

CS & IT ENGINEERING

Data Structure

Graphs

In One Shot



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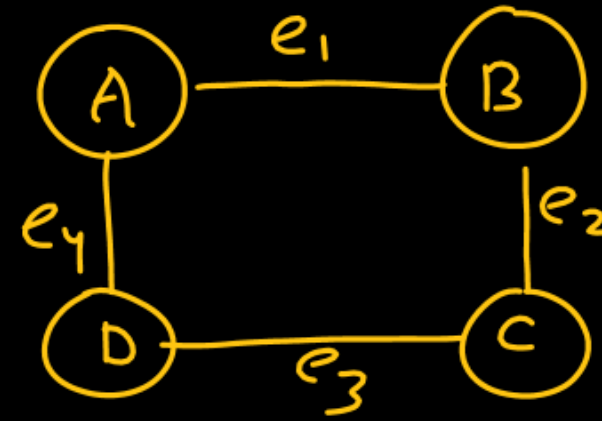
TOPICS TO BE
COVERED



Graphs

Non-linear data structure :

Graph



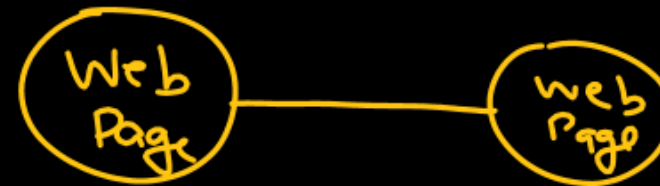
$G(V, E)$
↓ set of vertices
↘ set of Edges

