stacks} \\ \text{of} \\ \text{size } n \end{array} \right\}$ required to implement a queue of size n ?

A) 1

B) 2

C) 3

D) 4

Q

10	20	30	40	50	
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Insert (10)

Insert (20)

Insert (30)

Insert (40)

delete()

→ delete()

Insert (50)

delete

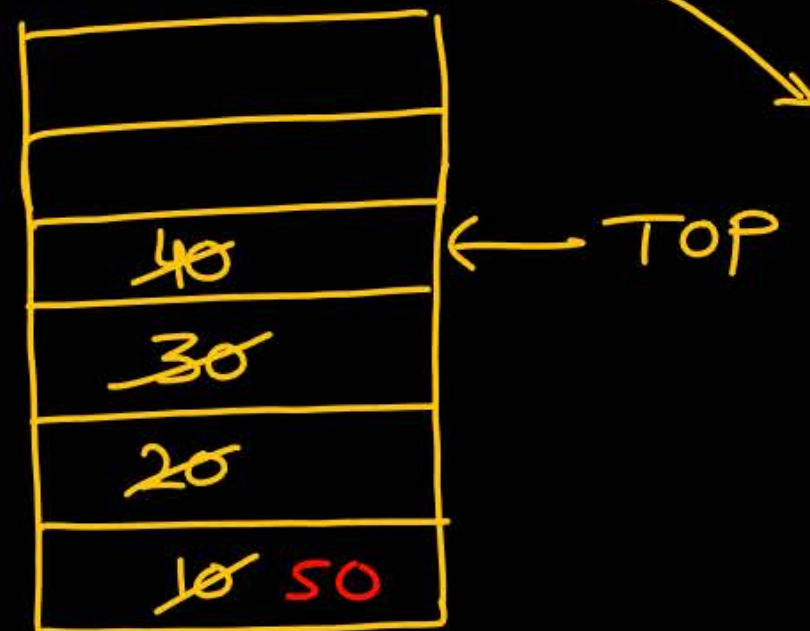
→ 10, 20, 30, 40

~~10~~, 30, 40

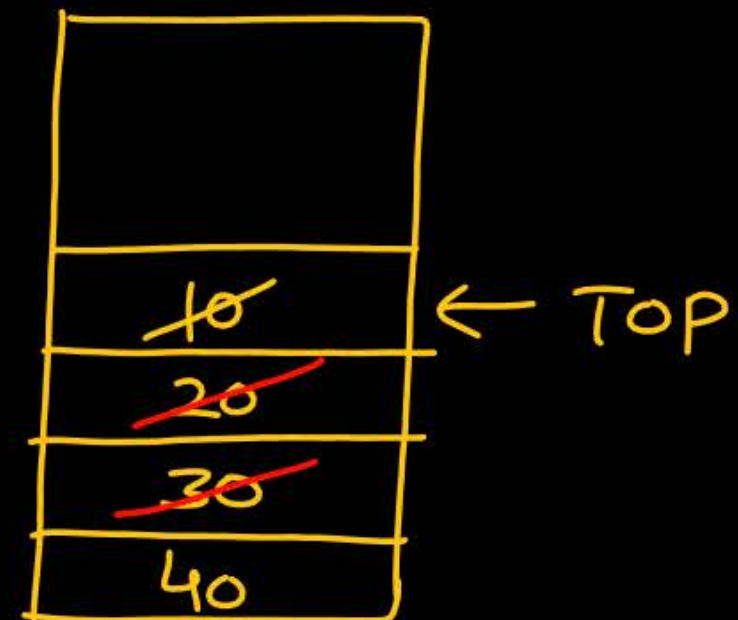
30, 40

30, 40, 50

40, 50



S1 (In)



S2 (out)

Push(10)

Push(20)

Push(30)

Push(40)

