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# 1 src/graph/unionfind.cpp

```
// Fast union find
// Uses 1-indexing
#include <bits/stdc++.h>
using namespace std;
struct unionFind {
        vector<int> u;
        vector<int> us;
        // Construct union find data structure of n vertices
        unionFind(int n) : u(n+1), us(n+1) {
                for (int i=1;i<=n;i++) {</pre>
                        u[i]=i;
                         us[i]=1;
        // Get the union of x
        int get(int x) {
                if (x==u[x]) return x;
                return u[x]=get(u[x]);
        // Union a and b
        void un(int a, int b) {
                a=get(a);
                b=get(b);
                if (a!=b) {
                         if (us[a] < us[b]) swap(a, b);</pre>
                         us[a]+=us[b];
                         u[b]=a;
        }
};
```

### 2 src/graph/stronglyconnected.cpp

```
// Uses Kosaraju's algorithm O(V+E)
// Components will be returned in topological order
// Uses 1-indexing
#include <bits/stdc++.h>
using namespace std;
struct SCC{
        vector<int> used;
        vector<vector<int> > g2;
        // First dfs
        void dfs1(vector<int>* g, int x, vector<int>& ns) {
                if (used[x]==1) return;
                used[x]=1;
                for (int nx:g[x]) {
                        g2[nx].push_back(x);
                        dfs1(g, nx, ns);
                ns.push_back(x);
        // Second dfs
        void dfs2(int x, vector<int>& co) {
                if (used[x]==2) return;
                used[x]=2;
                co.push_back(x);
                for (int nx:g2[x]) {
                        dfs2(nx, co);
        }
        // Returns strongly connected components of the graph in vector ret
        // n is the size of the graph, g is the adjacency list
        SCC(vector < int > * g, int n, vector < vector < int > > & ret) : used(n+1), g2(n+1) {
                vector<int> ns;
                for (int i=1;i<=n;i++) {
                        dfs1(g, i, ns);
                for (int i=n-1;i>=0;i--) {
                        if (used[ns[i]]!=2) {
                                ret.push_back(vector<int>());
                                dfs2(ns[i], ret.back());
        }
};
```

### 3 src/graph/rootedtree.cpp

```
// Build parent array of tree using O(n log n) space
// Query i:th parent in O(log n) time
// Query lca in O(log n) time
// Query distance in O(log n) time
// Uses 1-indexing
#include <bits/stdc++.h>
using namespace std;
struct RootedTree {
        // This has to be at least ceil(log2(n))
        const int logSize=22;
        vector<int> d;
        vector<array<int, logSize> > p;
        // Dfs for building parent array
        void dfs(vector<int>* g, int x, int pp, int dd) {
                p[x][0]=pp;
                for(int i=1;i<logSize;i++) {</pre>
                        p[x][i]=p[p[x][i-1]][i-1];
                d[x]=dd;
                for (int nx:g[x]) {
                        dfs(g, nx, x, dd+1);
        // Construct parent array data structure of tree of size n
        // g is the adjacency list of the tree
        RootedTree(vector<int>* g, int n, int root=1) : d(n+1), p(n+1) {
                dfs(g, root, 0, 0);
        // Returns the node h edges above x.
        // Returns 0 if no such node exists
        int parent(int x, int h) {
                for (int i=logSize-1;i>=0;i--) {
                        if ((1<<i)&h) {
                                x=p[x][i];
                return x;
        // Returns lca of nodes a and b
        int lca(int a, int b) {
                if (d[a]<d[b]) swap(a, b);
                a=parent(a, d[a]-d[b]);
                if (a==b) return a;
                for (int i=logSize;i>=0;i--) {
```