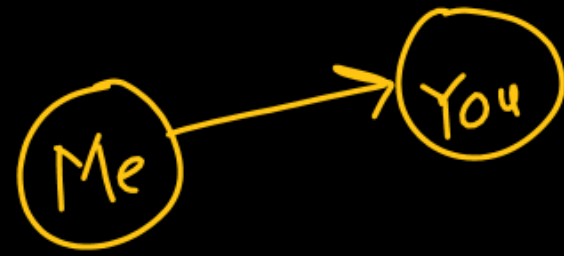
$V = \{A, B, C, D\}$

$E = \{e_1, e_2, e_3, e_4\}$

CS

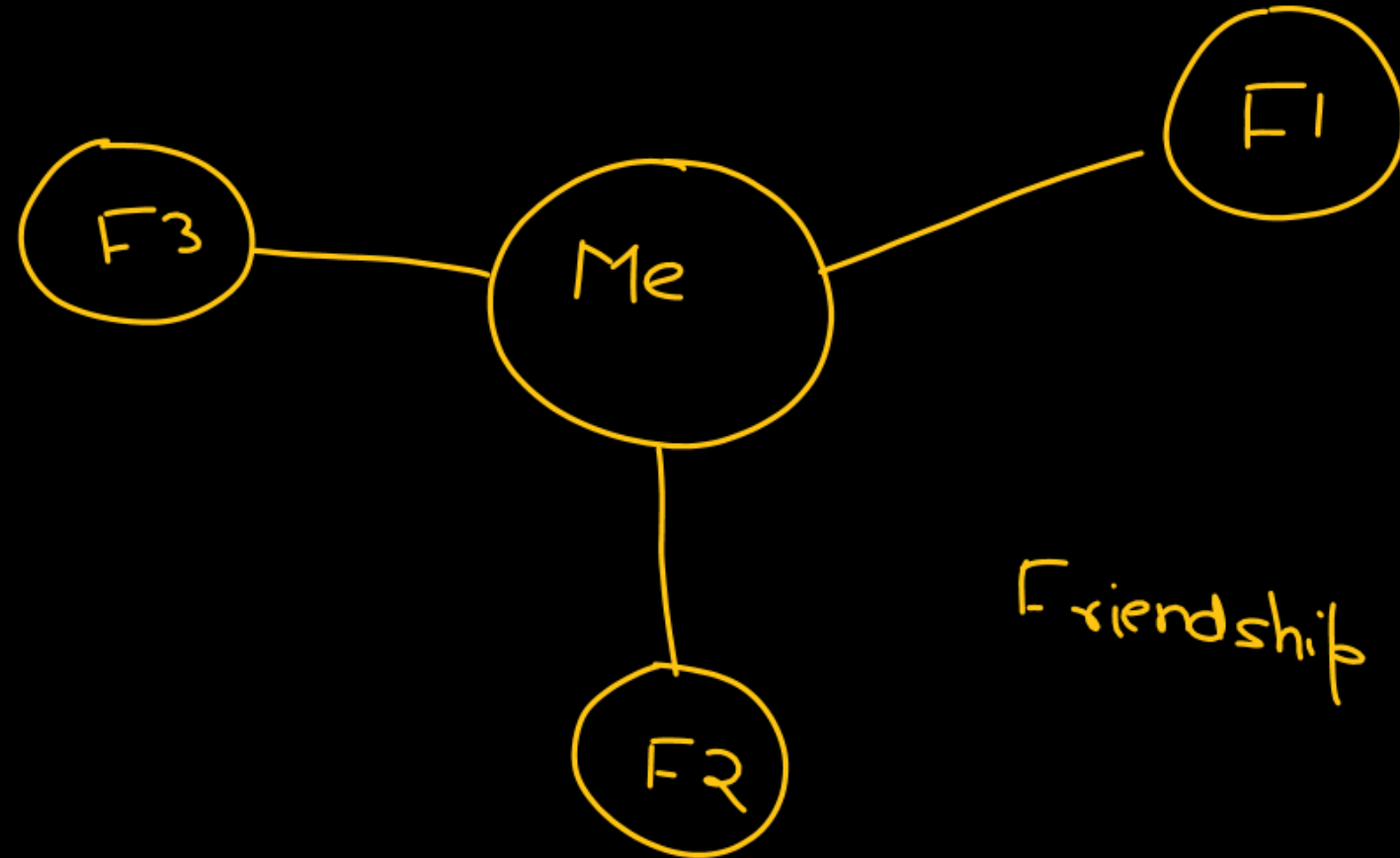
WWW



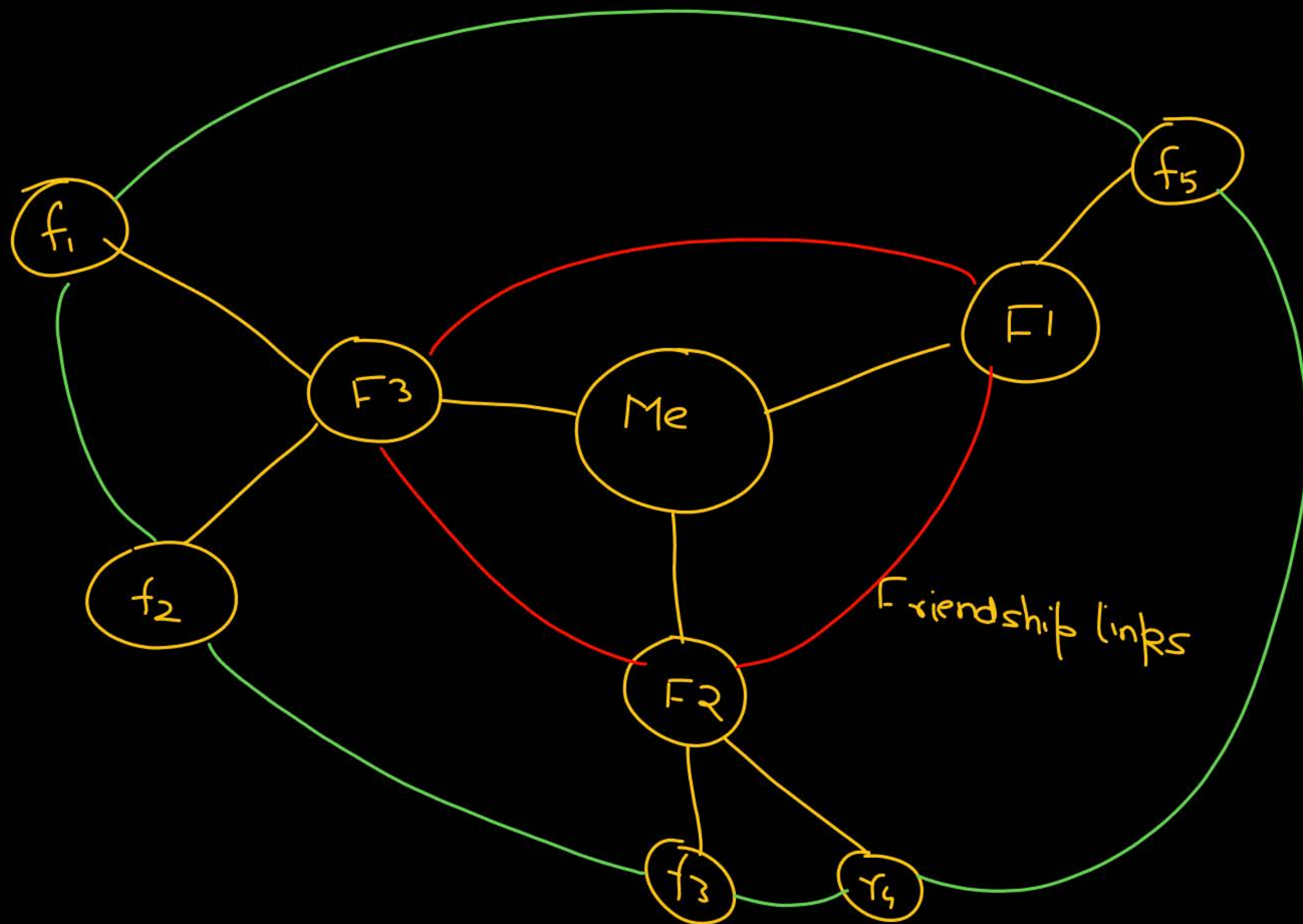


Social N/w

FB



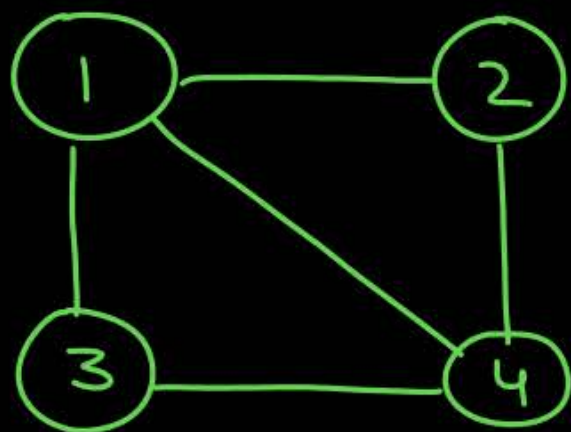
Friendship links



Graph Representation



$n=4$



$n \times n$ Matrix

