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# A Review on Swarm Intelligence Techniques in Automated Cryptanalysis of Classical Substitution Cipher

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**Abstract.** Between the year 2006 and 2019, a considerable new and different swarm intelligence techniques have been presented in the literature for automated cryptanalysis of classical substitution cipher. This paper compares the performance of these new and different swarm intelligence techniques. Three main comparison measures are considered to assess the performance of presented swarm intelligence techniques: efficiency, effectiveness, and success rate. To the best of author knowledge first time this kind of review has been carried out. It is noteworthy that among the presented swarm intelligence techniques the performance of cuckoo search technique is best with respect to all the measures.

## 1. Introduction

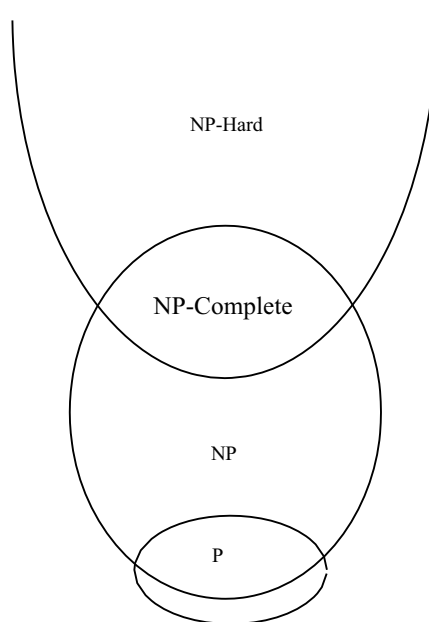
Combinatorial optimization is an approach to deal with a given problem and locate the best answer out of a very large set of possible solutions. The problems for which one need to find the best solutions are mostly comes under the umbrella of NP-hard and NP-complete combinatorial problems. The problem associated related to solving these problems is that the time and/or memory increases drastically with the increase in size of problems [1]. Branch and bound and simplex methods are examples of exact optimization techniques that can be used to speed up the search. However, often these techniques have prohibitive complexity requirements (time and/or memory) which makes the use of these techniques impractical [2]. In such cases, approximate techniques are utilized to determine an adequate solution [2].

The concept of Turing Machine (TM) and the class of decision problems are often used to understand the theory of NP-completeness. "yes" or "no" these are the two possible solutions that are associated with a decision problem [1]. In polynomial time the deterministic TM can solve a set of problems, let such problems categorized in a set P. Similarly, in polynomial time the non-deterministic TM can solve a set of problems, let such problems categorized in a set NP. Let  $P \subseteq NP$  (see Figure 1). When a decision problem belongs to both in NP and NP-hard (hard problems) such problems comes in the category of NP-completeness. Formally, a decision problem X is NP-complete if X satisfy the following two conditions [1]:



(i) X is in NP, and (ii) Every problem in NP is "reducible" to X in polynomial time.

If a candidate solution of X can be verified in polynomial time, then we can say that X is in NP [1]. Note that whether a problem satisfies condition (i) or not, but if it satisfies condition (ii) then said to be NP-hard problem [1]. In this paper the cryptanalysis problems that are considered to solve are comes in the class of NP-complete problems.



**Figure 1.** P, NP, NP-complete and NP-hard [1]

### 1.1. Automated Cryptanalysis

Cipher provides information security. Basically, ciphers are used to transform one form of text called "plaintext" into another form of text called "ciphertext" which is tough to break if the secret key is not known. Cryptanalysis is the process of finding weakness in the design of the ciphers. Cryptanalyst performs cryptanalysis. One of the most difficult tasks of the cryptanalyst is to discover (detect or search) the secret key of the cipher by knowing only some of the ciphertext characters. In terms of information security if cryptanalyst or attacker able to discover the secret key of the cipher then we say that the cipher has been successfully attacked. Attacking cipher comes in the class of NP-complete problem [3][4][5][6]. If the exhaustive search is carried out to detect secret key in the keyspace, then the whole keyspace required to be examined in the worst case that will take significant number of years [7][8][9]. However, automated attacks can be formed using swarm intelligence techniques that can search the ciphers key in an acceptable amount of time [10][11]. The automated cryptanalysis of the classical substitution cipher is considered in this paper. For details about this cipher the reader can refer [9].