### 4 src/graph/edmondskarp.cpp

```
// Edmonds Karp algorithm for maxflow O(V E^2) or O(f E)
// f is the capacity network and the actual flow can be found in it
// If edges for both directions are used finding actual flow is harder
// Uses 1-indexing
#include <bits/stdc++.h>
#define F first
#define S second
using namespace std;
typedef long long 11;
const int inf=2e9;
struct maxFlow{
        vector<vector<int> > f;
        vector<vector<int> > g;
        vector<int> fr;
        vector<int> used;
        int flow(int so, int si, int n) {
                queue<pair<pair<int, int>, int> > bfs;
                bfs.push(\{\{0, so\}, inf\});
                int fl=0;
                while(!bfs.empty()){
                        auto x=bfs.front();
                        bfs.pop();
                        if (used[x.F.S]) continue;
                        used[x.F.S]=1;
                        fr[x.F.S]=x.F.F;
                        if (x.F.S==si){
                                fl=x.S;
                                break;
                        for (int nx:g[x.F.S]){
                                if (f[x.F.S][nx]>0){
                                        bfs.push(\{\{x.F.S, nx\}, min(x.S, f[x.F.S][nx])\});
                for (int i=1;i<=n;i++) used[i]=0;
                if (fl>0){
                        int x=si;
                        while (fr[x]>0){
                                f[x][fr[x]]+=fl;
                                f[fr[x]][x]-=fl;
                                x=fr[x];
                        return fl;
```

```
return 0;
11 getMaxFlow(int source, int sink){
         int n=fr.size()-1;
         for (int i=1;i<=n;i++){
                 g[i].clear();
                 for (int ii=1;ii<=n;ii++){</pre>
                          if (f[i][ii]!=0||f[ii][i]!=0){
                                   g[i].push_back(ii);
         11 r=0;
         while (1){
                 int fl=flow(source, sink, n);
                 if (fl==0) break;
                 r+=(11)f1;
         return r;
}
void addEdge(int a, int b, int c){
         f[a][b]=c;
\texttt{maxFlow(int n)} \; : \; \texttt{f(n+1), g(n+1), fr(n+1), used(n+1)} \; \big\{
         for (int i=1;i<=n;i++){
                 f[i]=vector<int>(n+1);
```

**}**;

### 5 src/graph/eulertour.cpp

```
// Finds Euler tour of graph in O(E) time
// Parameters are the adjacency list, number of nodes,
// return value vector, and d=1 if the graph is directed
// Return array contains E+1 elements, the first and last
// elements are same
// Undefined behavior if Euler tour doesn't exist
// Note that Eulerian path can be reduced to Euler tour
// by adding an edge from the last vertex to the first
// In bidirectional graph edges must be in both direction
// Be careful to not add loops twice in case of bidirectional graph
#include <bits/stdc++.h>
#define F first
#define S second
using namespace std;
struct EulerTour {
        int dir;
        vector<vector<pair<int, int> > > g;
        vector<int> used;
        void dfs(int x, vector<int>& ret) {
                int t=x;
                vector<int> c;
                while (1) {
                        while (used[g[t].back().S]) g[t].pop_back();
                        auto nx=g[t].back();
                        g[t].pop_back();
                        used[nx.S]=1;
                        t=nx.F;
                        c.push_back(t);
                        if (t==x) break;
                for (int a:c) {
                        ret.push_back(a);
                        while (g[a].size()>0&&used[g[a].back().S]) g[a].pop_back();
                        if (g[a].size()>0) dfs(a, ret);
        EulerTour(vector<int>* og, int n, vector<int>& ret, int d=0) : dir(d), g(n+1) {
                int i2=0;
                for (int i=1;i<=n;i++) {
                        for (int nx:og[i]) {
                                if (d==1||nx<=i) {
                                        if (d==0&&nx<i) {
                                                g[nx].push_back({i, i2});
```

# 6 src/general.cpp

```
// Standard
#include <bits/stdc++.h>
#define F first
#define S second
typedef long long 11;
typedef __int128 lll;
typedef long double ld;
using namespace std;
// GCC extension namespaces
using namespace __gnu_pbds;
using namespace __gnu_cxx;
// Data structures
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
// Numeric
#include <ext/numeric>
int main(){
        // Fast I/O:
        ios_base::sync_with_stdio(0);
        cin.tie(0);
```

