

Simulation Results steps

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1 First Step

Table 1: Benchmark used

| Benchmark | # qubits | # gates | two-qubit gates (%) |
|---------------------|----------|---------|---------------------|
| 4gt11 ₈₂ | 5 | 27 | 67 |

Table 2: Step 1 results after 100 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|------------|-----------|-------|
| No | No | 3000 | 3000 | 0.03 | 0.99 | 0.98879 | 390 |
| minextendrc | No | 3000 | 3000 | 0.03 | 0.96 | 0.9404637 | 1582 |
| minextendrc | Yes | 3000 | 3000 | 0.03 | 0.98 | 0.9675513 | 1038 |
| minextend | No | 3000 | 3000 | 0.03 | 0.98 | 0.944128 | 1264 |
| minextend | Yes | 3000 | 3000 | 0.03 | 0.98 | 0.9585909 | 834 |
| base | No | 3000 | 3000 | 0.03 | 0.97 | 0.92331 | 1062 |
| base | Yes | 3000 | 3000 | 0.03 | 0.98 | 0.9568084 | 780 |

Table 3: Other mapper statistics

| Mapper | Init. place | # qubits | depth | # gates | # SWAPS | # meet. in between |
|-------------|-------------|----------|-------|---------|---------|--------------------|
| No | No | 5 | 78 | 84 | 0 | 0 |
| minextendrc | No | 7 | 226 | 237 | 17 | 3 |
| minextendrc | Yes | 6 | 173 | 174 | 10 | 2 |
| minextend | No | 8 | 158 | 228 | 16 | 1 |
| minextend | Yes | 6 | 139 | 165 | 9 | 0 |
| base | No | 6 | 177 | 228 | 16 | |
| base | Yes | 6 | 130 | 147 | 7 | |

1.1 Routing comparison

1.1.1 No initial placement

With Resource constraints

```
1 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
2     path from source[1]=[2]
3     path from target[2]=[1->5] implying:
  ⇨ swap(q1,q5)
4 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=9
5     path from source[1]=[3]
6     path from target[2]=[2->0] implying:
  ⇨ swap(q2,q0)
7 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=20
8     path from source[3]=[4->7->5] implying:
  ⇨ swap(q4,q7) swap(q7,q5)
9     path from target[3]=[3->0->2] implying:
  ⇨ swap(q3,q0) swap(q0,q2)
10 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=9
11     path from source[1]=[0]
12     path from target[2]=[5->2] implying:
  ⇨ swap(q5,q2)
13 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=12
14     path from source[2]=[7->5] implying:
  ⇨ swap(q7,q5)
15     path from target[2]=[0->2] implying:
  ⇨ swap(q0,q2)
16 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=9
17     path from source[1]=[5]
18     path from target[2]=[0->2] implying:
  ⇨ swap(q0,q2)
19 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=9
20     path from source[1]=[5]
21     path from target[2]=[0->2] implying:
  ⇨ swap(q0,q2)
22 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
23     path from source[1]=[0]
24     path from target[2]=[5->2] implying:
  ⇨ swap(q5,q2)
25 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=13
26     path from source[2]=[0->2] implying:
  ⇨ swap(q0,q2)
27     path from target[2]=[7->5] implying:
  ⇨ swap(q7,q5)
28 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
29     path from source[1]=[2]
30     path from target[2]=[3->0] implying:
  ⇨ swap(q3,q0)
31 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
32     path from source[1]=[2]
33     path from target[2]=[3->0] implying:
  ⇨ swap(q3,q0)
34 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
35     path from source[1]=[7]
36     path from target[2]=[2->5] implying:
  ⇨ swap(q2,q5)
```

