Simulation Results steps

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1 Simplest benchmarks results

Table 1: Benchmarks used

| Benchmark | # qubits | # gates |
|---|----------|---------|
| $4 gt 11_{82}$ | 5 | 27 |
| $4\mathrm{gt}12_{\mathrm{v}189}$ | 6 | 228 |
| $4\mathrm{gt}4_{\mathrm{v}072}$ | 6 | 258 |
| $4 \bmod 5_{\mathrm{bdd287}}$ | 7 | 70 |
| $4 \bmod 5_{\mathrm{v020}}$ | 5 | 20 |
| ${ m alu_{bdd288}}$ | 7 | 84 |
| $\mathrm{alu_{v027}}$ | 5 | 36 |
| $ m decod 24_{bdd294}$ | 6 | 73 |
| $ m decod 24_{enable 126}$ | 6 | 338 |
| ${ m graycode6_{47}}$ | 6 | 5 |
| $\mathrm{ham}3_{102}$ | 3 | 20 |
| $hwb4_{49}$ | 5 | 233 |
| $\bmod 10_{176}$ | 5 | 178 |
| $ mod 5 adder_{127} $ | 6 | 555 |
| $\mathrm{mod}5\mathrm{d}1_{63}$ | 5 | 22 |
| $mod8_{10177}$ | 6 | 440 |
| $\mathrm{one}_{\mathrm{twothreev199}}$ | 5 | 132 |
| $\mathrm{one}_{\mathrm{twothreev3101}}$ | 5 | 70 |
| $\rm rd32_{v066}$ | 4 | 34 |
| sf_{274} | 6 | 781 |
| sf_{276} | 6 | 778 |
| $\mathrm{sym}6_{145}$ | 7 | 3888 |
| $xor5_{254}$ | 6 | 7 |

$1.1 4gt11_{82}$

Table 2: Step 1 results after 1000 iterations

| Mapper | # qubits | depth | # gates | # SWAPS | p. success | f | V_Q |
|---------------|----------|------------------------|------------|---------|----------------------|------------|-------|
| No | 5 | 78 | 84 | 0 | 0.96 | 0.97823066 | 390 |
| minextendrc | 7 | 226 | 237 | 17 | 0.929 | 0.92937318 | 1582 |
| $\min extend$ | 8 | 158 | 228 | 16 | $\boldsymbol{0.947}$ | 0.9312172 | 1264 |
| base | 6 | 177 | 228 | 16 | 0.932 | 0.906571 | 1062 |

$1.2 ext{ } 4gt12-v1_{89}$

Table 3: Results after 1000 iterations

| Mapper | # qubits | depth | # gates | # SWAPS | p. success | f | V_Q |
|--------------------|----------|------------------------|---------|---------|------------|------------|-------|
| no | 6 | 416 | 658 | 0 | 0.768 | 0.66623522 | 2496 |
| minextendre | 9 | 1172 | 1360 | 78 | 0.562 | 0.44841106 | 10548 |
| $\min extend$ | 9 | 1008 | 1549 | 99 | 0.601 | 0.40972458 | 9072 |
| $_{\mathrm{base}}$ | 6 | 1069 | 1423 | 85 | 0.517 | 0.3581228 | 6414 |

$1.3 ext{ } 4\text{gt}4\text{-v}0_{72}$

Table 4: Results after 1000 iterations

| Mapper | # qubits | depth | # gates | # SWAPS | p. success | f | V_Q |
|---------------|----------|--------------------|---------------------|---------|----------------------|------------|-------|
| no | 6 | 442 | 746 | 0 | 0.786 | 0.68007548 | 2652 |
| minextendre | 9 | 1352 | 1592 | 94 | 0.452 | 0.37749204 | 12168 |
| \min extend | 8 | $\boldsymbol{963}$ | 1736 | 110 | 0.498 | 0.34067243 | 7704 |
| base | 6 | 1056 | $\boldsymbol{1547}$ | 89 | $\boldsymbol{0.532}$ | 0.35703954 | 6336 |