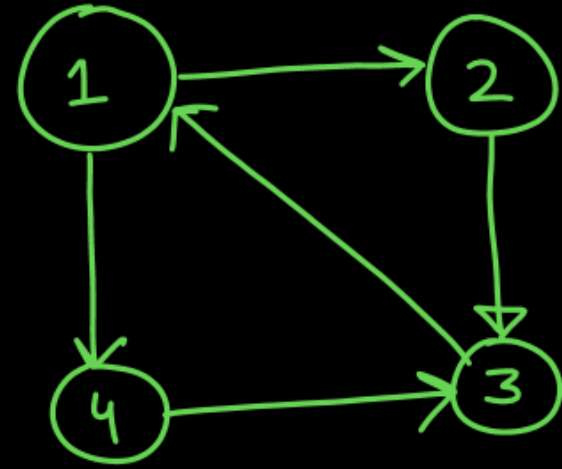
in which Each entry
is either 0 or 1

Undirected

$\hookrightarrow 2|E|$

$$A = \begin{matrix} & \begin{matrix} 1 & 2 & 3 & 4 \end{matrix} \\ \begin{matrix} 1 \\ 2 \\ 3 \\ 4 \end{matrix} & \begin{bmatrix} 0 & 1 & 1 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 \\ 1 & 1 & 1 & 0 \end{bmatrix} \end{matrix}$$