delete() ⇒ (i) Move all the elem. from S1 to S2

(ii) Pop() from S2

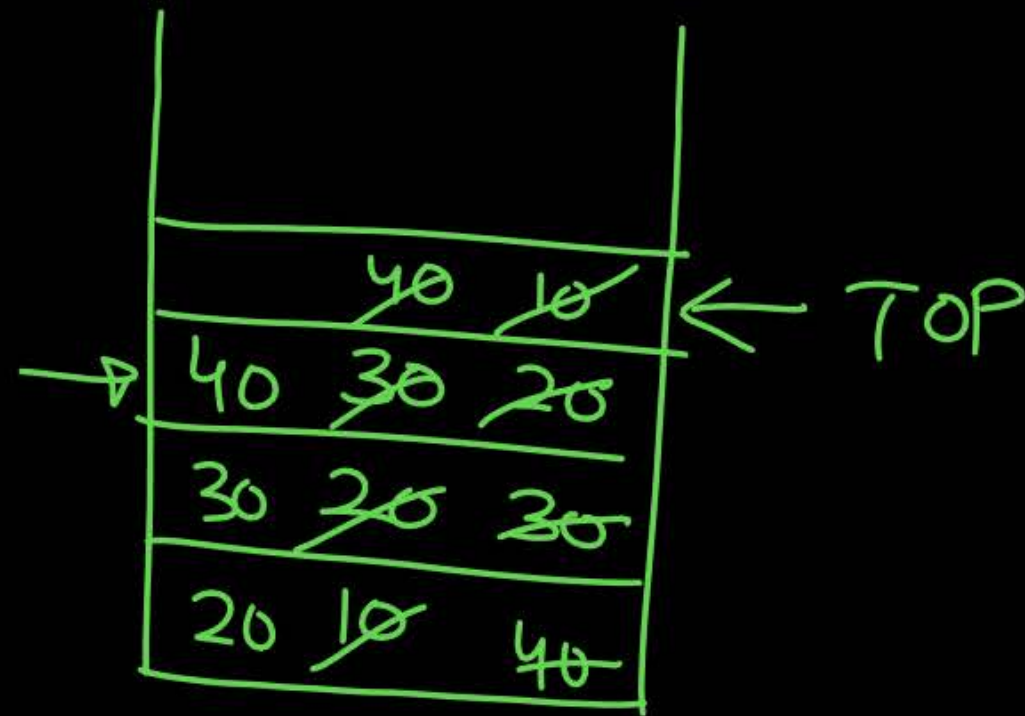
delete ⇒ look at S2, if it is not empty

Magical stack \rightarrow REVERSE op. Support.

Insert \rightarrow Push()

10	20	30	40
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delete 20 30 40



\Rightarrow (i) REVERSE

(ii) Pop()

(iii) REVERSE

Gate 2003

Let S be a stack of size $n \geq 1$ ^{help} starting with empty stack, suppose we push first n natural no. in sequence and then performs n pop operations. Assume push & pop takes X sec. each.

Y sec. elapse b/w the end of one such stack operation and the start of next operation.

For $m \geq 1$, define the stack life of m as the time elapsed from the end of push(m) to the start of pop operation that remove m from S . The avg. stack life of an ele. in stack is:

- A) $n(X+Y)$ ☒
- B) $3Y+2X$ ☒
- ☒ C) $n(X+Y)-X$
- D) $Y+2X$ ☒

$$2(Y+Y)-X = X+2Y$$

Push(1)

Push(2)

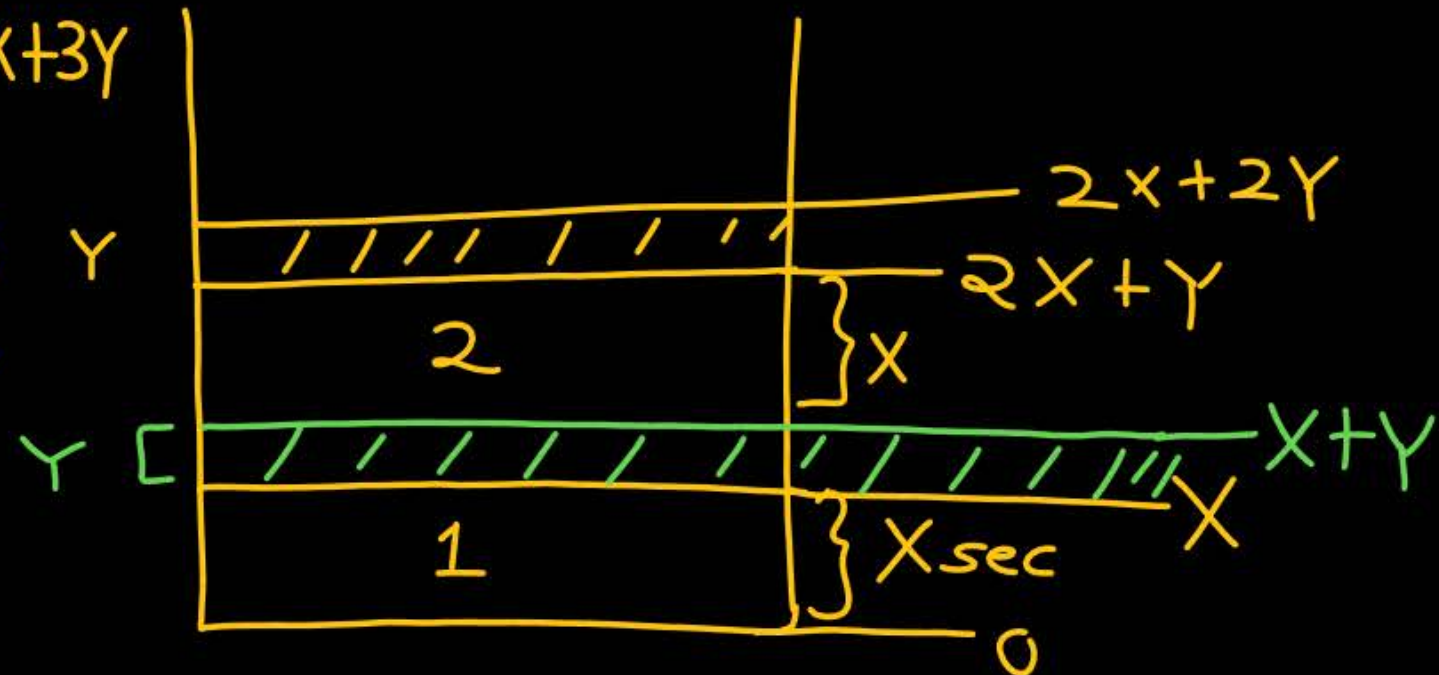
/// Pop()