$1.4 \mod 5$ -bdd₂₈₇

Table 5: Results after 1000 iterations

| Mapper | # qubits | depth | # gates | # SWAPS | p. success | f | V_Q |
|---------------|----------|-----------|---------|------------|------------|------------|-------|
| no | 7 | 147 | 203 | 0 | 0.916 | 0.87474237 | 1029 |
| minextendre | 9 | 436 | 500 | 33 | 0.753 | 0.65935538 | 3924 |
| $\min extend$ | 9 | $\bf 332$ | 500 | 33 | 0.798 | 0.69281491 | 2988 |
| base | 7 | 334 | 419 | ${\bf 24}$ | 0.776 | 0.67942877 | 2338 |

$1.5 \quad 4 \bmod 5 \text{-v} 0_{20}$

Table 6: Results after 1000 iterations

| Mapper | # qubits | depth | # gates | # SWAPS | p. success | f | V_Q |
|---------------|----------|------------------------|---------|---------|----------------------|------------|-------|
| no | 5 | 53 | 61 | 0 | 0.985 | 0.97145968 | 265 |
| minextendrc | 9 | 139 | 142 | 9 | 0.944 | 0.9092329 | 1251 |
| \min extend | 8 | $\bf 128$ | 160 | 11 | 0.938 | 0.88981602 | 1024 |
| base | 6 | 133 | 119 | 8 | $\boldsymbol{0.947}$ | 0.89871898 | 714 |

$1.6 \quad alu_{\rm bdd288}$

Table 7: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|--------------------|----------|--------------------|---------|------------------------|------------|------------|-------|
| no | 7 | 247 | 0 | 165 | 0.94 | 0.89851036 | 1155 |
| minextendre | 8 | 571 | 36 | 495 | 0.847 | 0.78096707 | 3960 |
| $\min extend$ | 8 | 616 | 41 | 383 | 0.846 | 0.73109047 | 3064 |
| $_{\mathrm{base}}$ | 7 | $\boldsymbol{472}$ | 25 | 360 | 0.841 | 0.71637503 | 2520 |

$1.7 \quad alu_{v027}$

Table 8: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|------------|---------|------------------------|------------|------------|-------|
| no | 5 | 107 | 0 | 80 | 0.98 | 0.96369032 | 400 |
| minextendre | 9 | 278 | 19 | 248 | 0.959 | 0.92602273 | 2232 |
| $\min extend$ | 10 | 296 | 21 | 156 | 0.944 | 0.89032214 | 1560 |
| $_{ m base}$ | 6 | 278 | 19 | 214 | 0.915 | 0.84492332 | 1284 |

$1.8 \quad decod 24_{bdd 294}$

Table 9: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|---------|-------|------------|------------|-------|
| no | 6 | 207 | 0 | 144 | 0.938 | 0.91098461 | 864 |
| minextendrc | 9 | 441 | 26 | 407 | 0.888 | 0.7749599 | 3663 |
| \min extend | 7 | 468 | 29 | 328 | 0.816 | 0.73708015 | 2296 |
| base | 6 | 405 | 22 | 300 | 0.781 | 0.71803687 | 1800 |

$1.9 \quad decod 24_{enable 126}$

Table 10: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | $\overline{V_Q}$ |
|---------------|----------|---------------------|---------|------------------------|------------|------------|------------------|
| no | 6 | 978 | 0 | 612 | 0.894 | 0.74038417 | 3672 |
| minextendre | 9 | 2049 | 119 | 1788 | 0.831 | 0.57285276 | 16092 |
| \min extend | 10 | 2184 | 134 | 1440 | 0.805 | 0.50947313 | 14400 |
| base | 6 | $\boldsymbol{1959}$ | 109 | 1446 | 0.74 | 0.42630108 | 8676 |