## 2. Performance Measurement Criteria

The substitution cipher was discussed in the section 1.2. One can ask what the weakness in the cipher is so that it can be attacked. The answer is – the encryption process used in the substitution cipher does not altered the character frequency distribution significantly. Therefore, the swarm intelligence techniques are capable to match the known language statistics with the character frequency statistics (n- grams) of the encrypted message (a standard strategy to automatically attack the classical ciphers).

There are three criteria based on which the performance of swarm intelligence techniques can be assessed with regard to automated attacks: (1) number of ciphertext characters available for the attack (effectiveness measurement criterion); (2) number of key elements detected correctly (success rate measurement criterion); (3) time required to recover the key (efficiency measurement criterion). Based on these three main criteria we will assess the performance of different swarm intelligence techniques in the result section.

## 3. Literature Review

The application of swarm intelligence techniques in automated attacks of classical substitution ciphers was first reported in 2006 in [12][13], and the outcomes have demonstrated that swarm intelligence strategies are exceptionally efficient and effective. With this inspiration, numerous swarm intelligence techniques have been reported for mounting automated attacks on the substitution cipher, for example, particle swarm optimization, bees algorithm, ant colony optimization, firefly algorithm, and cuckoo search. Among all these algorithms the cuckoo search proposed by Jain and Chaudhary [9][11] has shown the best performance with respect to all the comparison criteria. For automated cryptanalysis of the “classical substitution cipher, hereinafter, substitution cipher” multiple swarm intelligence techniques have been used in the past that have been mentioned above. Below we describe the standard form of these techniques in brief.

Kennedy and Eberhart [14] proposed a population-based swarm intelligence strategy, namely, particle swarm optimization. This strategy has been formulated by means of reproduction investigations of winged creatures rushing. This strategy is starts with a random population of individuals called “particles”. With each particle (or molecule) following parameters are associated: position and velocity. During fly in the multidimensional search space, every molecule changes its position dependent on its own understanding and of neighboring particles. That is, the particle tries to reach to the optimal solution by using its best position and the neighboring best position. The closeness of every molecule to the global optimum is assessed using a fitness function. For point-by-point depiction on the particle swarm optimization the reader can refer [15].

Pham et al. [16] have proposed a population-based swarm intelligence strategy, namely, bees algorithm. The algorithm copies the nourishment rummaging conduct of swarms of bumble bees. In its essential form, the algorithm plays out a sort neighborhood search joined with arbitrary hunt. For point- by-point depiction on the bees algorithm the reader can refer [16].

Bilchev and Parmee [17] developed the first ant colony optimization technique for continuous function optimization. Local optimization was focused on this method. The local search strategy was extended to a global search strategy by Wodrich and Bilchev [18] which was further modified by Jayaraman et al. [19]. This approach performs a bilevel search, with a local search component to exploit good regions of the search space, and a global search component to explore bad regions [19]. For point-by-point depiction on the ant colony optimization the reader can refer [15].

Yang [20] has proposed a population-based swarm intelligence strategy, namely, firefly algorithm. This algorithm is initialized with a random population of individuals called “fireflies”. This technique has been devised based on the flashing pattern of tropical fireflies. Flashing pattern can be idealized using three rules which are mentioned in [20]. For point-by-point depiction on the firefly algorithm the reader can refer [20].

Yang and Deb [21] has proposed a population-based swarm intelligence strategy, namely, cuckoo search. This method is starts with a random population of individuals called “nests”. A best nest (a nest with optimal value w. r. t. objective function) is picked from the available nests. Afterwards, from existing nests one more nest is picked randomly, say,  $i$ th nest. Using  $i$ th nest and best nest, a new nest is generated via Lévy flights. In this process a small fraction of worst nests is also abandoned by new nests. After numerous repetitions, the process stops, and we get a solution with good value regarding the objective function. For point-by-point depiction on the cuckoo search the reader can refer [21][22].

In the literature, particle swarm optimization (PSO), bees algorithm, ant colony optimization, firefly algorithm, and cuckoo search have been utilized to tackle many optimization issues. These methods have also utilized for the optimization problems related to cryptology. The cryptology problems solved using these methods and their applications is shown in Table 1.