### 7 src/math/gaussjordan.cpp

```
// Solves system of linear equations in O(n^3)
// Using doubles or mod 2
// Using doubles might have large precision errors or overflow
// Returns 0 if no solution exists, 1 if there is one solution
// or 2 if infinite number of solutions exists
// If at least one solution exists, it is returned in ans
// You can modify the general algorithm to work mod p by using modular inverse
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
typedef long double ld;
const ld eps=1e-12;
// Using doubles
int gaussD (vector<vector<ld> > a, vector<ld>& ans) {
        int n=(int)a.size();
        int m=(int)a[0].size()-1;
        vector<int> where(m,-1);
        for (int col=0,row=0;col<m\&\&row<n;col++) {
                int sel=row;
                for (int i=row;i<n;i++) {</pre>
                         if (abs(a[i][col])>abs(a[sel][col])) sel=i;
                if (abs(a[sel][col])<eps) continue;</pre>
                for (int i=col;i<=m;i++) {</pre>
                        swap (a[sel][i], a[row][i]);
                where[col]=row;
                for (int i=0;i<n;i++) {
                         if (i!=row) {
                                 ld c=a[i][col]/a[row][col];
                                 for (int j=col; j<=m; j++) {</pre>
                                         a[i][j]-=a[row][j]*c;
                row++;
        ans.assign(m, 0);
        for (int i=0;i<m;i++) {
                if (where[i]!=-1) ans[i]=a[where[i]][m]/a[where[i]][i];
        for (int i=0;i<n;i++) {
                1d sum=0;
                for (int j=0; j < m; j++) {
                        sum+=ans[j]*a[i][j];
```

```
if (abs(sum-a[i][m])>eps) return 0;
        for (int i=0;i<m;i++) {</pre>
                if (where[i]==-1) return 2;
        return 1;
// mod 2
// n is number of rows m is number of variables
const int M=4;
int gaussM(vector<br/>bitset<M> > a, int n, int m, bitset<M-1>& ans) {
        vector<int> where (m, -1);
        for (int col=0,row=0;col<m&&row<n;col++) {</pre>
                for (int i=row;i<n;i++) {</pre>
                         if (a[i][col]) {
                                 swap (a[i], a[row]);
                                 break;
                if (!a[row][col]) continue;
                where[col]=row;
                for (int i=0;i<n;i++) {
                         if (i!=row&&a[i][col]) {
                                 a[i]^=a[row];
                row++;
        ans=0;
        for (int i=0;i<m;i++) {</pre>
                if (where[i]!=-1) ans[i]=a[where[i]][m];
        for (int i=0;i<n;i++) {
                int sum=0;
                for (int j=0; j < m; j++) {
                         sum^=ans[j]*a[i][j];
                if (sum!=a[i][m]){
                         return 0;
        for (int i=0;i<m;i++){</pre>
                if (where[i]==-1) return 2;
        return 1;
int main() {
        // Should output 2, 1 2 0
```

```
vector<vector<ld>> d(3);
d[0]={3, 3, -15, 9};
d[1]={1, 0, -2, 1};
d[2]={2, -1, -1, 0};
vector<ld> da;
cout<<gaussD(d, da)<<endl;</pre>
cout << da[0] << " " << da[1] << " " << da[2] << end1;
// Should output 1, 110
// Note that bitsets are printed in reverse order
bitset<M> r1("0110");
bitset<M> r2("1101");
bitset<M> r3("0111");
vector < bitset < M > > m = \{r1, r2, r3\};
bitset<M-1> ma;
cout<<gaussM(m, 3, 3, ma)<<endl;</pre>
cout<<ma<<endl;</pre>
```