$1.10 \quad {\rm graycode} 6_{47}$

Table 11: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|--------------------|----------|---------|---------|------------------------|------------|------------|-------|
| no | 6 | 21 | 0 | 32 | 0.995 | 0.99332325 | 192 |
| minextendre | 7 | 111 | 10 | 111 | 0.991 | 0.98223938 | 777 |
| $\min extend$ | 10 | 102 | 9 | 61 | 0.987 | 0.97012132 | 610 |
| $_{\mathrm{base}}$ | 6 | 84 | 7 | 82 | 0.991 | 0.98075312 | 492 |

$1.11 \quad ham 3_{102}$

Table 12: Results after 1000 iterations

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|--|----------|---------|---------|------------------------|------------|------------|-------|
| no | 3 | 61 | 0 | 60 | 0.987 | 0.98246387 | 180 |
| minextendrc | 4 | 115 | 6 | 127 | 0.971 | 0.95999051 | 508 |
| $\min \operatorname{ext} \operatorname{end}$ | 4 | 115 | 6 | 121 | 0.974 | 0.96288976 | 484 |
| base | 4 | 106 | 5 | 98 | 0.973 | 0.95944625 | 392 |

$1.12 \mod 10_{176}$

Table 13: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|-----------|------------------------|------------|------------|-------|
| no | 5 | 515 | 0 | 327 | 0.9 | 0.82976826 | 1635 |
| minextendre | 7 | 1199 | 76 | 1090 | 0.758 | 0.62105388 | 7630 |
| $\min extend$ | 10 | 1127 | 68 | 687 | 0.733 | 0.60641905 | 6870 |
| base | 6 | 983 | 52 | 734 | 0.697 | 0.56115058 | 4404 |

Table 14: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|--|------------|------------|
| no | 0.738 | 0.59602509 |
| minextendre | 0.453 | 0.31989048 |
| $\min \operatorname{ext} \operatorname{end}$ | 0.443 | 0.31320313 |
| base | 0.372 | 0.27839542 |

$1.13 \quad mod5 adder_{127}$

Table 15: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|----------------------------|----------|------------|---------|-------------|----------------------|------------|-------|
| no | 6 | 1583 | 0 | 944 | 0.71 | 0.45135226 | 5664 |
| minextendre | 9 | 3320 | 193 | 2878 | 0.491 | 0.1922222 | 25902 |
| $\operatorname{minextend}$ | 10 | 3779 | 244 | 2667 | 0.548 | 0.18165444 | 26670 |
| $_{\mathrm{base}}$ | 6 | $\bf 3248$ | 185 | 2378 | $\boldsymbol{0.591}$ | 0.18911191 | 14268 |

Table 16: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|----------------------------|------------|------------|
| no | 0.528 | 0.18188697 |
| minextendrc | 0.36 | 0.1484162 |
| $\operatorname{minextend}$ | 0.399 | 0.14349585 |
| base | 0.465 | 0.12694018 |

$1.14 \mod 5d1_{63}$

Table 17: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|---------|------------------------|------------|------------|-------|
| no | 5 | 69 | 0 | 59 | 0.989 | 0.98368741 | 295 |
| minextendrc | 8 | 195 | 14 | 209 | 0.958 | 0.93474128 | 1672 |
| $\min extend$ | 8 | 195 | 14 | 136 | 0.969 | 0.93997349 | 1088 |
| base | 6 | 195 | 14 | 146 | 0.95 | 0.91002595 | 876 |

Table 18: Results after 1000 iterations, $t_1=t_2=1000$

| Mapper | p. success | f |
|--|------------|------------|
| no | 0.97 | 0.95187372 |
| minextendre | 0.901 | 0.84099717 |
| $\min \operatorname{ext} \operatorname{end}$ | 0.914 | 0.83627787 |
| base | 0.892 | 0.7849484 |