$A_{ij} = 1$ if node i is adjacent to
node j
 $= 0$, otherwise



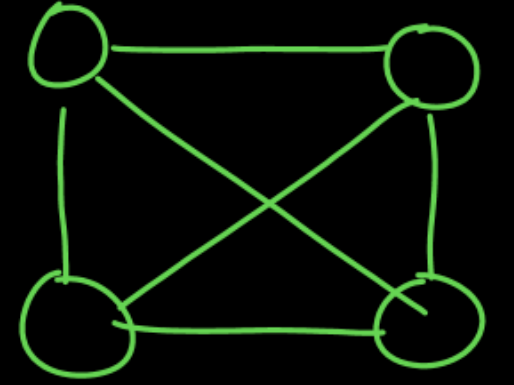
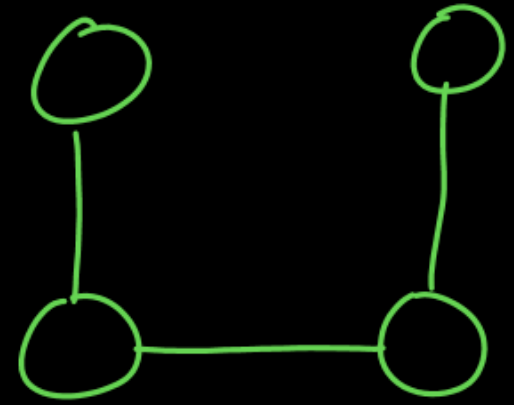
$$\begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \end{array} \begin{bmatrix} & 1 & 2 & 3 & 4 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

