

# CS & IT ENGINEERING

Data Structure



**Tree**  
**Chapter- 5**  
**Lec- 10**



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TOPICS TO BE  
COVERED

Tree-X

infix :  $a \times b + e/f - g$

$\times$   $/$   
 $+$   $-$

Expression tree :

leaf : Operands

Internal  
nodes : operators



$\Rightarrow a \times b$

inorder :  $a \times b$

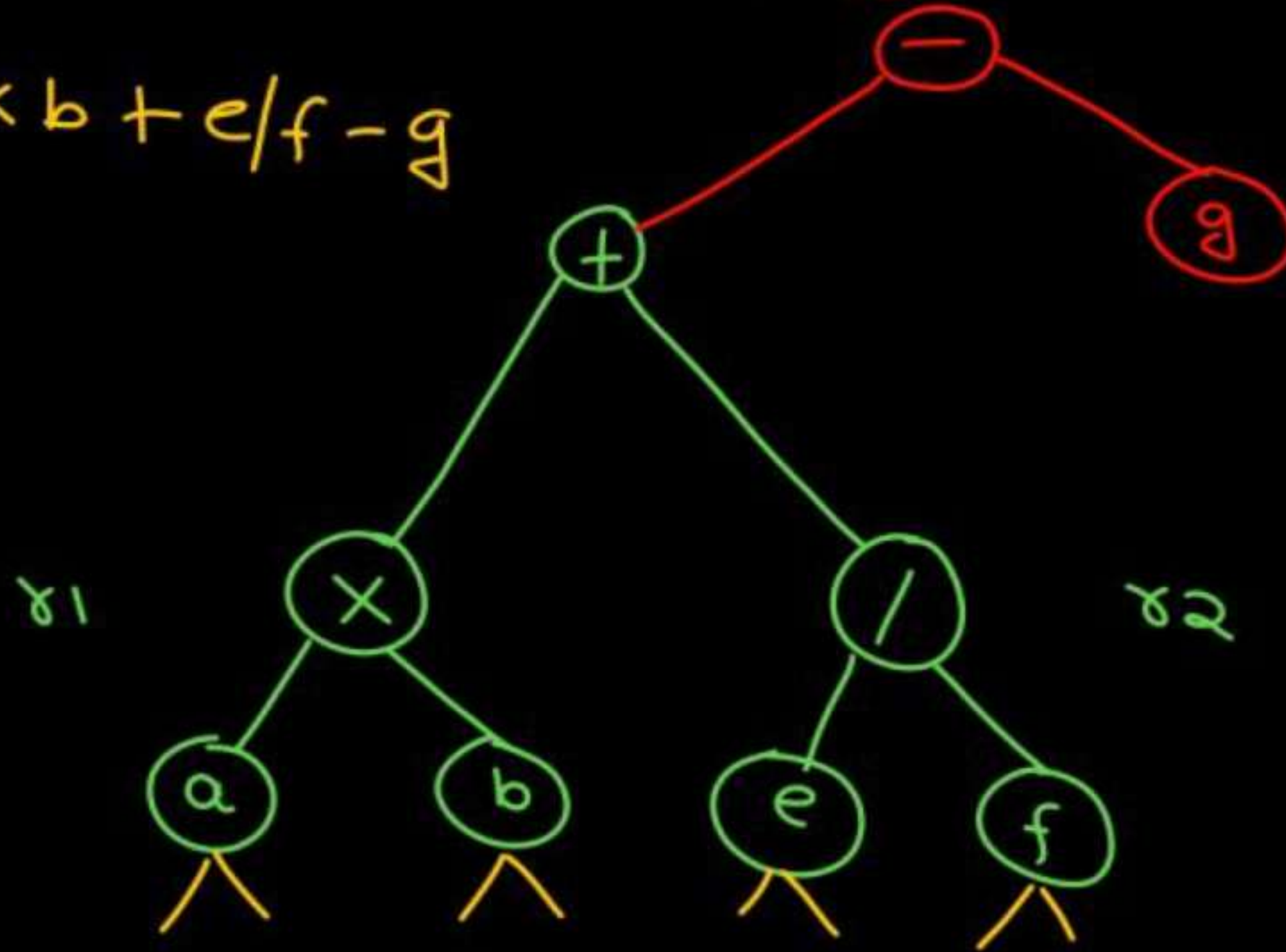
infix:  $(a \times b) + \frac{e}{f} - g$

