

CS & IT ENGINEERING

Algorithms

Analysis of Algorithm

Lecture No. - 02

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Sir

Recap of Previous Lecture



Topic

Introduction to Course

Topic

Algorithm Concept

Statements/Steps

Topic

Algorithm Lifecycle Steps

(Fund. Basic opn)

Design & Analysis

Topic

Topic

Topics to be Covered



Topics

Need for Analysis [What & why]

Methodology of Analysis [How]

Types of Analysis





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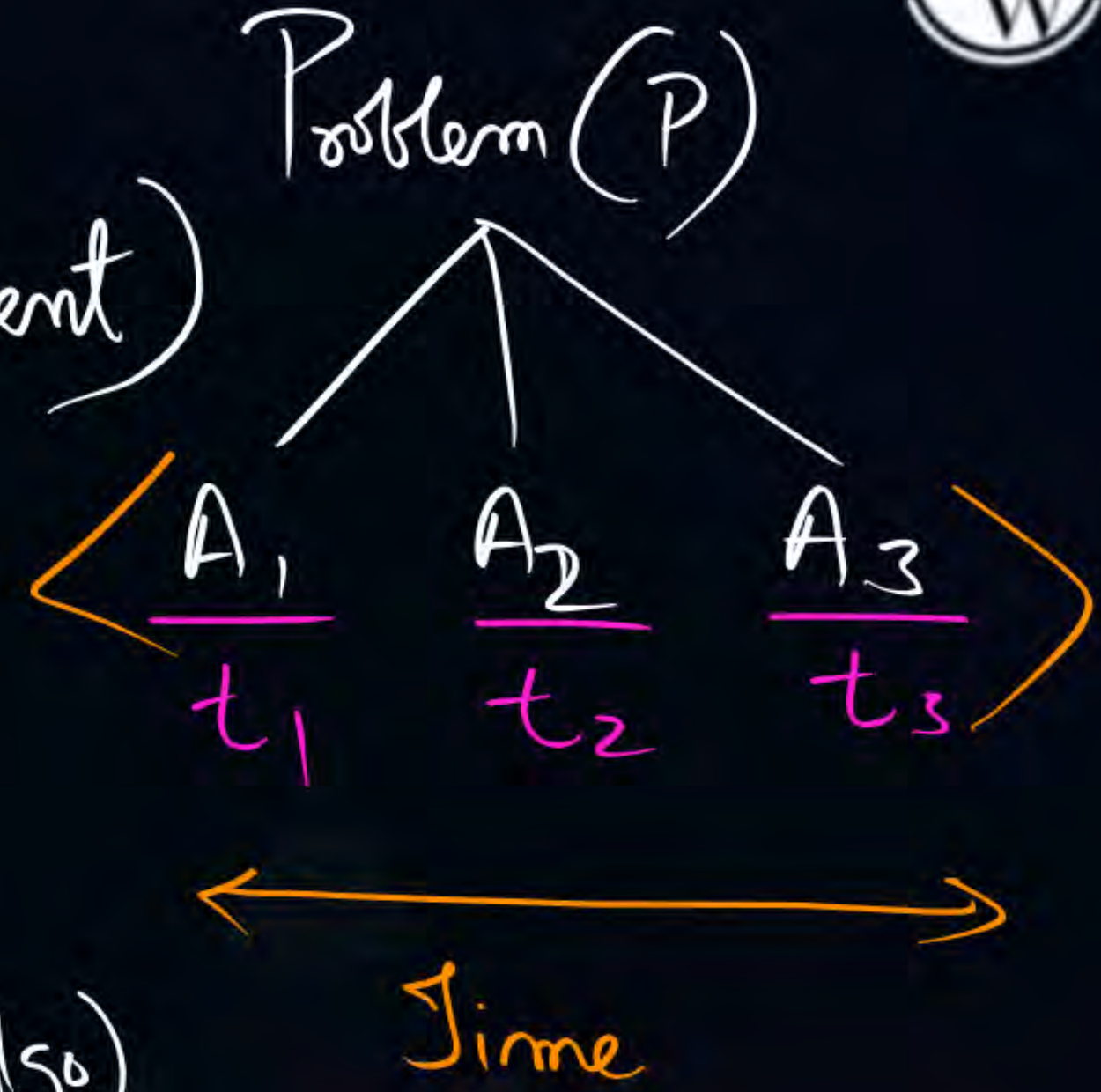
Need for analysis (why?)

