

# 1 $P_{nest}$

```
type Image = [[:Int:]:]
type Hist a = [:a:]

hbalance :: Image -> Image
hbalance img =
    let h = hist img
        a = accu h
        a0 = headP a
        agmax = lastP a
        n = normalize a0 agmax a
        s = scale gmax n
        img' = apply s img
    in img'

hist :: Image -> Hist Int
hist =
    sparseToDenseP (gmax+1) 0
    . mapP (\g -> (headP g,lengthP g))
    . groupP
    . sortP
    . concatP

accu :: Hist Int -> Hist Int
accu = scanlP (+) 0

normalize :: Int -> Int -> Hist Int -> Hist Double
normalize a0' agmax' as =
    let a0 = fromIntegral a0'
        agmax = fromIntegral agmax'
        divisor = agmax - a0
    in [: (fromIntegral freq' - a0) / divisor | freq' <- as :]

scale :: Int -> Hist Double -> Hist Int
scale gmax as = [: floor (a * fromIntegral gmax) | a <- as :]

apply :: Hist Int -> Image -> Image
apply as img = mapP (mapP (as !:)) img
```

## 2 Work and Depth Table

- $n$  sei die Anzahl der Bildpixel
- $w$  sei die Bildbreite
- $h$  sei die Bildhöhe
- $p$  sei die Anzahl der PUs (gang members).

Table 1: Work and Depth complexities

function or variable	O(W)	O(D)
hbalance	$\max(n \log n, gmax)$	$\log \max(n, gmax)$
hist	$\max(n \log n, gmax)$	$\log n$
sparseToDenseP	$gmax$	1
groupP	$n$	$\log n$
sortP	$n \log n$	$\log n$
concatP	1	1
accu	$gmax$	$\log gmax$
scanlP	$gmax$	$\log gmax$
normalize	$gmax$	1
scale	$gmax$	1
apply	$n = w \cdot h \cdot O(1)$	1
mapP f xs	$W(f, x) \cdot size(xs)$	1
headP/lastP	1	1
indexP, !:	1	1

## 3 Other aspects e.g. sync-points, programmer workload, simplicity

- optimisations: no optimisations. Uses many synchronisation points (the many bulkd-functions imply much communication)
- progammer-workload: failry easy to write. I had written it in less than 1 hour.
- simplicity: Implementation can be understood without comments, however needs some time.