$\gamma_1$                    $\gamma_2$

$\gamma_1 + \gamma_2 - g$

$B - \gamma$

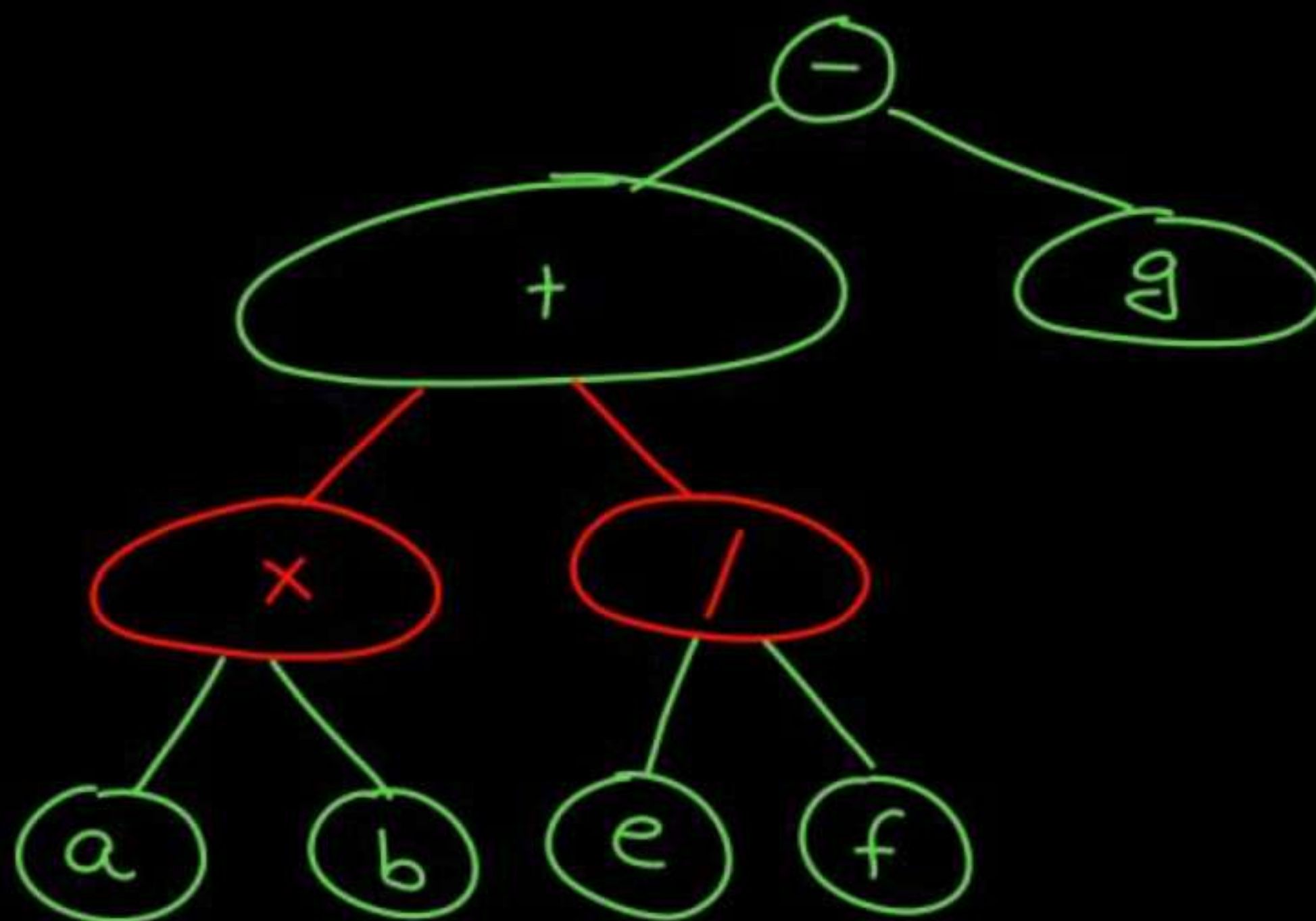