10^{10} \Rightarrow users

$10^{10} \times 10^{10}$

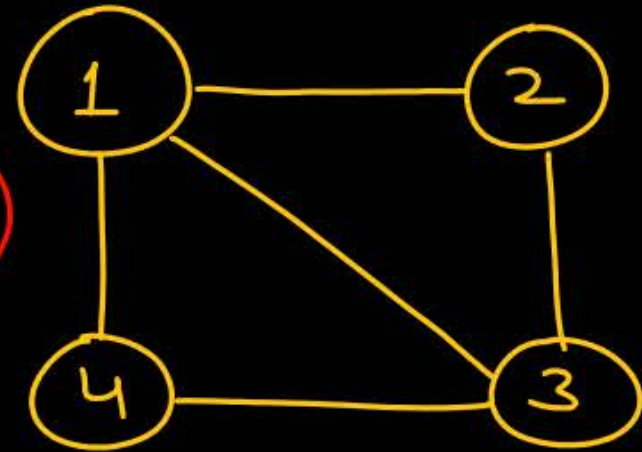
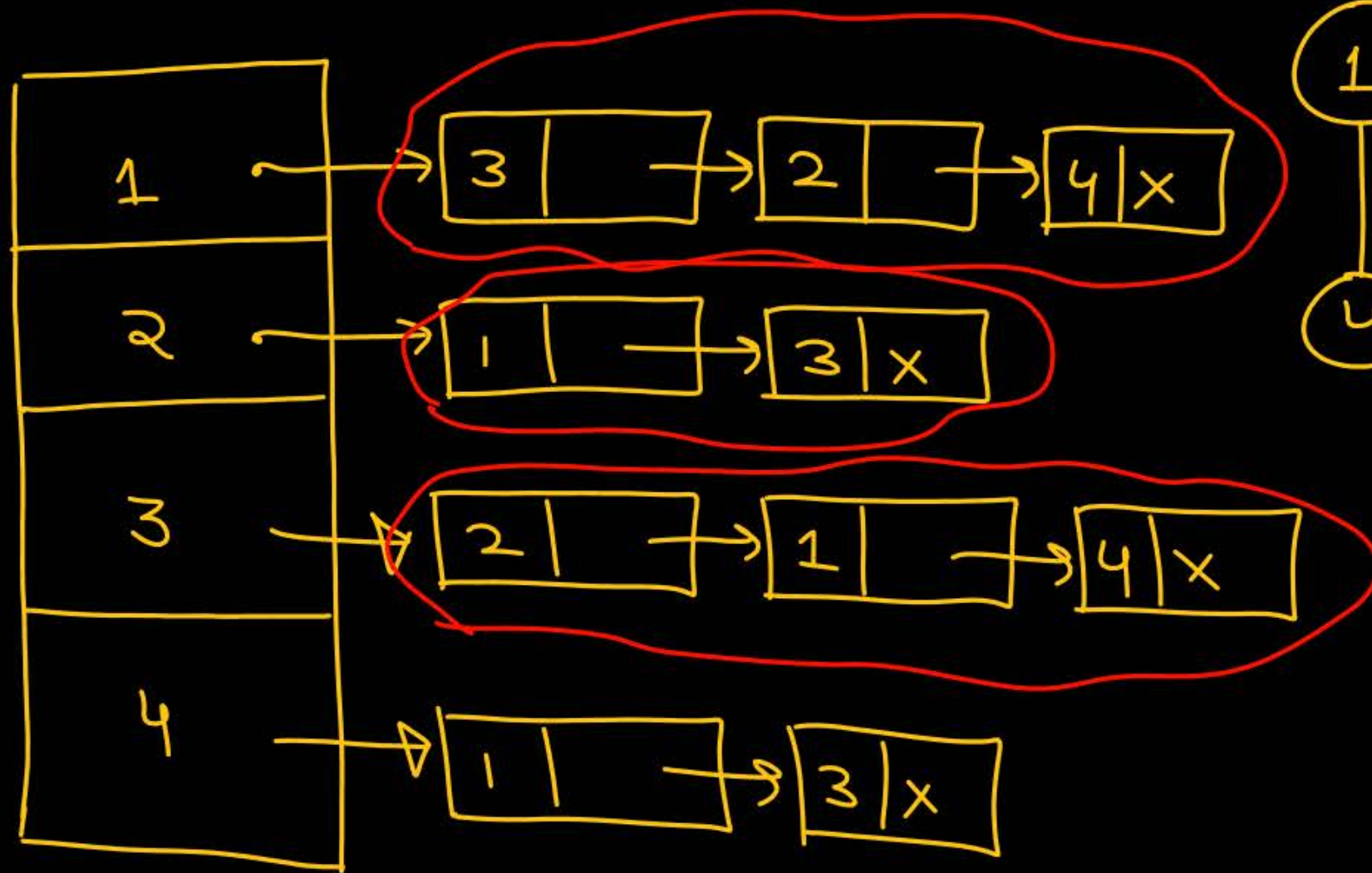
Adj. Matrix