**Table 1.** Applications of Cryptology Problems Solved using PSO, Bees Algorithm, Ant Colony Optimization, Firefly Algorithm, and Cuckoo Search

Authors [Reference]	Swarm Intelligence Technique Used	Problem Solved	Application
Uddin and Youssef [12] Ali et al. [23] Sadiq [24]	PSO	Automated Cryptanalysis of Classical Substitution Cipher	Modern Substitution Ciphers Uses Functions of Classical Substitution Cipher in a Complicated Way [8].
Ali [25]	Bees Algorithm		
Uddin and Youssef [13] Grari et al. [26]	Ant Colony Optimization		
Luthra et al. [27] Singh et al. [28]	Firefly Algorithm		
Jain and Chaudhari [9] Jain and Chaudhari [11]	Cuckoo Search		
Hameed and Hmood [29] Jassim [30]	PSO	Automated Cryptanalysis of Classical Transposition Cipher	Modern Transposition Ciphers Uses Functions of Classical Transposition Cipher in a Complicated Way [8].
Russell et al. [31] Mekhaznia and Menai [32] Heydari and Senejani [33]	Ant Colony Optimization Cuckoo Search		
Shahzad et al. [34] Abd-Elmonim et al. [35] Pandey and Mishra [36] Jadon et al. [37]	PSO	Automated Cryptanalysis of Data Encryption	DES is a Modern Block Cipher Used for Encryption of Confidential Information [8].

Khan et al. [38] Grari et al. [39]	Ant Colony Optimization	Standard (DES)	
Amic et al. [40]	Firefly Algorithm		
AbdulHalim [41]	PSO	Automated Cryptanalysis of Knapsack Cipher	Knapsack Cipher is a Reasonable Alternative, Particularly for Security of Little Implanted Gadgets, e.g., Cellular Devices [8].
Palit et al. [42]	Firefly Algorithm		
Bhateja et al. [10] Bhateja et al. [43]	Cuckoo Search PSO	Automated Cryptanalysis of Vigenere Cipher	Modern Substitution Ciphers Uses Functions of Vigenere Substitution Cipher in a Complicated Way [8].
Grari et al. [44]	Ant Colony Optimization	Automated Cryptanalysis of Simplified Advanced Encryption Standard (AES)	AES is a Modern Block Cipher Used for Encryption of Confidential Information [8].
Ahmed et al. [45]	Firefly Algorithm	Construction of Novel Substitution-Box	Novel Substitution-Box Can be Used in Design of Stream Ciphers. Stream Ciphers are Used for Encryption of Confidential Information [45]

#### 4. Comparative Analysis

Recall from Section 2, the standard strategy for escalating attacks on the substitution cipher is the matching of the known language statistics with the observed n-gram statistics of the decrypted message. Through matching we determined the cost of the candidate key. A candidate key is a key which is evolved using swarm intelligence technique during the hunt of original secret key.

**Fitness Function.** The input of this function is the candidate key. This function determines the “quality” of the candidate key. For example, from the population of the evolved candidate keys, a key  $K$  is selected. Using  $K$ , a known ciphertext is decrypted. Afterwards, an examination is carried out between n-gram statistics of the decoded ciphertext and the known language statistics. Thusly, the fitness of  $K$  is determined. Formally, Eq. (1) is utilized for statistics comparison.

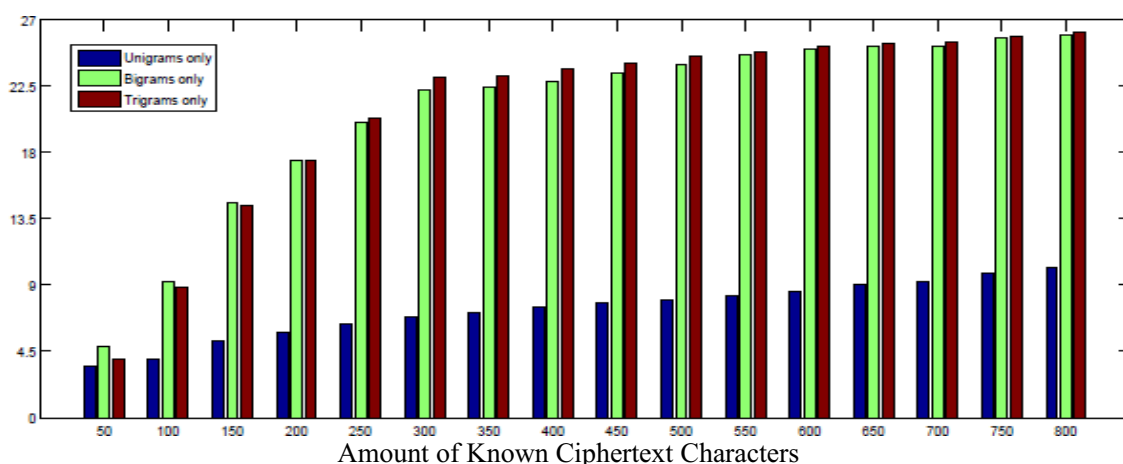
$$\alpha(\sum_{i \in \zeta} |k_i^u - d_i^u|) + \beta(\sum_{i,j \in \zeta} |k_{i,j}^b - d_{i,j}^b|) + \gamma(\sum_{i,j,k \in \zeta} |k_{i,j,k}^t - d_{i,j,k}^t|) \quad (1)$$