inorder:  $a \times b + e/f - g$



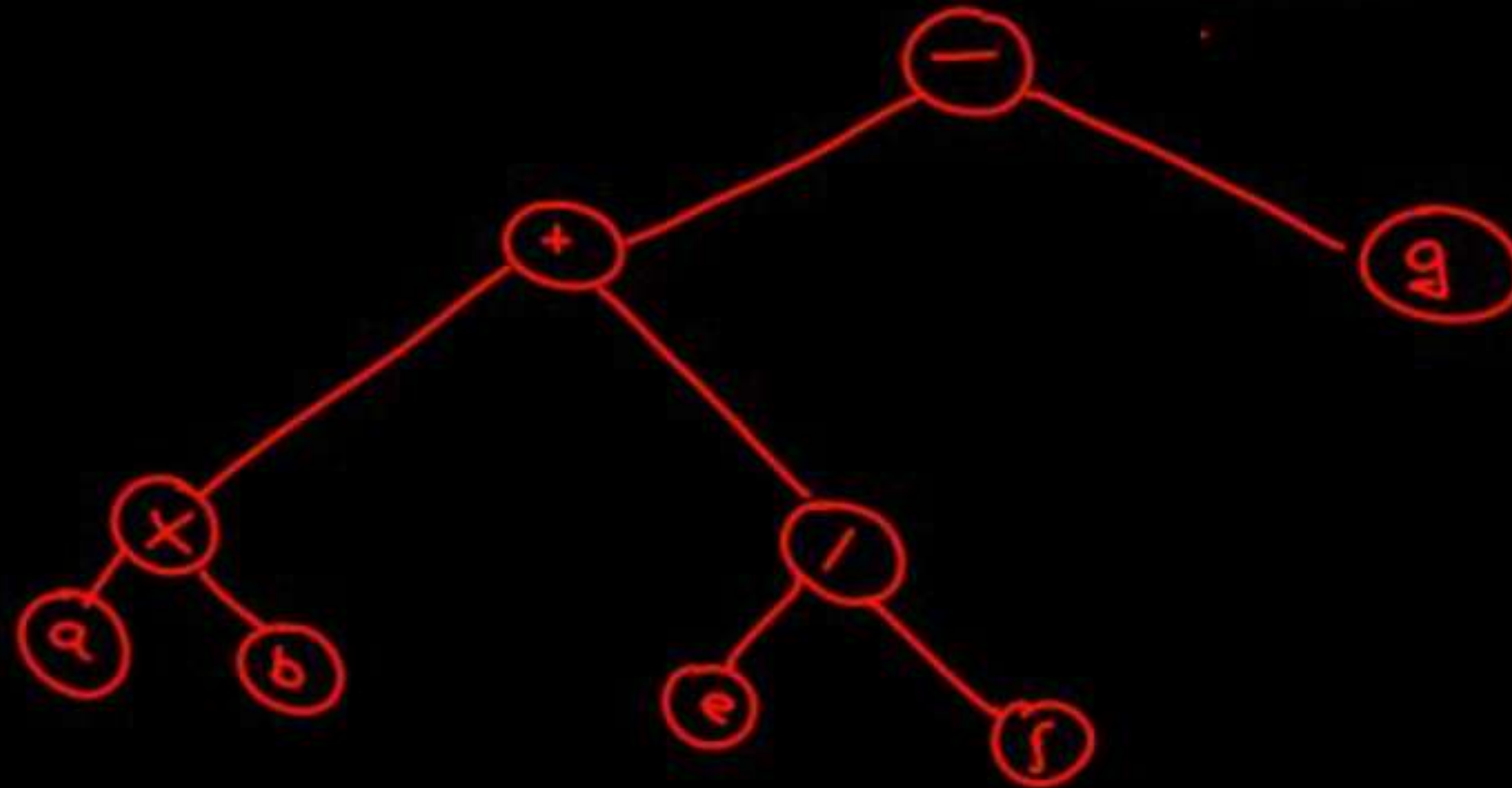
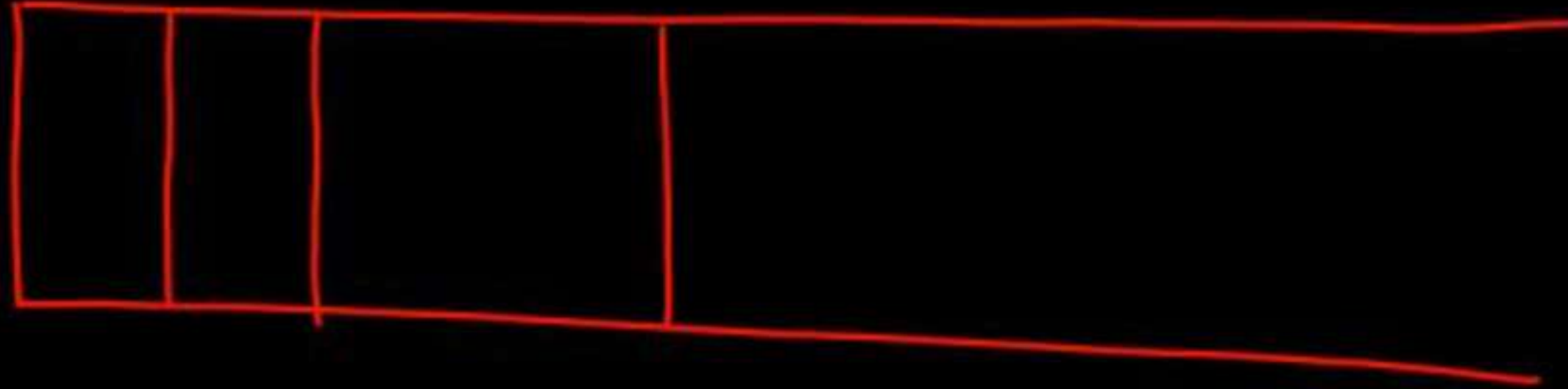