Without Resource constraints

```
1 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
2     path from source[1]=[2]
3     path from target[2]=[1->5] implying:
  ⇨ swap(q1,q5)
4 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=0
5     path from source[2]=[3->0] implying:
  ⇨ swap(q3,q0)
6     path from target[1]=[2]
7 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=9
8     path from source[3]=[4->1->5] implying:
  ⇨ swap(q4,q1) swap(q1,q5)
9     path from target[2]=[0->2] implying:
  ⇨ swap(q0,q2)
10 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=0
11     path from source[3]=[3->6->8] implying:
  ⇨ swap(q3,q6) swap(q6,q8)
12     path from target[1]=[5]
13 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
14     path from source[1]=[1]
15     path from target[2]=[8->5] implying:
  ⇨ swap(q8,q5)
16 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
17     path from source[1]=[1]
18     path from target[2]=[8->5] implying:
  ⇨ swap(q8,q5)
19 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
20     path from source[1]=[1]
21     path from target[2]=[8->5] implying:
  ⇨ swap(q8,q5)
22 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=10
23     path from source[1]=[8]
24     path from target[2]=[1->5] implying:
  ⇨ swap(q1,q5)
25 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=0
26     path from source[1]=[8]
27     path from target[2]=[2->6] implying:
  ⇨ swap(q2,q6)
28 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=8
29     path from source[1]=[8]
30     path from target[3]=[0->2->5] implying:
  ⇨ swap(q0,q2) swap(q2,q5)
31 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=4
32     path from source[1]=[8]
33     path from target[2]=[2->6] implying:
  ⇨ swap(q2,q6)
34 ... the minimally extending path with swaps is:
  ⇨ cycleExtend=2
35     path from source[2]=[1->5] implying:
  ⇨ swap(q1,q5)
36     path from target[1]=[8]
```

1.1.2 With initial placement

With Resource constraints

```

1 ... Virt2Real(v->r) ... result Virt2Real map of
  ↳ InitialPlace before adding unused virtual
  ↳ qubits and unused locations : (0->10)
  ↳ (1->4) (2->1) (3->5) (4->7) (5->2147483647)
  ↳ (6->2147483647) (7->2147483647)
  ↳ (8->2147483647) (9->2147483647)
  ↳ (10->2147483647) (11->2147483647)
  ↳ (12->2147483647) (13->2147483647)
  ↳ (14->2147483647) (15->2147483647)
  ↳ (16->2147483647)
2 ... Virt2Real(v->r) ... final result Virt2Real
  ↳ map of InitialPlace: (0->10) (1->4) (2->1)
  ↳ (3->5) (4->7) (5->0) (6->2) (7->3) (8->6)
  ↳ (9->8) (10->9) (11->11) (12->12) (13->13)
  ↳ (14->14) (15->15) (16->16)
3 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
4     path from source[1]=[4]
5     path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
6 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
7     path from source[1]=[4]
8     path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
9 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
10    path from source[1]=[4]
11    path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
12 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
13    path from source[1]=[10]
14    path from target[2]=[4->7] implying:
  ↳ swap(q4,q7)
15 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
16    path from source[1]=[10]
17    path from target[2]=[5->8] implying:
  ↳ swap(q5,q8)
18 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
19    path from source[2]=[10->8] implying:
  ↳ swap(q10,q8)
20    path from target[2]=[1->5] implying:
  ↳ swap(q1,q5)
21 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
22    path from source[1]=[8]
23    path from target[2]=[7->5] implying:
  ↳ swap(q7,q5)
24 ... the minimally extending path with swaps is:
  ↳ cycleExtend=12
25    path from source[2]=[4->1] implying:
  ↳ swap(q4,q1)
26    path from target[2]=[8->5] implying:
  ↳ swap(q8,q5)

```

Without Resource constraints

```

1 ... Virt2Real(v->r) ... result Virt2Real map of
  ↳ InitialPlace before adding unused virtual
  ↳ qubits and unused locations : (0->10)
  ↳ (1->4) (2->1) (3->5) (4->7) (5->2147483647)
  ↳ (6->2147483647) (7->2147483647)
  ↳ (8->2147483647) (9->2147483647)
  ↳ (10->2147483647) (11->2147483647)
  ↳ (12->2147483647) (13->2147483647)
  ↳ (14->2147483647) (15->2147483647)
  ↳ (16->2147483647)
2 ... Virt2Real(v->r) ... final result Virt2Real
  ↳ map of InitialPlace: (0->10) (1->4) (2->1)
  ↳ (3->5) (4->7) (5->0) (6->2) (7->3) (8->6)
  ↳ (9->8) (10->9) (11->11) (12->12) (13->13)
  ↳ (14->14) (15->15) (16->16)
3 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
4     path from source[1]=[4]
5     path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
6 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
7     path from source[1]=[4]
8     path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
9 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
10    path from source[1]=[4]
11    path from target[2]=[10->7] implying:
  ↳ swap(q10,q7)
12 ... the minimally extending path with swaps is:
  ↳ cycleExtend=10
13    path from source[1]=[10]
14    path from target[2]=[4->7] implying:
  ↳ swap(q4,q7)
15 ... the minimally extending path with swaps is:
  ↳ cycleExtend=0
16    path from source[1]=[10]
17    path from target[2]=[5->8] implying:
  ↳ swap(q5,q8)
18 ... the minimally extending path with swaps is:
  ↳ cycleExtend=8
19    path from source[1]=[10]
20    path from target[3]=[1->5->7] implying:
  ↳ swap(q1,q5) swap(q5,q7)
21 ... the minimally extending path with swaps is:
  ↳ cycleExtend=4
22    path from source[1]=[10]
23    path from target[2]=[5->8] implying:
  ↳ swap(q5,q8)
24 ... the minimally extending path with swaps is:
  ↳ cycleExtend=2
25    path from source[2]=[4->7] implying:
  ↳ swap(q4,q7)
26    path from target[1]=[10]

