

CS & IT ENGINEERING

Graph Theory

Discrete Mathematics



DPP 08 Discussion Notes



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TOPICS TO BE COVERED

01 Question

02 Discussion

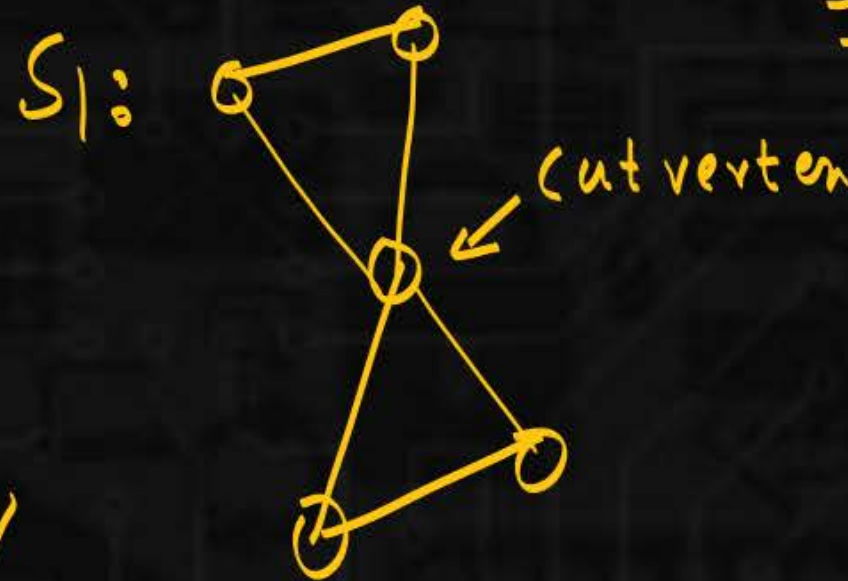
Q.1

Consider the following statements:

S_1 : If a connected graph G has a cut vertex, then G has a cut edge. (false)

S_2 : If a connected graph G has a cut edge then G has a cut vertex. (false)
Which of the following is true?

- A. S_1 only
- B. S_2 only
- C. Both S_1 and S_2
- D. Neither S_1 nor S_2 ✓

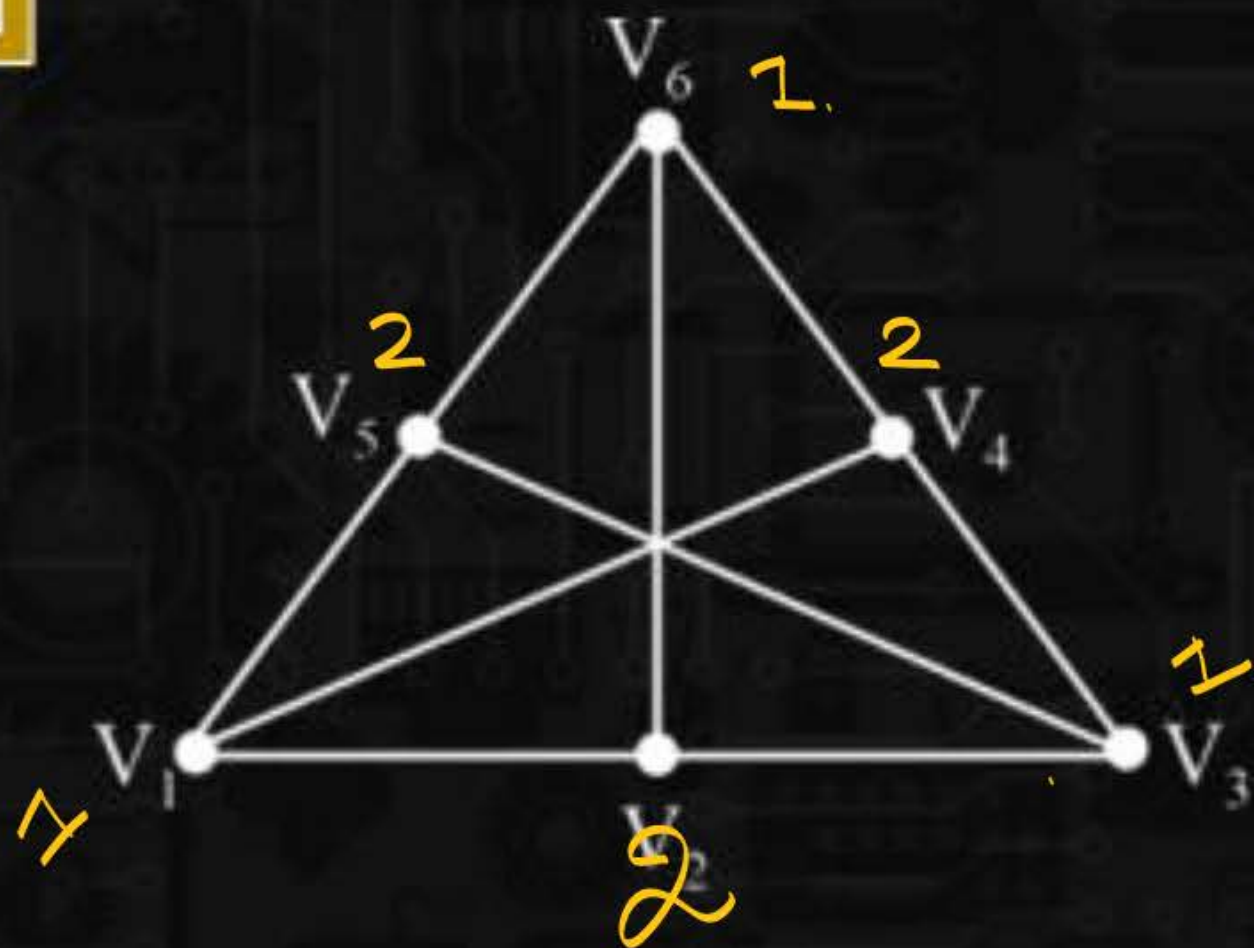


Q.2

For the graph shown below, the chromatic number is 2.