### 8 src/math/miller-rabin.cpp

```
// Deterministic Miller-Rabin primality test
// Works for all 64 bit integers
// Support of 128 bit integers is required to test over 32 bit integers
// Source: http://qubit.pw/trophy.pdf
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
typedef __int128 lll;
111 powmod(111 a, 111 p, 111 mod){
        if (p==0) return 1;
        if (p==2) return (a*a)%mod;
        if (p\%2==1) return (a*powmod(a, p-1, mod))\%mod;
        111 t=powmod(a, p/2, mod);
        return (t*t)%mod;
bool is_w(ll a, ll even, ll odd, ll p){
        111 u = powmod(a, odd, p);
        if (u==1) return 0;
        for (ll j=1; j<even; j*=2) \{
                if (u==p-1) return 0;
                u*=u;
                u%=p;
        return 1;
bool isPrime(11 p) {
        if (p==2) return 1;
        if (p<=1||p\%2==0) return 0;
        11 odd=p-1;
        11 even=1;
        while (odd\%2==0) {
                even*=2;
                odd/=2;
        11 b[7]={2, 325, 9375, 28178, 450775, 9780504, 1795265022};
        for (ll i=0;i<7;i++) {
                11 a=b[i]%p;
                if (a==0) return 1;
                if (is_w(a, even, odd, p)) return 0;
        return 1;
```

### 9 src/math/fft.cpp

```
// Fast Fourier transform and convolution using it
// O(n log n)
// Source: http://cses.fi/kkkk.pdf
#include <bits/stdc++.h>
using namespace std;
typedef long double ld;
typedef long long 11;
typedef complex<ld> co;
const ld PI=atan2(0, -1);
vector<co> fft(vector<co> x, int d) {
        int n=x.size();
        for (int i=0;i<n;i++) {
                int u=0;
                for (int j=1; j< n; j*=2) {
                        u*=2;
                        if (i&j) u++;
                if (i<u) {
                         swap(x[i], x[u]);
        for (int m=2; m <= n; m *= 2) {
                co wm=exp(co\{0, d*2*PI/m\});
                for (int k=0; k< n; k+=m) {
                        co w=1;
                         for (int j=0; j< m/2; j++) {
                                 co t=w*x[k+j+m/2];
                                 co u=x[k+j];
                                 x[k+j]=u+t;
                                 x[k+j+m/2]=u-t;
                                 w = wm;
                         }
        if (d==-1) {
                for (int i=0;i<n;i++) {
                        x[i]/=n;
        return x;
vector<11> conv(vector<11> a, vector<11> b) {
        int as=a.size();
        int bs=b.size();
        vector<co> aa(as);
        vector<co> bb(bs);
        for (int i=0;i<as;i++) {
                aa[i]=a[i];
```

```
for (int i=0;i<bs;i++) {</pre>
                bb[i]=b[i];
        int n=1;
        while (n < as+bs-1) n*=2;
        aa.resize(n*2);
        bb.resize(n*2);
        aa=fft(aa, 1);
        bb=fft(bb, 1);
        vector<co> c(2*n);
        for (int i=0; i<2*n; i++) {
                c[i]=aa[i]*bb[i];
        c=fft(c, -1);
        c.resize(as+bs-1);
        vector<11> r(as+bs-1);
        for (int i=0;i<as+bs-1;i++){
                r[i]=(ll)round(c[i].real());
        return r;
int main(){
        // Shoud print 12 11 30 7
        vector<11> a={3, 2, 7};
        vector < 11 > b = \{4, 1\};
        vector<11> c=conv(a, b);
        for (11 t:c){
                cout<<t<<endl;</pre>
```

# 10 src/string/lcparray.cpp

```
// Constructs LCP array from suffix array in O(n) time
// You can change vector\!<\!int\!> s to string s
#include <bits/stdc++.h>
using namespace std;
vector<int> lcpArray(vector<int> s, vector<int> sa) {
        int n=s.size();
        int k=0;
        vector<int> ra(n), lcp(n);
        for (int i=0;i<n;i++) ra[sa[i]]=i;</pre>
        for (int i=0;i<n;i++) {
                if (k) k--;
                if (ra[i]==n-1) {
                         k=0;
                         continue;
                int j=sa[ra[i]+1];
                while (k< n\&\&s[(i+k)\%n] == s[(j+k)\%n]) k++;
                lcp[ra[i]]=k;
                if (ra[(sa[ra[i]]+1)%n]>ra[(sa[ra[j]]+1)%n]) k=0;
        return lcp;
```