1) To determine Resource Consumption
(what)

$\langle \underline{\text{Time}} + \underline{\text{Space}} + \text{Registers} + \text{Cost} + \dots \rangle$
(PC-Domain)

2) Performance ^{Time} Comparison
to find out efficient soln (Also)

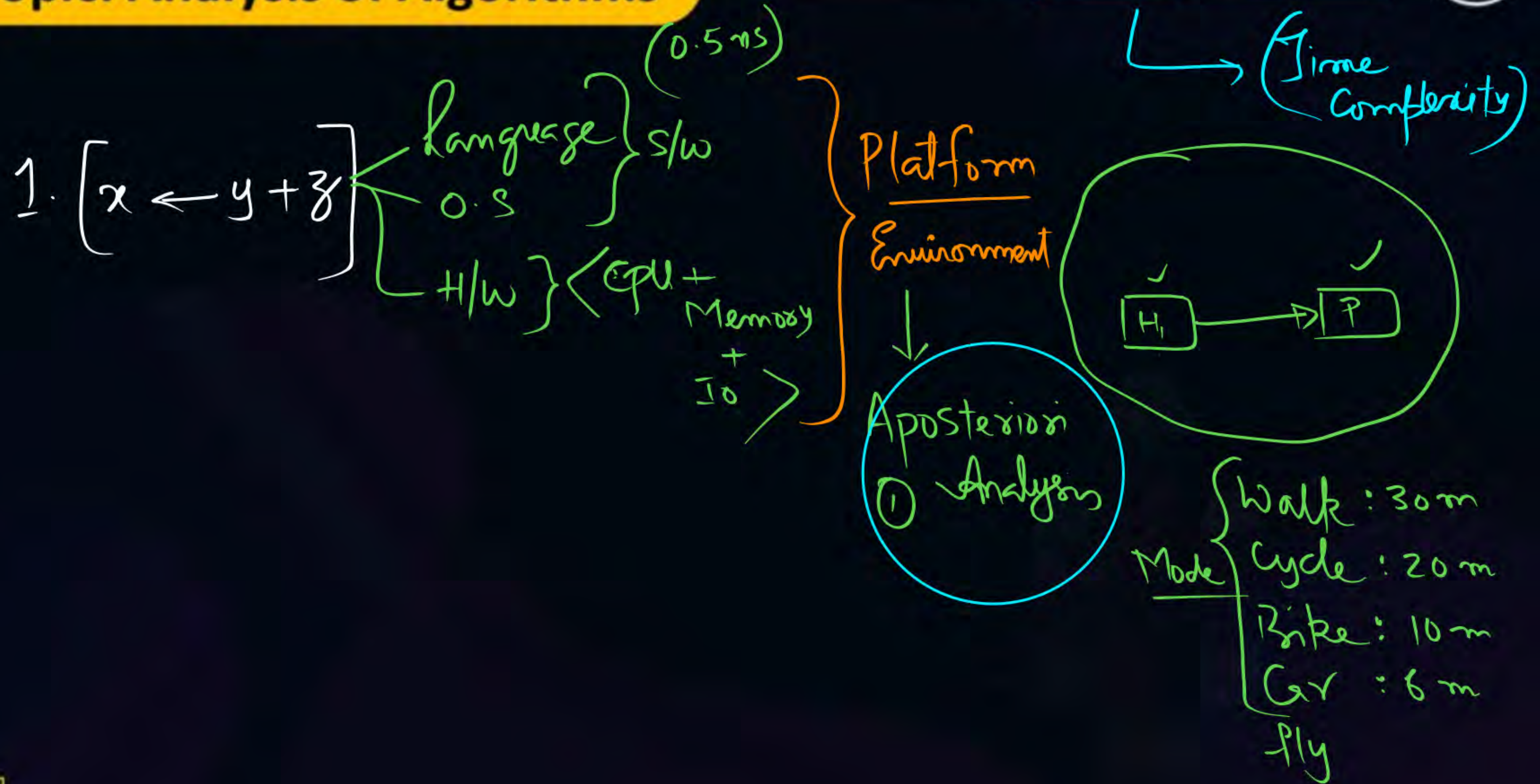
(Efficient)





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Methodology of Analysis (How)