[NAT]



$$\chi(G) = 2$$

Q.3

If G is a connected graph with 10 vertices and vertex connectivity is 3, then minimum number of edges necessary in G is 15.



[NAT]

$$n=10 \quad k(G)=3$$

$$k(G) \leq \frac{2e}{n}$$

$$3 \leq \frac{2 \cdot e}{10}$$

$$30 \leq 2e$$

$$15 \leq e$$

Q.4

Which of the following options is/are correct?

[MSQ]




(T)

A.

The chromatic number of a graph with at least 1 edge is at least 2.

B.

A graph is null graph  if and only if its chromatic number is 2. (false)

C.

For any graph, $K_G \leq 1 + \Delta(G) \leq n$ where $\Delta(G)$ is maximum degree and K_G is chromatic number.

$$X(G) \leq 1 + \Delta(G) \leq n. \quad (T)$$
$$3 \leq 1 + 2 \leq 3$$

D.

The ^{very} chromatic number of a multi graph is equal to its equivalent simple graph chromatic number. (T)

Q.5

[MCQ]



Consider the following statements:

S_1 : A graph is bipartite graph if and only if its chromatic number is 2. (τ)

S_2 : The chromatic number of a tree is 2. Thus, every tree is bipartite graph. (τ)

Which of the following statement is False?

A. S_1 only

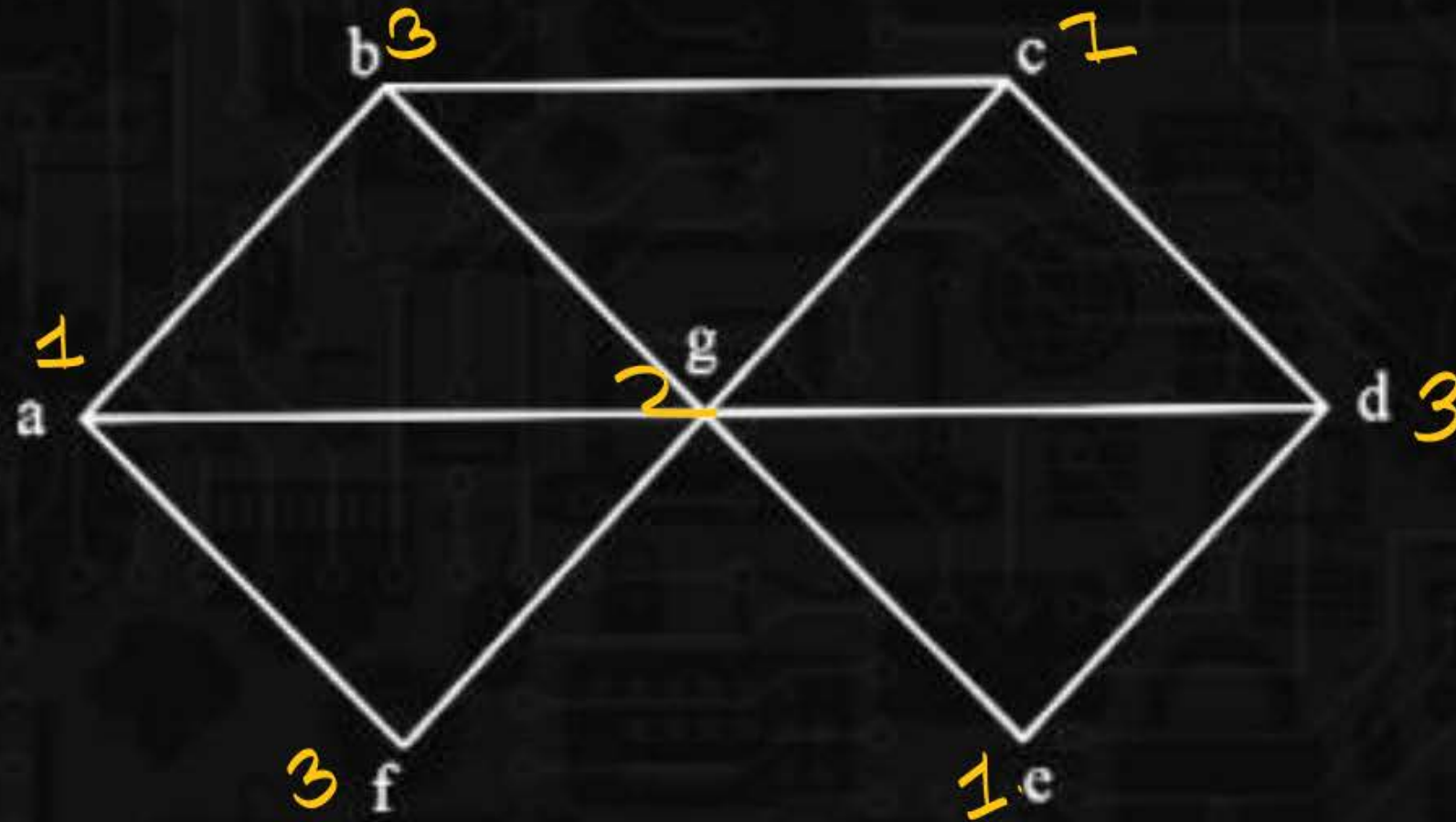
B. S_2 only

C. Both S_1 and S_2

D. Neither S_1 nor S_2 ✓

Q.6

What is the chromatic number of the given graph?



[NAT]

$$\chi(G) = 3$$