### 11 src/string/suffixarray.cpp

```
// Suffix array in O(n log^2 n)
// ~300ms runtime for 10^5 character string, ~2000ms for 5*10^5
// You can change vector<int> s to string s
#include <bits/stdc++.h>
#define F first
#define S second
using namespace std;
vector<int> suffixArray(vector<int> s) {
        int n=s.size();
        vector<int> k(n);
        for (int i=0;i<n;i++) {</pre>
                k[i]=s[i];
        vector<pair<int, int>, int> > v(n);
        for (int t=1;t<=n;t*=2) {</pre>
                for (int i=0;i<n;i++) {
                         int u=-1;
                         if (i+t<n) u=k[i+t];</pre>
                         v[i] = \{ \{k[i], u\}, i\};
                sort(v.begin(), v.end());
                int c=0;
                for (int i=0;i<n;i++) {
                         if (i>0&&v[i-1].F!=v[i].F) c++;
                         k[v[i].S]=c;
                if (c==n-1) break;
        vector<int> sa(n);
        for (int i=0;i<n;i++) sa[k[i]]=i;</pre>
        return sa;
```

# $12 ext{ src/string/z.cpp}$

```
// Computes the Z array in linear time
// z[i] is the length of the longest common prefix of substring
// starting at i and the string
// You can use string s instead of vector<int> s
// z[0]=0
#include <bits/stdc++.h>
using namespace std;
vector<int> zAlgo(vector<int> s) {
        int n=s.size();
        vector<int> z(n);
        int 1=0;
        int r=0;
        for (int i=1;i<n;i++) {
                z[i]=max(0, min(z[i-l], r-i));
                while (i+z[i] < n \& s[z[i]] == s[i+z[i]]) z[i] ++;
                if (i+z[i]>r) {
                        l=i;
                        r=i+z[i];
        return z;
```

#### 13 src/geom/convexhull.cpp

```
// Computes the convex hull of given set of points in O(n \log n)
// Uses Andrew's algorithm
// The points on the edges of the hull are not listed
// Change > to >= in ccw function to list the points on the edges
#include <bits/stdc++.h>
#define X real()
#define Y imag()
using namespace std;
typedef long double ld;
typedef long long 11;
// Coordinate type
typedef 11 CT;
typedef complex<CT> co;
bool ccw(co a, co b, co c) {
        return ((c-a)*conj(b-a)).Y>0;
vector<co> convexHull(vector<co> ps) {
        auto cmp = [](co a, co b) {
                if (a.X==b.X)
                        return a.Y<b.Y;</pre>
                else {
                        return a.X<b.X;</pre>
        };
        sort(ps.begin(), ps.end(), cmp);
        ps.erase(unique(ps.begin(), ps.end()), ps.end());
        int n=ps.size();
        if (n<=2) return ps;
        vector<co> hull;
        hull.push_back(ps[0]);
        for (int d=0;d<2;d++) {
                if (d) reverse(ps.begin(), ps.end());
                int s=hull.size();
                for (int i=1;i<n;i++) {
                        while ((int)hull.size()>s&&!ccw(hull[hull.size()-2], hull.back(), ps[i]))
                                hull.pop_back();
                        hull.push_back(ps[i]);
        hull.pop_back();
        return hull;
```