$1.15 \mod 8_{10177}$

Table 19: Results after 1000 iterations, $t_1=t_2=3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | $\overline{V_Q}$ |
|---------------|----------|---------|---------|-------|------------|------------|------------------|
| no | 6 | 1270 | 0 | 794 | 0.858 | 0.70131629 | 4764 |
| minextendre | 10 | 2674 | 156 | 2275 | 0.52 | 0.39211003 | 22750 |
| $\min extend$ | 10 | 2827 | 173 | 1761 | 0.411 | 0.29686116 | 17610 |
| $_{ m base}$ | 6 | 2773 | 167 | 2006 | 0.335 | 0.26106507 | 12036 |

Table 20: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|---------------|------------|------------|
| no | 0.698 | 0.42021822 |
| minextendre | 0.244 | 0.19792409 |
| $\min extend$ | 0.123 | 0.14638911 |
| base | 0.068 | 0.16412249 |

$1.16 \quad one_{twothreev199}$

Table 21: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | $\overline{V_Q}$ |
|---------------|----------|---------|---------|------------------------|------------|------------|------------------|
| no | 5 | 383 | 0 | 256 | 0.832 | 0.78653106 | 1280 |
| minextendrc | 7 | 887 | 56 | 839 | 0.633 | 0.59855522 | 5873 |
| $\min extend$ | 10 | 869 | 54 | 530 | 0.729 | 0.62135956 | 5300 |
| base | 6 | 833 | 50 | 609 | 0.662 | 0.57083541 | 3654 |

Table 22: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|---------------|------------|------------|
| no | 0.602 | 0.55524768 |
| minextendre | 0.266 | 0.38317882 |
| $\min extend$ | 0.355 | 0.33820922 |
| base | 0.26 | 0.31493265 |

1.17 one_{twothreev3101}

Table 23: Results after 1000 iterations, $t_1=t_2=3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|---------|------------------------|------------|------------|-------|
| no | 5 | 203 | 0 | 143 | 0.937 | 0.88807716 | 715 |
| minextendre | 8 | 464 | 29 | 440 | 0.746 | 0.620299 | 3520 |
| $\min extend$ | 8 | 509 | 34 | $\bf 302$ | 0.732 | 0.63161506 | 2416 |
| base | 6 | 428 | 25 | 323 | 0.742 | 0.62081173 | 1938 |

Table 24: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|--|-------------|------------|
| no | 0.809 | 0.69629912 |
| minextendrc | 0.411 | 0.31374806 |
| $\min \operatorname{ext} \operatorname{end}$ | 0.391 | 0.31579028 |
| base | 0.42 | 0.31189591 |

$1.18 \quad rd32_{v066}$

Table 25: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|---------|------------------------|----------------------|------------|-------|
| no | 4 | 102 | 0 | 83 | 0.983 | 0.97241164 | 332 |
| minextendre | 7 | 219 | 13 | 195 | 0.947 | 0.91458844 | 1365 |
| $\min extend$ | 7 | 228 | 14 | ${\bf 142}$ | $\boldsymbol{0.958}$ | 0.91079208 | 994 |
| $_{ m base}$ | 5 | 219 | 13 | 169 | 0.955 | 0.90759692 | 845 |

Table 26: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|--|----------------------|------------|
| no | 0.95 | 0.9176419 |
| minextendre | 0.88 | 0.79475368 |
| $\min \operatorname{ext} \operatorname{end}$ | $\boldsymbol{0.902}$ | 0.77708902 |
| base | 0.896 | 0.77242986 |

$1.19 ext{ sf}_{274}$

Table 27: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------------------|------------|------------------------|----------------------|------------|-------|
| no | 6 | 2227 | 0 | 1359 | 0.484 | 0.34974095 | 8154 |
| minextendre | 7 | 5116 | 321 | 4515 | 0.0 | 0.16778098 | 31605 |
| \min extend | 10 | 5071 | 316 | $\boldsymbol{3007}$ | $\boldsymbol{0.097}$ | 0.14752778 | 30070 |
| base | 6 | $\boldsymbol{4450}$ | 247 | 3289 | 0.088 | 0.15461728 | 19734 |