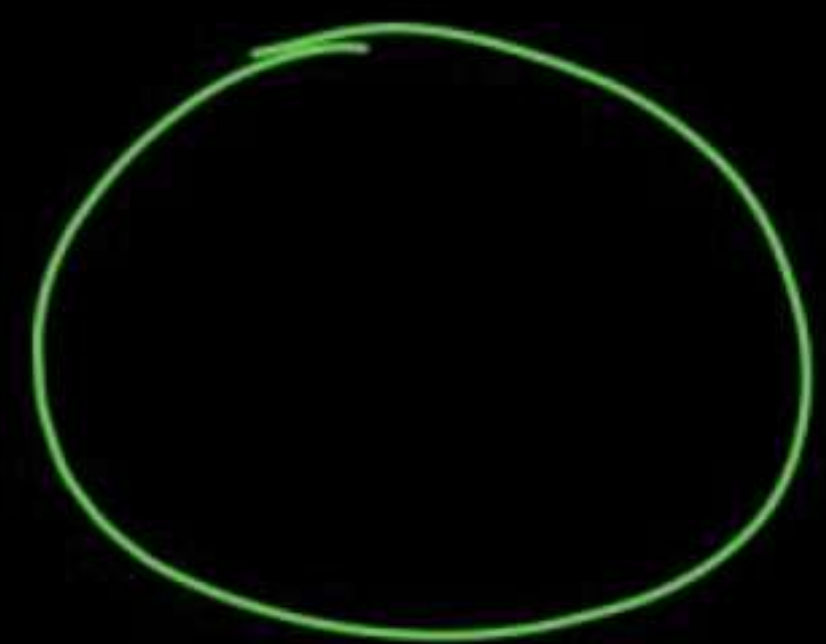
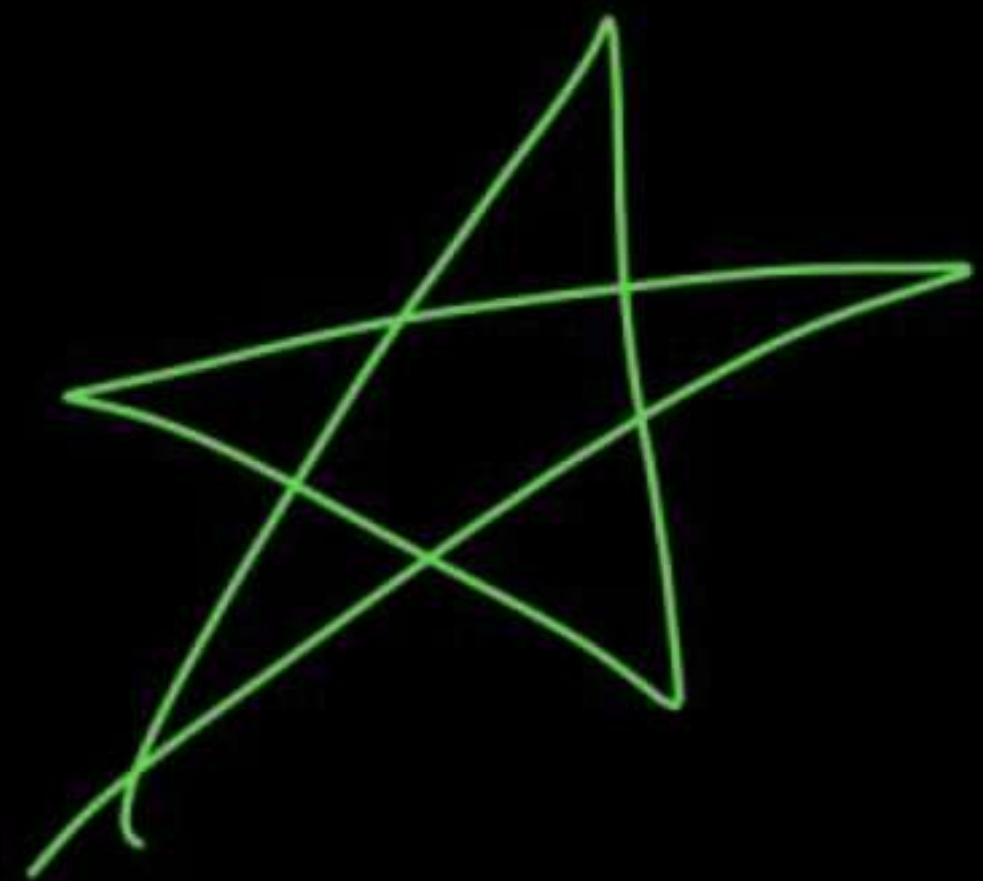
$$a \times b + e / f - g$$