Pop()

	start Push	End Push	Pop start	Pop End
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1	0	X	$3x+3Y$	$4x+3Y$
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2	$x+Y$	$2x+Y$	$2x+2Y$	$3x+2Y$
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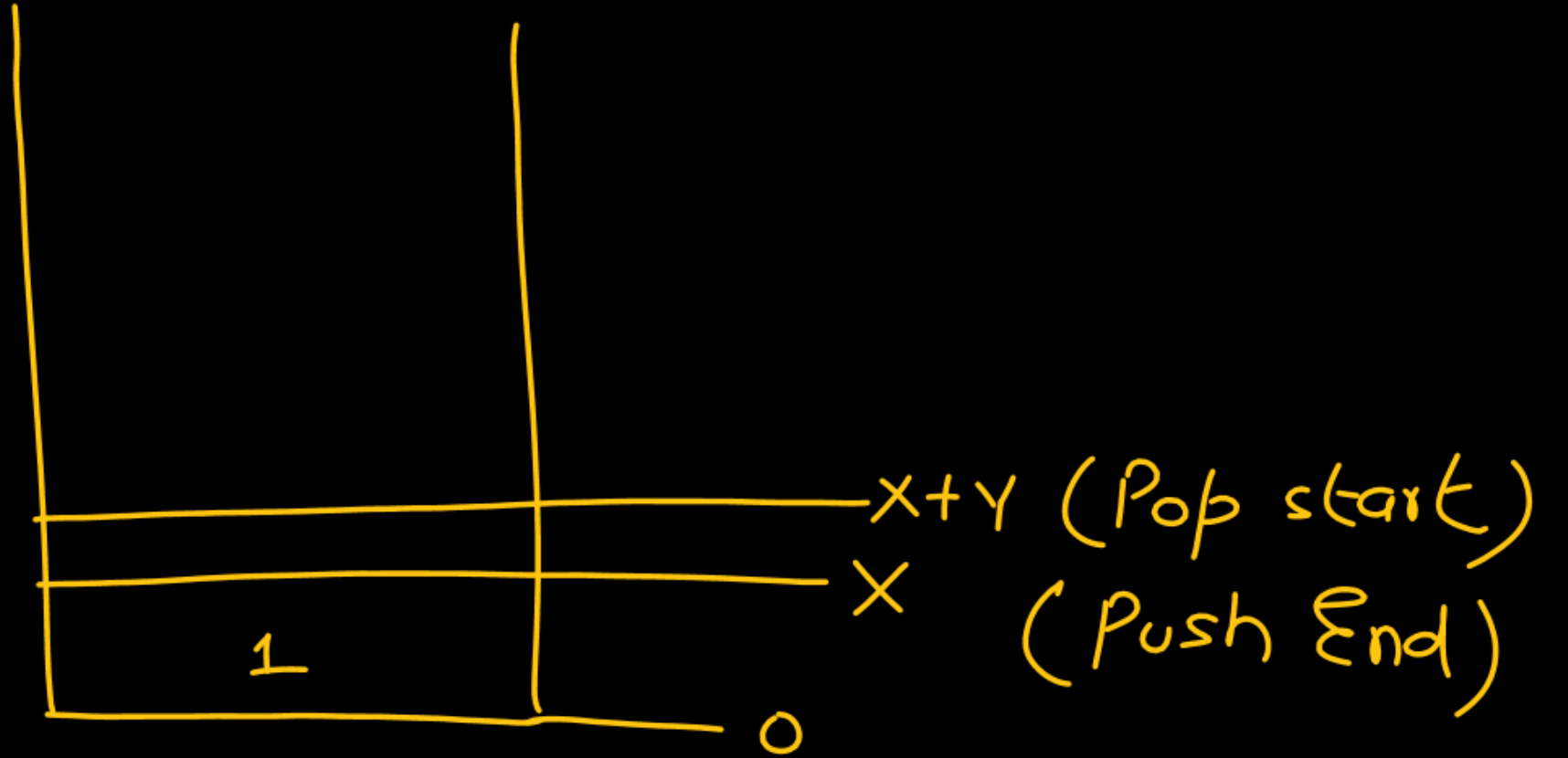
Life time = Pop start - Push end

$$\text{Lifetime}_1 = 2x+3Y$$

$$\text{Lifetime}_2 = Y$$

$$\text{Avg} = \frac{2x+3Y+Y}{2} = x+2Y$$

$$\text{Life time}_1 = (X+Y) - X$$



$$\eta = 1$$

$$(X+Y) - X$$

Gate 2004

A CLL is used to implement a Queue. A single variable P is used to access the queue. To which node should P point such that both enqueue & dequeue can be performed in constant time.

- A) rear node
- B) front node
- C) Not possible
- D) Node next to front