Table 28: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|------------------------------|------------|------------|
| no | 0.108 | 0.16219308 |
| minextendre | 0.002 | 0.19857107 |
| $\min \operatorname{extend}$ | 0.0 | 0.1458942 |
| base | 0.0 | 0.14493197 |

$1.20 ext{ sf}_{276}$

Table 29: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | $\overline{V_Q}$ |
|-------------|----------|---------|---------|---------------------|----------------------|------------|------------------|
| no | 6 | 2224 | 0 | 1360 | 0.472 | 0.30846996 | 8160 |
| minextendre | 9 | 4852 | 292 | 4103 | 0.0 | 0.16746873 | 36927 |
| \min | 10 | 4807 | 287 | $\boldsymbol{2747}$ | $\boldsymbol{0.092}$ | 0.14342305 | 27470 |
| base | 6 | 4447 | 247 | 3280 | 0.089 | 0.13928494 | 19680 |

Table 30: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|------------------------------|------------|------------|
| no | 0.034 | 0.15718296 |
| minextendre | 0.0 | 0.22111901 |
| $\min \operatorname{extend}$ | 0.0 | 0.15992956 |
| base | 0.0 | 0.14842314 |

$1.21 \quad sym6_{145}$

Table 31: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|---------------|----------|---------|---------------------|-------|------------|------------|--------|
| no | 7 | 11185 | 0 | 6759 | 0.506 | 0.15429107 | 47313 |
| minextendre | 8 | 24658 | 1497 | 20984 | 0.513 | 0.22079977 | 167872 |
| \min extend | 10 | 25756 | 1619 | 14156 | 0.546 | 0.12489321 | 141560 |
| base | 7 | 21679 | $\boldsymbol{1166}$ | 15613 | 0.531 | 0.12176519 | 109291 |

Table 32: Results after 1000 iterations, $t_1 = t_2 = 1000$

| Mapper | p. success | f |
|--|------------|------------|
| no | 0.513 | 0.1407412 |
| minextendre | 0.518 | 0.24438143 |
| $\min \operatorname{ext} \operatorname{end}$ | 0.543 | 0.1533595 |
| base | 0.53 | 0.14274046 |

$1.22 \quad xor 5_{254}$

Table 33: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | # qubits | # gates | # SWAPS | depth | p. success | f | V_Q |
|--|----------|---------|---------|-------|------------|------------|-------|
| no | 6 | 23 | 0 | 36 | 0.995 | 0.99375935 | 216 |
| minextendre | 7 | 68 | 5 | 75 | 0.984 | 0.9736118 | 525 |
| $\min \operatorname{ext} \operatorname{end}$ | 7 | 68 | 5 | 58 | 0.958 | 0.94092446 | 406 |
| base | 6 | 104 | 9 | 92 | 0.942 | 0.91559086 | 552 |

Table 34: Results after 1000 iterations, $t_1 = t_2 = 3000$

| Mapper | p. success | f |
|--|------------|------------|
| no | 0.984 | 0.97720823 |
| minextendre | 0.952 | 0.91998206 |
| $\min \operatorname{ext} \operatorname{end}$ | 0.896 | 0.84674549 |
| $_{\mathrm{base}}$ | 0.837 | 0.77312906 |

2 Correlation and Plots

Pearson correlation formula:

$$\rho_{X,Y} = \frac{\text{cov}(X,Y)}{\sigma_X \sigma_Y}$$

2.1 $t_1 = 3000$

Table 35: Pearson correlation coefficient for decoherence time of $t_1=3000$ and measurement error 0f 0.005

| | # of Gates | # of SWAPs | Depth | V_Q |
|----------------|------------|------------|------------------------|---------|
| $\rho_{f,Y}$ | -0.9360 | -0.8614 | -0.9091 | -0.8728 |
| $\rho_{p_s,Y}$ | -0.9257 | -0.8700 | -0.9060 | -0.8680 |