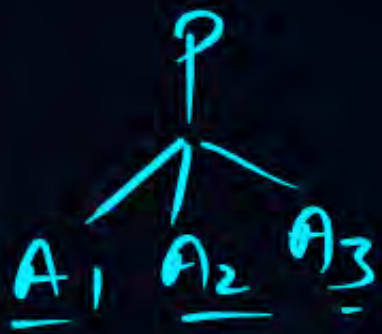


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Aposteriori Analysis [Platform dependent]

h/w
slw



Advantages

- 1) It gives exact values in real units

Drawbacks/Limitation

- 1) It is difficult to carry out; (manual work)
- 2) Cannot consider for all cases of IP's; (Inputs)
- 3) Non-uniformity:

"Performance comparison becomes difficult"



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2) Apriori Analysis



Analytic Framework:

[Platform Independent]

- Take into account all possible IP's;
- Allows us to calculate the relative efficiency (Perf) of Two Algo's in a way that is independent of Platform;
- Can be carried out by studying the high level description of Algorithm without actual Implementation;
- It is easy to carry out;



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Drawback:

- will not give real/actual values in units
- Estimates/Approximates



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Components of Analytic Framework:

- ✓ 1) A language (Pseudo) for describing Algorithm steps.
- ✓ 2) A Computation Model that the Algorithm executes within it;
- ✓ 3) A metric for measuring Algo running time;
- ✓ 4) An approach/Notation to characterize running time,

$a = b + c;$
 $a \leftarrow b + c$



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Algorithm Test

1. $x \leftarrow y + z;$ 2 units (const)

2. $\text{for } i \leftarrow 1 \text{ to } n$
 $\langle a \leftarrow b + c \rangle$

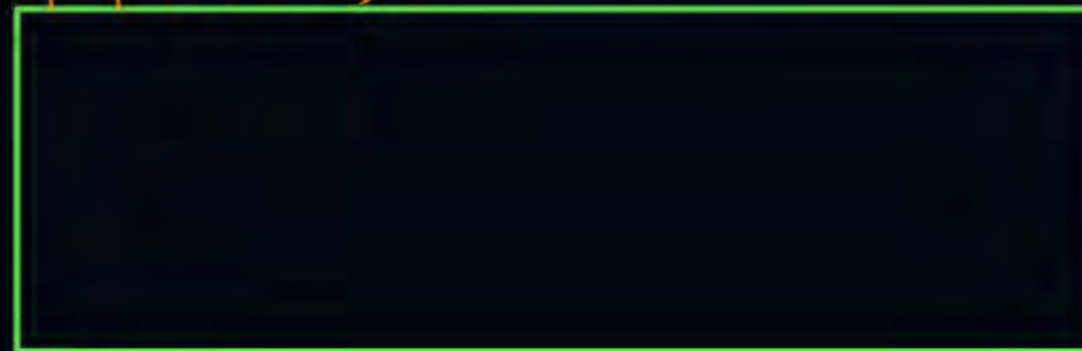
3. $\text{for } i \leftarrow 1 \text{ to } n$
 $n \rightarrow \text{for } j \leftarrow 1 \text{ to } n$
 $k \leftarrow k * m;$

$i++ : 3(n)$
 $\text{for } i \leftarrow 1 \text{ to } 3$

3 Inc. $\left\{ \begin{array}{l} i=1 \\ i=2 \\ i=3 \\ i=4 \end{array} \right\}$ 4 Comp's $(n+1)$

Step-count
RAM Model of Computation 

Memory



(Hyp. m/c)

CPU



$$\left[\begin{array}{l} 1 + (n+1) \\ + n + \\ n + n \end{array} \right] = (4n+2)$$

$$\begin{aligned} & (1 + (n+1) + n : i \\ & + n + (n+1) \cdot n + n \cdot n : j \\ & + n \cdot n + n \cdot n) \\ & = \underline{4n^2 + 4n + 2} \end{aligned}$$

Each Fund. op'n
Basic op'n
takes one unit
of time



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$$Time = 2 + (4n + 2) + (4n^2 + 4n + 2)$$

$$Time = (4n^2 + 8n + 6) \text{ units}$$

n : (input size)

ASN/Notation

$\rightarrow O(n^2)$

Repr. the Time

(Comparison) ^{metric}

Linear-Search

	1	2	3	4	5		n
A						-	

(x)

THANK - YOU