last



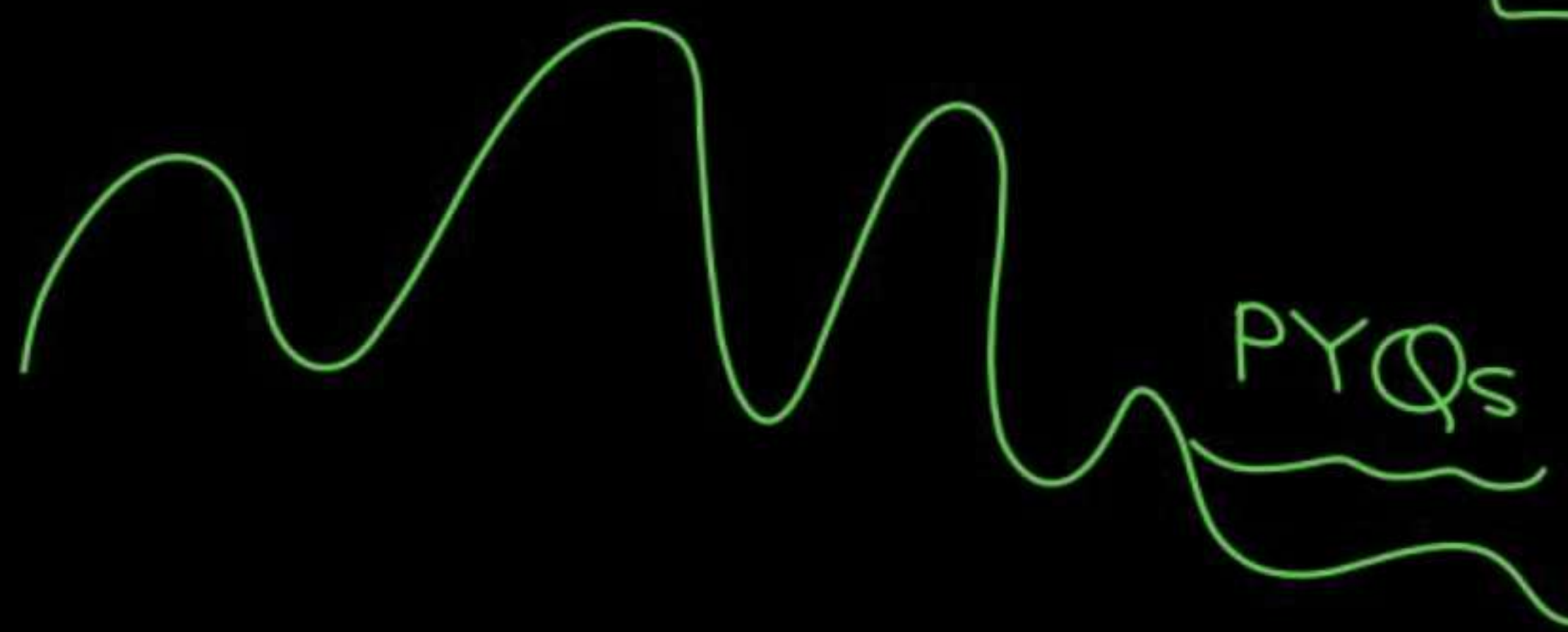
infix:  $a \times b + e / f - g$   
Postfix:  $a b \times e f / + g -$