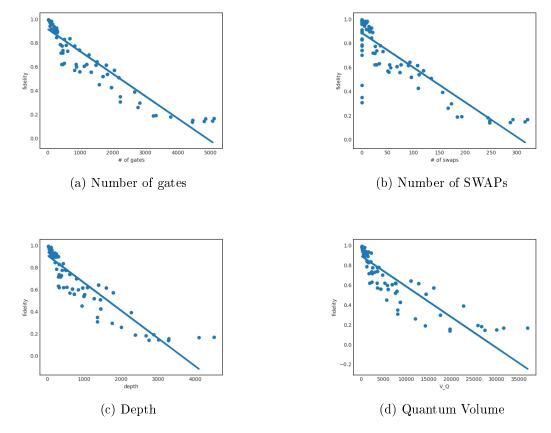


Figure 1: Plotting fidelity against number of gates, swaps, depth and Quantum Volume

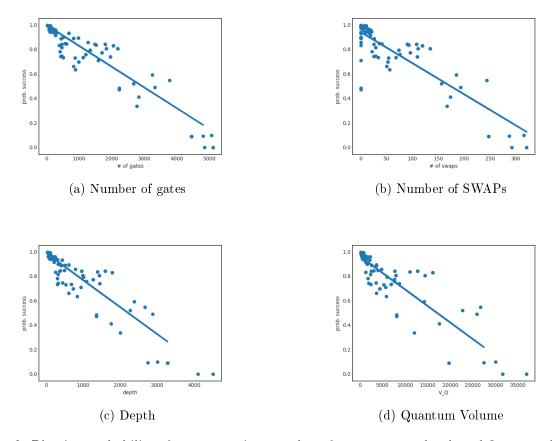


Figure 2: Plotting probability of success against number of gates, swaps, depth and Quantum Volume

2.1.1 Two-qubit gates

2.2 $t_1 = 1000$

Table 36: Pearson correlation coefficient for decoherence time of $t_1 = 1000$ and measurement error 0f 0.005

| | # of Gates | # of SWAPs | Depth | V_Q |
|---------------|------------|------------|------------------------|---------|
| $\rho_{f,Y}$ | -0.7637 | -0.6658 | -0.7354 | -0.7029 |
| $ ho_{p_s,Y}$ | -0.8341 | -0.7484 | -0.8076 | -0.7686 |

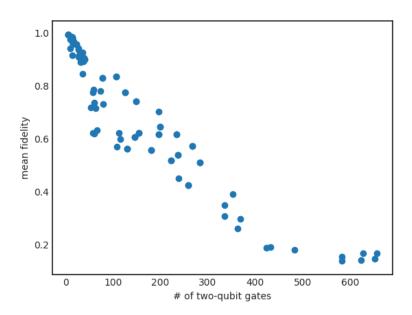


Figure 3: Number of two-qubit gates against fidelity

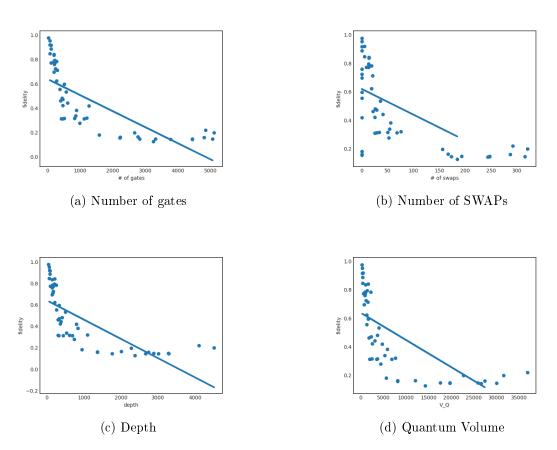


Figure 4: Plotting fidelity against number of gates, swaps, depth and Quantum Volume

