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**Exercise 21.23** - Consider the three transactions  $T_1$ ,  $T_2$ , and  $T_3$ , and the schedules  $S_1$  and  $S_2$  given below. Draw the serializability (precedence) graphs for  $S_1$  and  $S_2$  and state whether each schedule is serializable or not. If a schedule is serializable, write down <u>all</u> of the equivalent serial schedule(s). If a schedule is not serializable, write down <u>all</u> cycles.

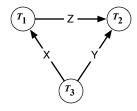
 $T_1$ :  $r_1(X)$ ;  $r_1(Z)$ ;  $w_1(X)$ 

 $T_2$ :  $r_2(Z)$ ;  $r_2(Y)$ ;  $w_2(Z)$ ;  $w_2(Y)$ 

 $T_3$ :  $r_3(X)$ ;  $r_3(Y)$ ;  $w_3(Y)$ 

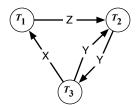
 $S_1$ :  $r_1(X)$ ;  $r_2(Z)$ ;  $r_1(Z)$ ;  $r_3(X)$ ;  $r_3(Y)$ ;  $w_1(X)$ ;  $w_3(Y)$ ;  $r_2(Y)$ ;  $w_2(Z)$ ;  $w_2(Y)$ 

 $S_2$ :  $r_1(X)$ ;  $r_2(Z)$ ;  $r_3(X)$ ;  $r_1(Z)$ ;  $r_2(Y)$ ;  $r_3(Y)$ ;  $w_1(X)$ ;  $w_2(Z)$ ;  $w_3(Y)$ ;  $w_2(Y)$ 



 $S_1$  Serializable:

$$T_3 \rightarrow T_1 \rightarrow T_2$$



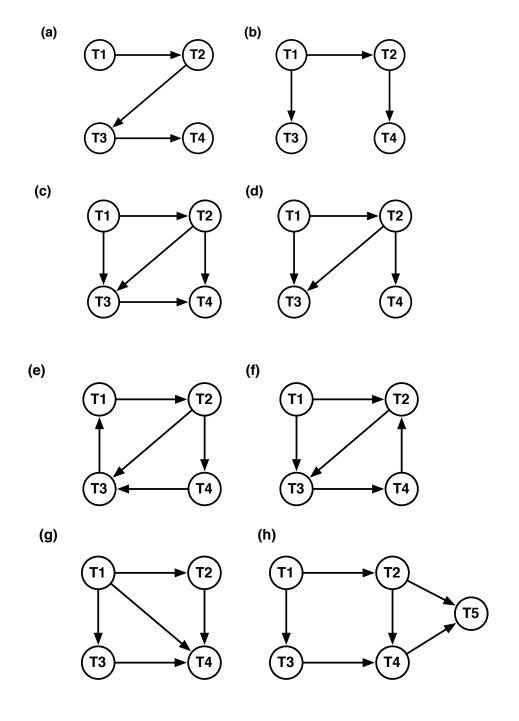
*S*<sub>2</sub> Non-Serializable:

Cycle:  $Z(T_1 \rightarrow T_2)$ ;  $Y(T_2 \rightarrow T_3)$ ;  $X(T_3 \rightarrow T_1)$ 

Cycle:  $Y(T_2 \rightarrow T_3)$ ;  $Y(T_3 \rightarrow T_2)$ 

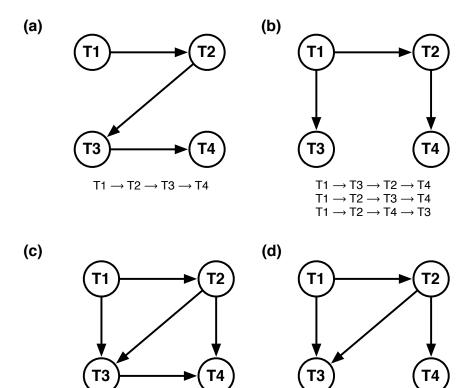
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Here are some precedence graphs that have already been drawn. They are simplified in that they do not indicate the database item in conflict for each edge. If a schedule is serializable, write down <u>all</u> of the equivalent serial schedule(s). If a schedule is not serializable, write down <u>all</u> cycles.



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#### **Answers:**

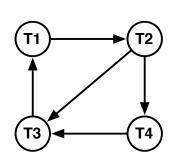


 $T1 \to T2 \to T3 \to T4$ 

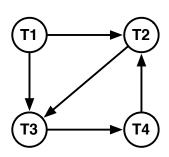
 $\begin{array}{c} T1 \longrightarrow T2 \longrightarrow T3 \longrightarrow T4 \\ T1 \longrightarrow T2 \longrightarrow T4 \longrightarrow T3 \end{array}$ 

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(e)



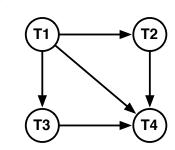
**(f)** 



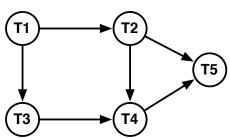
Cycle:  $(T1 \rightarrow T2)$ ,  $(T2 \rightarrow T3)$ ,  $(T3 \rightarrow T1)$ 

Cycle: (T2→T3), (T3→T4), (T4→T2)

(g)



(h)



 $T1 \to T2 \to T3 \to T4$ 

 $T1 \to T3 \to T2 \to T4$ 

 $\begin{array}{c} T1 \longrightarrow T3 \longrightarrow T2 \longrightarrow T4 \longrightarrow T5 \\ T1 \longrightarrow T2 \longrightarrow T3 \longrightarrow T4 \longrightarrow T5 \end{array}$