#### 14 src/geom/basic.cpp

```
// Basic geometry functions using complex numbers
// Mostly copied from https://github.com/ttalvitie/libcontest/
/* Useful functions of std
        CT abs(co x): Length
        CT norm(co x): Square of length
        CT arg(co x): Angle
        co polar(CT length, CT angle): Complex from polar components
*/
#include <bits/stdc++.h>
#define X real()
#define Y imag()
using namespace std;
typedef long double ld;
typedef long long 11;
// Coordinate type
typedef ld CT;
typedef complex<CT> co;
// Return true iff points a, b, c are CCW oriented.
bool ccw(co a, co b, co c) {
        return ((c - a) * conj(b - a)).Y > 0;
// Return true iff points a, b, c are collinear.
// NOTE: doesn't make much sense with non-integer CT.
bool collinear(co a, co b, co c) {
        return ((c - a) * conj(b - a)).Y == 0;
// Rotate x with agle ang
co rotate(co x, CT ang) {
       return x*polar((CT)1, ang);
// Check whether segments [a, b] and [c, d] intersect.
// The segments must not be collinear. Doesn't handle edge cases (endpoint of
// a segment on the other segment) consistently.
bool intersects(co a, co b, co c, co d) {
        return ccw(a, d, b) != ccw(a, c, b) && ccw(c, a, d) != ccw(c, b, d);
// Interpolate between points a and b with parameter t.
co interpolate(CT t, co a, co b) {
        return a + t * (b - a);
// Return interpolation parameter between a and b of projection of v to the
// line defined by a and b.
```

```
// NOTE: no rounding behavior specified for integers.
CT projectionParam(co v, co a, co b) {
        return ((v - a) / (b - a)).X;
// Compute the distance of point v from line a..b.
// NOTE: Only for non-integers!
CT pointLineDistance(co p, co a, co b) {
        return abs(((p - a) / (b - a)).Y) * abs(b - a);
// Compute the distance of point v from segment a..b.
// NOTE: Only for non-integers!
CT pointSegmentDistance(co p, co a, co b) {
        co z = (p - a) / (b - a);
       if(z.X < 0) return abs(p - a);
        if(z.X > 1) return abs(p - b);
       return abs(z.Y) * abs(b - a);
// Return interpolation parameter between a and b of the point that is also
// on line c..d.
// NOTE: Only for non-integers!
CT intersectionParam(co a, co b, co c, co d) {
        co u = (c - a) / (b - a);
        co v = (d - a) / (b - a);
       return (u.X * v.Y - u.Y * v.X) / (v.Y - u.Y);
```

# $15 ext{ src/datastructure/fastmap.cpp}$

```
// Implements map operations for keys known in construction
// Undefined behavior when key doesn't exist
// O(n \log n) construction and O(\log n) access
#include <bits/stdc++.h>
using namespace std;
template<typename keyT, typename valueT>
struct FastMap {
        vector<keyT> keys;
        vector<valueT> values;
        FastMap(const vector<keyT>&ks) : keys(ks), values(ks.size()) {
                sort(keys.begin(), keys.end());
        valueT& operator[](keyT key) {
                auto it=lower_bound(keys.begin(), keys.end(), key);
                return values[it-keys.begin()];
        }
};
```

### 16 src/datastructure/treap.cpp

```
// Treap implementation with pointers
// Expected running time of split and merge is O(log n)
#include <bits/stdc++.h>
using namespace std;
typedef struct node* pnode;
struct node {
        pnode l,r;
        int pr,c;
        node() {
                1=0;
                r=0;
                c=1;
                pr=rand();
};
// Returns the size of the subtree t
int cnt(pnode t) {
        if (t) return t->c;
        return 0;
// Updates the size of the subtree t
void upd(pnode t) {
        if (t) t->c=cnt(t->1)+cnt(t->r)+1;
// Put lazy updates here
void push(pnode t) {
        if (t) {
                // Something
        }
// Merges trees l and r into tree t
void merg(pnode& t, pnode l, pnode r) {
        push(1);
        push(r);
        if (!1) t=r;
        else if(!r) t=1;
        else {
                if (l->pr>r->pr) {
                        merg(1->r, 1->r, r);
                        t=1;
                else {
                        merg(r->1, 1, r->1);
                        t=r;
```

```
upd(t);
// Splits tree t into trees l and r
// Size of tree l will be k
void split(pnode t, pnode& 1, pnode& r, int k) {
        if (!t) {
                1=0;
                r=0;
                return;
        else {
                push(t);
                if (cnt(t->1)>=k) {
                        split(t->1, 1, t->1, k);
                        r=t;
                else {
                        split(t->r, t->r, r, k-cnt(t->l)-1);
                        1=t;
        upd(t);
```