For clarification on Eq. (1) the reader can refer [9]. In any case, in the writing it has demonstrated that typically the best operational reason for a fitness function utilized in automated cryptanalysis of substitution ciphers are the bigrams only, i.e.,  $n = 2$  [9, 11-13, 26]. These realities persuade us to utilize

the fitness function which is mentioned in Eq. (2) that depends on just the bigrams.

$$Cost_k = \sum_{i,j \in \zeta} |k_{i,j}^b - d_{i,j}^b| \quad (2)$$

**Experiment.** For performing experiments, the considered swarm intelligence techniques have been implemented in Java. We followed the guidelines reported in the respective papers during implementation of each of the swarm intelligence techniques. Known ciphertext, length of the ciphertext, and the English language bigram statistics are input to every algorithm as shown in figure 2 and table 2.



**Figure 2.** Plotting of Average Outcomes: Number of Key Components Accurately Recovered Utilizing Cost Function Dependent on Unigrams Just, Bigrams Just and Trigrams as it were

**Table 2.** Cryptanalysis Results Obtained Through Various Swarm Intelligence Strategies on the Substitution Cipher

Year	Authors [Reference]	Swarm Intelligence Techniques Used	Maximum Number of Ciphertext Characters Used	Average Number of Key Elements Correctly Recovered out of 27	Mean Performance Time (in seconds) to recover the key
2006	Uddin and Youssef [12]	PSO	1000	24.87	0.437
2006	Uddin and Youssef [13]	Ant Colony Optimization	1000	25.02	0.367

<b>2010</b>	<b>Ali et al. [23]</b>	<b>PSO</b>	<b>1000</b>	<b>24.93</b>	<b>0.441</b>
2011	Luthra et al. [27]	Firefly Algorithm	1000	24.61	0.320
2012	Sadiq [24]	PSO	1000	24.95	0.435
2013	Singh et al. [28]	Firefly Algorithm	1000	24.73	0.320
2013	Ali [25]	Bees Algorithm	1000	24.13	0.523
2016	Grari et al. [39]	Ant Colony Optimization	1000	25.13	0.357
2015, 2019	Jain and Chaudhari [9, 11]	Cuckoo Search	<b>800</b>	<b>26.17</b>	<b>0.137</b>

**Analysis of Results.** Regarding all the performance criteria, we mention the obtained results in the Table 2. Note that the swarm intelligence technique that takes a greater number of ciphertext characters are said to be less effective than the swarm intelligence technique which takes lesser number of ciphertext characters. From the obtained results, we can observe that the cuckoo search proposed in [9] and [11] is most effective because taking only 800 number of ciphertext characters for successful recovery of key. From the obtained results, we can clearly observe that the cuckoo search technique proposed in [9] and [11] takes only 800 ciphertext characters and as an outcome able to recover 26.17 number of key elements. The time taken by the algorithm is also lowest which is 0.137 seconds.

## 5. Conclusions

The efficient, effective, and successful utilization of various swarm intelligence techniques in solving the substitution cipher is presented. The following outcomes are noted: (1) In terms of successful attacks and efficiency the PSO proposed by Sadiq [24] performs better than the PSO proposed by Uddin and Youssef [12] and Ali et al. [23]. (2) In terms of successful attacks and efficiency the ant colony optimization proposed by Grari et al. [39] performs better than the ant colony optimization proposed by Uddin and Youssef [13]. (3) In terms of successful attacks, the firefly algorithm proposed by Singh et al. [28] performs better than the firefly algorithm proposed by Luthra et al. [27]. (4) In terms of all the measures the performance of Bees algorithm proposed by Ali [25] is worst. (5) In terms of all the measures the performance of the cuckoo search technique proposed by Jain and Chaudhari [9, 11] is extremely significantly best.

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