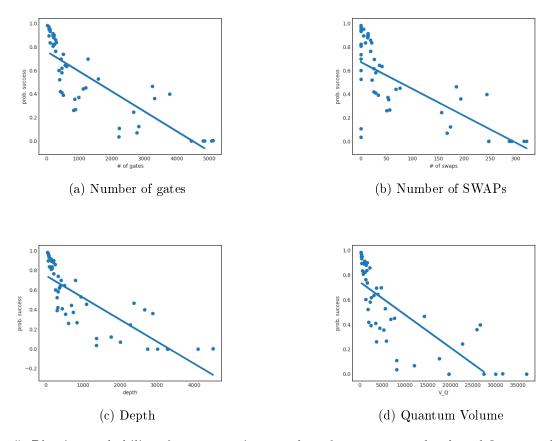


Figure 5: Plotting probability of success against number of gates, swaps, depth and Quantum Volume

2.2.1 Two-qubit gates

2.3 No measurement error and $t_1 = 3000$

Table 37: Pearson correlation coefficient for decoherence time of $t_1 = 3000$ and probability 0 for the measurement

| | # of Gates | # of SWAPs | Depth | V_Q |
|---------------|------------|------------|------------------------|---------|
| $\rho_{f,Y}$ | -0.9246 | -0.8482 | -0.9012 | -0.8697 |
| $ ho_{p_s,Y}$ | -0.9495 | -0.8972 | -0.9334 | -0.8985 |

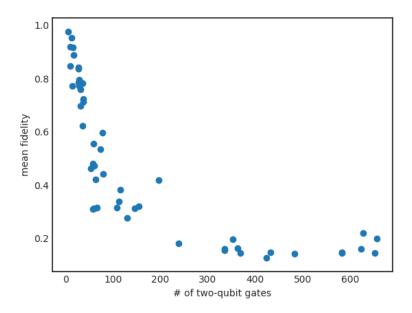


Figure 6: Number of two-qubit gates against fidelity

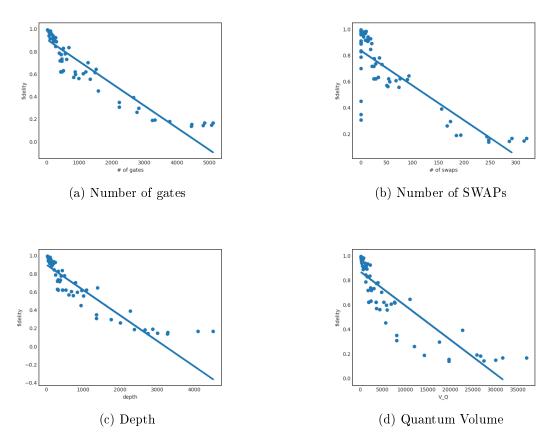


Figure 7: Plotting fidelity against number of gates, swaps, depth and Quantum Volume

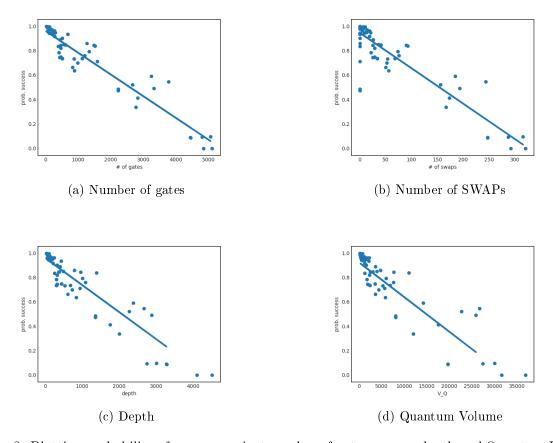


Figure 8: Plotting probability of success against number of gates, swaps, depth and Quantum Volume

2.3.1 Two-qubit gates analysis

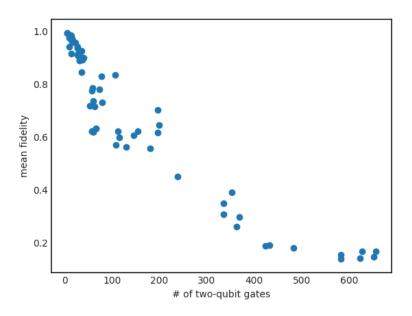


Figure 9: Number of two qubit gates against fidelity