```

2 1000 iterations

Table 4: Step 1 results after 1000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|------------|------------|-------|
| No | No | 3000 | 3000 | 0.03 | 0.96 | 0.97823066 | 390 |
| minextendrc | No | 3000 | 3000 | 0.03 | 0.929 | 0.92937318 | 1582 |
| minextendrc | Yes | 3000 | 3000 | 0.03 | 0.939 | 0.94685216 | 1038 |
| minextend | No | 3000 | 3000 | 0.03 | 0.947 | 0.9312172 | 1264 |
| minextend | Yes | 3000 | 3000 | 0.03 | 0.949 | 0.94748374 | 834 |
| base | No | 3000 | 3000 | 0.03 | 0.932 | 0.906571 | 1062 |
| base | Yes | 3000 | 3000 | 0.03 | 0.9509 | 0.9459456 | 780 |

3 10000 iterations

Table 5: Step 1 results after 10000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|------------|-------------|-------|
| No | No | 3000 | 3000 | 0.03 | 0.961 | 0.980342528 | 390 |
| minextendrc | No | 3000 | 3000 | 0.03 | 0.9372 | 0.937136544 | 1582 |
| minextendrc | Yes | 3000 | 3000 | 0.03 | 0.9435 | 0.951650597 | 1038 |
| minextend | No | 3000 | 3000 | 0.03 | 0.9519 | 0.93665818 | 1264 |
| minextend | Yes | 3000 | 3000 | 0.03 | 0.9556 | 0.954629151 | 834 |
| base | no | 3000 | 3000 | 0.03 | 0.9417 | 0.9156453 | 1062 |
| base | yes | 3000 | 3000 | 0.03 | 0.953 | 0.95037428 | 780 |

3.1 Conclusions

3.1.1 Probability of success

Table 6: Probability of success difference between the number of iterations

| Mapper | Init. place | 100 it. | 1000 it. | 10000 it. | Diff 1000-100 | Diff 10000-1000 |
|-------------|-------------|---------|----------|-----------|---------------|-----------------|
| No | No | 0.99 | 0.96 | 0.961 | -0.0300 | 0.0010 |
| minextendrc | No | 0.96 | 0.929 | 0.9372 | -0.0310 | 0.0082 |
| minextendrc | Yes | 0.98 | 0.939 | 0.9435 | -0.0410 | 0.0045 |
| minextend | No | 0.98 | 0.947 | 0.9519 | -0.0330 | 0.0049 |
| minextend | Yes | 0.98 | 0.949 | 0.9556 | -0.0310 | 0.0066 |
| base | No | 0.97 | 0.932 | 0.9417 | -0.0380 | 0.0097 |
| base | Yes | 0.98 | 0.9509 | 0.953 | -0.0291 | 0.0021 |

Table 7: Mean value of the probability of success difference between number of iterations

| Iterations comparison | Mean diff |
|-----------------------|-----------|
| 1000-100 | -0.0333 |
| 10000-1000 | 0.0053 |

3.1.2 Fidelity

Table 8: Fidelity difference between the number of iterations

| Mapper | Init. place | 100 it. | 1000 it. | 10000 it. | Diff 1000-100 | Diff 10000-1000 |
|-------------|-------------|-----------|------------|-------------|---------------|-----------------|
| No | No | 0.98879 | 0.97823066 | 0.980342528 | -0.0106 | 0.0021 |
| minextendrc | No | 0.9404637 | 0.92937318 | 0.937136544 | -0.0111 | 0.0078 |
| minextendrc | Yes | 0.9675513 | 0.94685216 | 0.951650597 | -0.0207 | 0.0048 |
| minextend | No | 0.944128 | 0.9312172 | 0.93665818 | -0.0129 | 0.0054 |
| minextend | Yes | 0.9585909 | 0.94748374 | 0.954629151 | -0.0111 | 0.0071 |
| base | No | 0.92331 | 0.906571 | 0.9156453 | -0.0167 | 0.0091 |
| base | Yes | 0.9568084 | 0.9459456 | 0.95037428 | -0.0109 | 0.0044 |

