

$$2) 25^{75^{10}} \bmod 36$$

$$k = 75^{10}$$

$$\varphi(36) = 12$$

$$k = 12h + b$$

$$k = 75^{10} \Rightarrow b = 75^{10} \bmod 12$$

$$\varphi(12) = \varphi(2^2) \cdot \varphi(3) = 4$$

$$15^{2 \cdot 4 + 2} \bmod 12 = 15^2 \bmod 12$$

$$b = 15^2 \bmod 12 = 9 \bmod 12$$

$$x = 25^9 \bmod 36$$

$$9_{10} = 1001_2$$

$$1 \quad 1 \quad 1 \quad 25 \quad 25$$

$$0 \quad 25 \quad 625 \quad 625 \quad 73$$

$$0 \quad 73 \quad 169 \quad 169 \quad 25$$

$$1 \quad 25 \quad 625 \quad 75625 \quad 1$$

$$1) \varphi(15) = \varphi(5) \cdot \varphi(3) = 4 \cdot 2 = 8$$

$$\varphi(2002) = \varphi(2) \cdot \varphi(7) \cdot \varphi(71) \cdot \varphi(13) = 6 \cdot 6 \cdot 70 \cdot 12 = 720$$

$$\varphi(20) = \varphi(2^2) \cdot \varphi(5) = 2 \cdot 4 = 8$$

$$\varphi(10) = \varphi(2) \cdot \varphi(5) = 4$$

$$\varphi(36) = \varphi(2^2) \cdot \varphi(3^2) = 12$$



$$3. \quad 36^{20+15} \bmod 2002 \equiv 36^{35} \bmod 2002.$$

$$35_{10} = \overline{100011}_2$$

$$d_i \quad ( \quad C^2 \quad C^2, d_i, d. \quad C^2, d_i, d \bmod k.$$

$$1 \quad 1 \quad 1 \quad 36 \quad 36$$

$$0 \quad 36 \quad 1296 \quad 1296 \quad 1296.$$

$$0 \quad 1296 \quad 1679616 \quad 1679616 \quad 1940$$

$$0 \quad 1940 \quad 3763600 \quad 3763600 \quad 1842.$$

$$1 \quad 1842 \quad 3392964 \quad 122146404 \quad 680$$

$$1. \quad 680 \quad 462400 \quad 16846400 \quad 7772.$$

$$2) \quad 25^{30} \bmod 36.$$