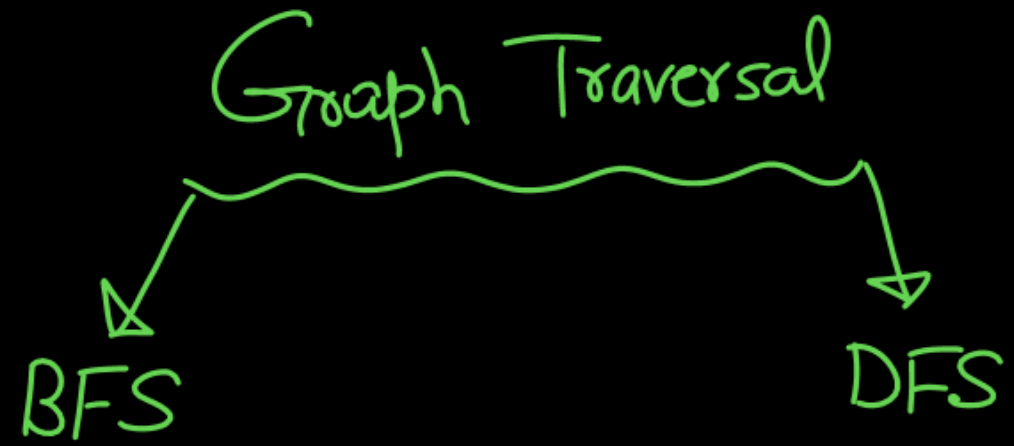
Sparse
Entry 1



C++ \Rightarrow array of vector

Adjacency List





visiting a node :

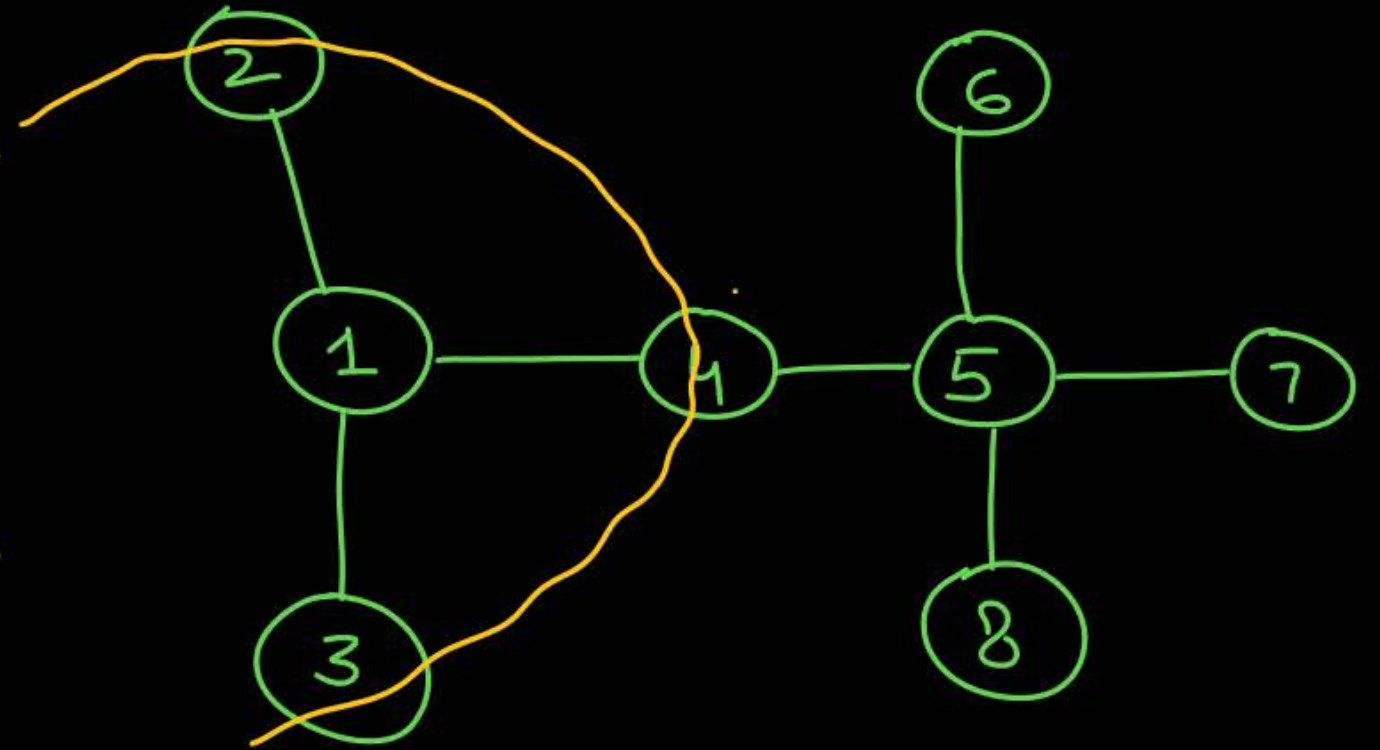
Exploring a node :