Table 9: Mean value of the fidelity difference between number of iterations

| Iterations comparison | Mean diff |
|-----------------------|-----------|
| 1000-100 | -0.0134 |
| 10000-1000 | 0.0058 |

4 Simplest benchmarks results

Table 10: Benchmarks used

| Benchmark | # qubits | # gates |
|-------------------------|----------|---------|
| 4gt12 _{v189} | 6 | 228 |
| 4gt4 _{v072} | 6 | 258 |
| 4mod5 _{bdd287} | 7 | 70 |
| 4mod5 _{v020} | 5 | 20 |

4.1 4gt12-v1₈₉

Table 11: Results after 1000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|--------------|-------------------|-------|
| no | no | 3000 | 3000 | 0.005 | 0.768 | 0.66623522 | 2496 |
| minextendrc | no | 3000 | 3000 | 0.005 | 0.562 | 0.44841106 | 10548 |
| minextend | no | 3000 | 3000 | 0.005 | 0.601 | 0.40972458 | 9072 |
| base | no | 3000 | 3000 | 0.005 | 0.517 | 0.3581228 | 6414 |

Table 12: Other mapper statistics

| Mapper | Init. place | # qubits | depth | # gates | # SWAPS |
|-------------|-------------|----------|-------------|-------------|-----------|
| no | no | 6 | 416 | 658 | 0 |
| minextendrc | no | 9 | 1172 | 1360 | 78 |
| minextend | no | 9 | 1008 | 1549 | 99 |
| base | no | 6 | 1069 | 1423 | 85 |

4.2 4gt4-v0₇₂

Table 13: Results after 1000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|--------------|-------------------|-------|
| no | no | 3000 | 3000 | 0.005 | 0.786 | 0.68007548 | 2652 |
| minextendrc | no | 3000 | 3000 | 0.005 | 0.452 | 0.37749204 | 12168 |
| minextend | no | 3000 | 3000 | 0.005 | 0.498 | 0.34067243 | 7704 |
| base | no | 3000 | 3000 | 0.005 | 0.532 | 0.35703954 | 6336 |

Table 14: Other mapper statistics

| Mapper | Init. place | # qubits | depth | # gates | # SWAPS |
|-------------|-------------|----------|------------|-------------|-----------|
| no | no | 6 | 442 | 746 | 0 |
| minextendrc | no | 9 | 1352 | 1592 | 94 |
| minextend | no | 8 | 963 | 1736 | 110 |
| base | no | 6 | 1056 | 1547 | 89 |

4.3 4mod5-bdd₂₈₇

Table 15: Results after 1000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|--------------|-------------------|-------|
| no | no | 3000 | 3000 | 0.005 | 0.916 | 0.87474237 | 1029 |
| minextendrc | no | 3000 | 3000 | 0.005 | 0.753 | 0.65935538 | 3924 |
| minextend | no | 3000 | 3000 | 0.005 | 0.798 | 0.69281491 | 2988 |
| base | no | 3000 | 3000 | 0.005 | 0.776 | 0.67942877 | 2338 |

Table 16: Other mapper statistics

| Mapper | Init. place | # qubits | depth | # gates | # SWAPS |
|-------------|-------------|----------|------------|------------|-----------|
| no | no | 7 | 147 | 203 | 0 |
| minextendrc | no | 9 | 436 | 500 | 33 |
| minextend | no | 9 | 332 | 500 | 33 |
| base | no | 7 | 334 | 419 | 24 |

4.4 4mod5-v0₂₀

Table 17: Results after 1000 iterations

| Mapper | Init. place | t_1 | t_2 | meas. err. | p. success | f | V_Q |
|-------------|-------------|-------|-------|------------|--------------|------------------|-------|
| no | no | 3000 | 3000 | 0.005 | 0.985 | 0.97145968 | 265 |
| minextendrc | no | 3000 | 3000 | 0.005 | 0.944 | 0.9092329 | 1251 |
| minextend | no | 3000 | 3000 | 0.005 | 0.938 | 0.88981602 | 1024 |

Table 18: Other mapper statistics

| Mapper | Init. place | # qubits | depth | # gates | # SWAPS |
|-------------|-------------|----------|------------|------------|----------|
| no | no | 5 | 53 | 61 | 0 |
| minextendrc | no | 9 | 139 | 142 | 9 |
| minextend | no | 8 | 128 | 160 | 11 |