Algo  
Graph  
⇒ 1 lecture

Tree  
└→ Revise  
Doubt



Doubt





+ DPP  
+ P/Q  
+ Test Series

10 hrs  $\rightarrow$  2 days

Hard rules

$\rightarrow$  follow

200 pages  $\times 10$

= 2000 pages



✓ infix:  $2 + 3 \times 4$

Prefix:  $+ 2 \times 3 4$

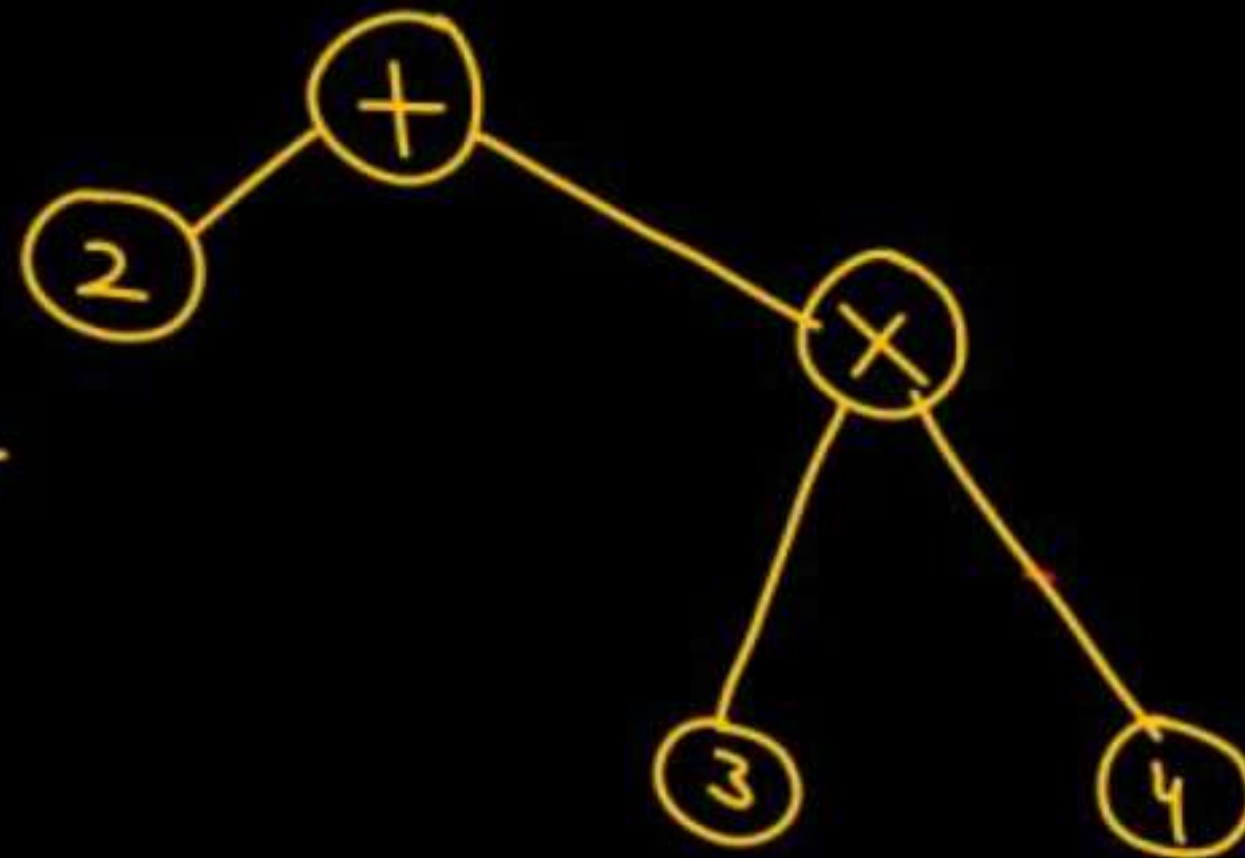
Reverse:  $4 3 \times 2 +$



Inorder:  $2 + 3 \times 4$

Preorder:  $+ 2 \times 3 4$

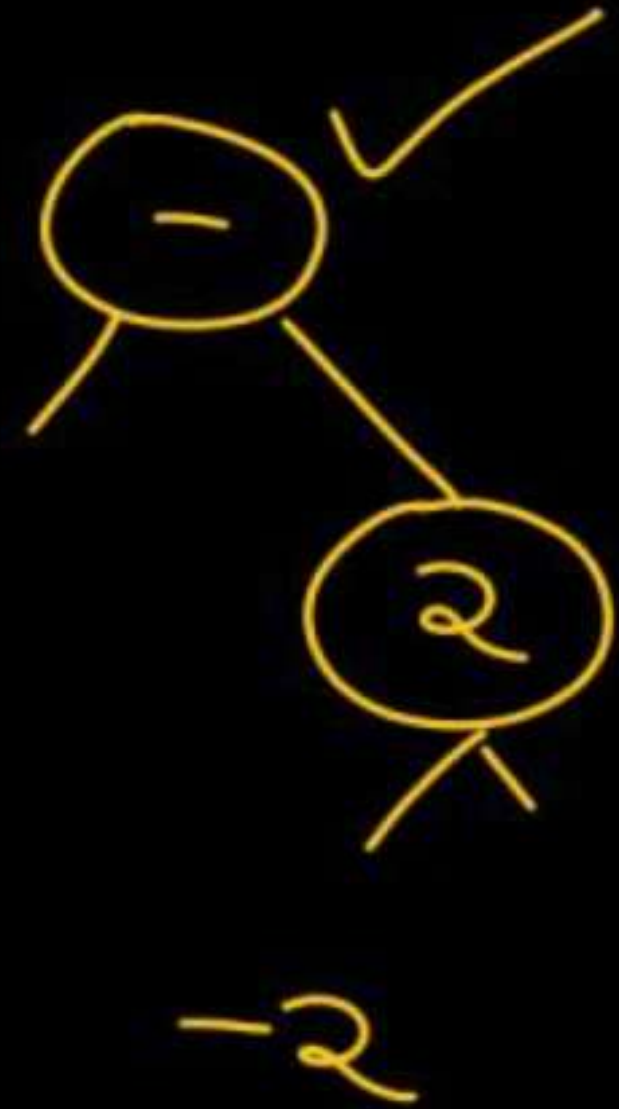
Postorder:  $2 3 4 \times +$



Unary operator } -2

Fail

exp: -2



infix:  $3 \times \log(x+1)$

Postfix:



programming

$$3 \times \log(\underbrace{x+1}_{\textcircled{1}})$$

$$3 \times \log(\underbrace{[x \ 1 +]}_{\text{operand}})$$

operator

$$\underset{\text{op1}}{3} \times \underbrace{[x \ 1 + \log]}_{\text{op2}}$$

Postfix:  $3 \ x \ 1 + \log \ x$

## Tree

- 1.) Binary tree
- 2.) Complete binary tree
- 3.) K-ary tree: Every internal node  $\Rightarrow$  K child