Queue
BFS

✓ ✓ ✓ ✓ ✓ ✓ ✓ ✓
(1) (2) (3) (4) (5) (6) (7) (8)

1 2 3 4 5 6 7 8

1 distance 2 3 distance
distance



Queue
BFS

1, 4, 5

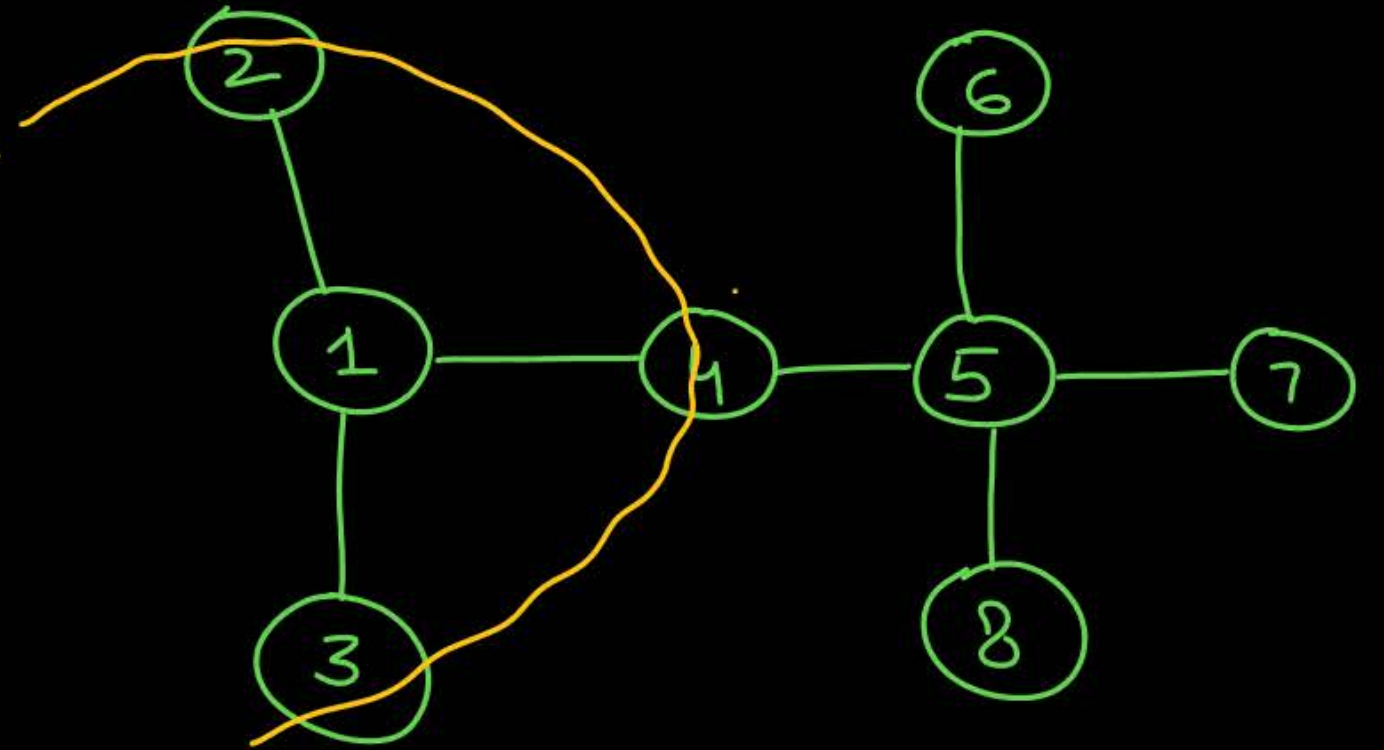
1, 3, 2, 4, 5, 6, 7, 8

1, 3, 2, 4, 5, 6, 8, 7

1, 3, 2, 4, 5, 7, 6, 8

1, 3, 2, 4, 5, 7, 8, 6

1, 2, 3, 4, 5, 6, 7, 8



1 2 3 4 5 6 7 8

1 distance

2

distance

3 distance

1, 2

Explore Explore
start start

Explore
stop

✓
x

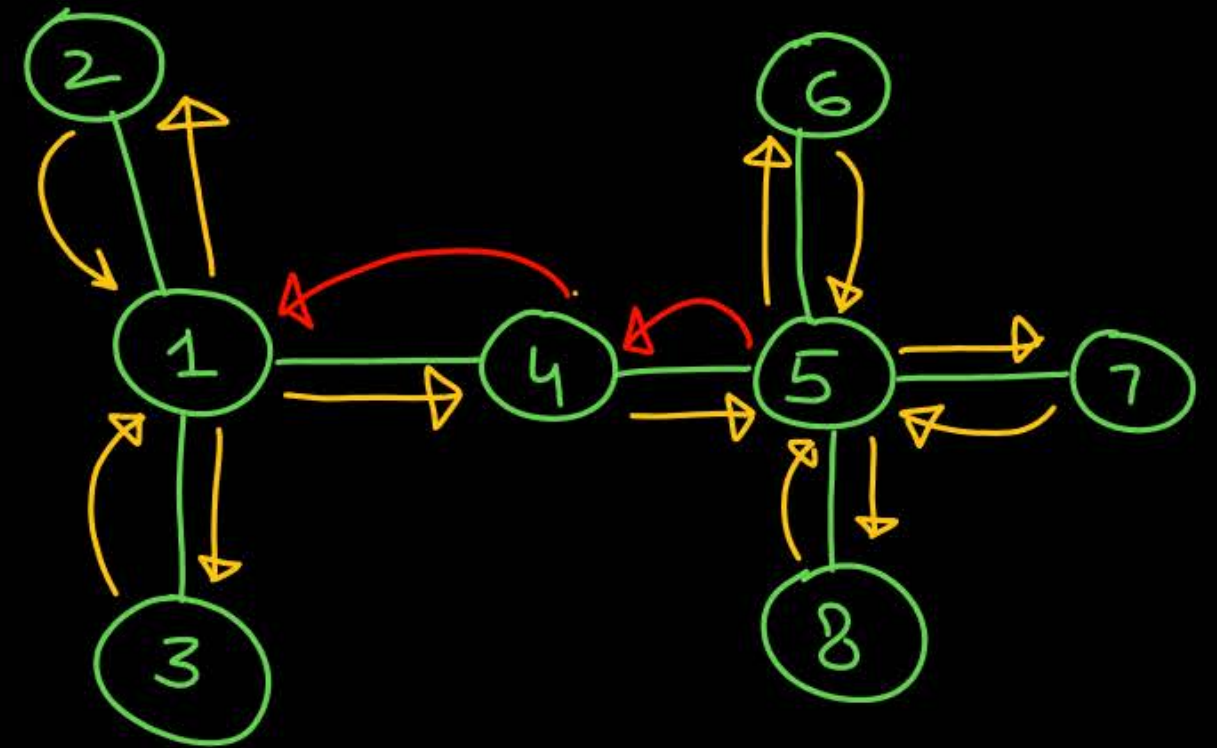
✓

✓

✓

✓

1, 2, 3, 4, 5, 6, 7, 8



1, 2, 6, 5, 7, 8, 4, 1, 3

Source node

① Hashing

② Hashing

8:30