$L + I = K \times I + 1$
$L = (K - 1)I + 1$

- 4.) Full binary tree
- 5.)  $n_{\max} = 2^{h+1} - 1$   
 $n_{\min} = h + 1$

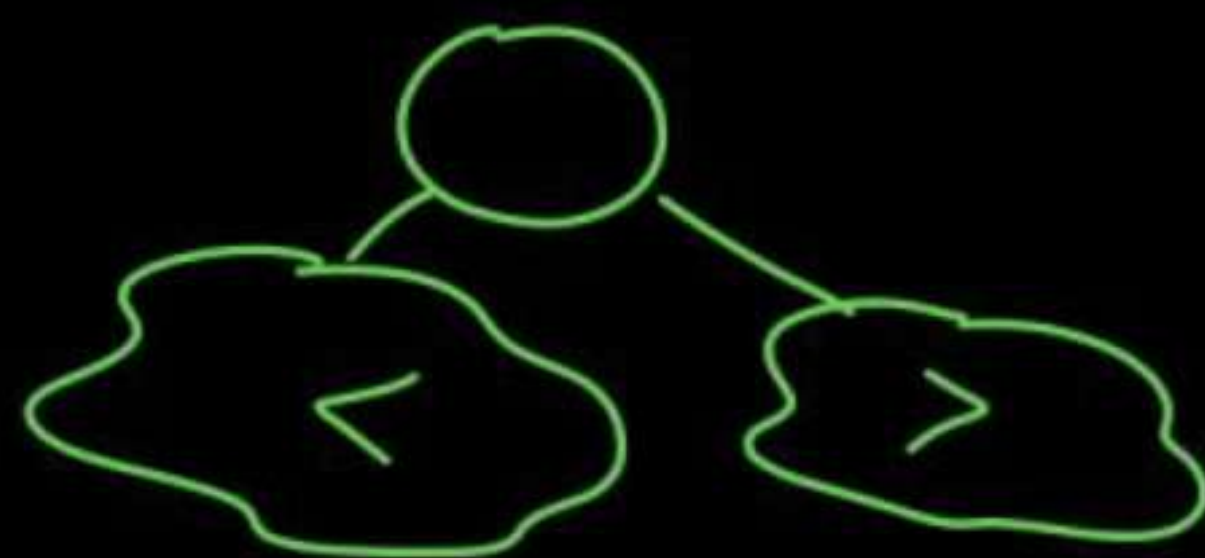
6.)  $n_{\max} \Rightarrow 2^{h+1} - 1$       CBT, BT, BST, AVL tree

$n_{\min} \Rightarrow 2^h$       CBT

$n_{\min} \Rightarrow$  AVL

$n(h) = 1 + n(h-1) + n(h-2)$
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- 7.) BST : Inorder : Asc. order of keys.





8.) # unlabelled binary tree with  $n$  nodes =  $\frac{2^n C_n}{n+1}$

# labelled binary tree with  $n$  nodes  
 &  $n$  distinct keys =  $\frac{2^n C_n}{n+1} \times n!$

# BST with  $n$  keys =  $\frac{2^n C_n}{n+1}$

# Given a <sup>BT</sup> structure with  $n$  nodes & given  $n$  distinct keys  
 BST  $\Rightarrow 1$

q. # Binary tree with a given preorder of length  $n = \frac{2^n C_n}{n+1}$   
 " " " Inorder "  $= \frac{2^n C_n}{n+1}$   
 " " " Postorder "  $= \frac{2^n C_n}{n+1}$

Shortcut / long  $\left. \begin{array}{l} \text{In + Pre} \Rightarrow \text{tree} \\ \text{In + Post} \Rightarrow \text{tree} \end{array} \right\}$

BST  $\rightarrow$  Skewed





infix:  $2 + 3 \times 4$

Postfix:  $\checkmark 2 \checkmark 3 \checkmark 4 \checkmark \times \checkmark + \underline{\underline{\text{End}}}$

