04_homework2

Randy 2/4/2021

BIOS7721 Homework2

Introduction

- dataset contains 500 patients
- human tissue valve in aortic position
- subcoronary implantation (SI) or root replacement (RR)
- followed over time and longitudinal aortic gradient measurements
- at risk of experiencing death following their surgery

```
aort <- here::here("aort_new.csv") %>%
  read_csv() %>%
  janitor::clean_names()

## aort data is in longitudial form
## each row is for one visit
## one subject has many visit
# View(aort)
```

Question1. Survival analysis with a time-varying covariate

a. create the start/stop time data set

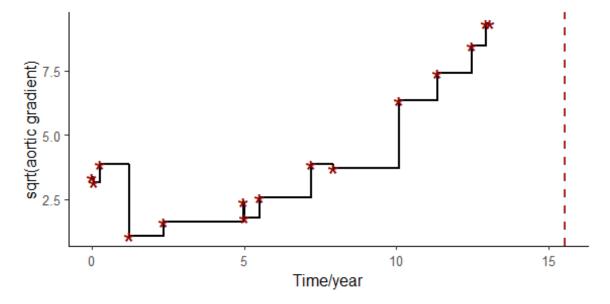
- the beginning of a time interval represents a measurement time
- the end of the final time window represents the survival time
- You also need a new status indicator
- indicator value of 0 for all intervals
- the last indicator is 1 if an event is observed
- the last indicator is 0 if a patient is censored
- print the rows for Patients 1 and 2.

```
aort1 <- aort %>%
  ## tmerge cannot bear duplicate id
  filter(time == 0) %>%
  ## time based merge for survial data
  survival::tmerge(
   data1 = .,
   data2 = .,
   id = id,
    ## the tdc and event use
   ## the final value in the data
    ## 4 types of operational arguments:
   ## tdc/cumtdc/event/cumevent
   death = event(survtime, event)) %>%
  ## start stop death added
  survival::tmerge(
   data1 = .,
   data2 = aort,
   id = id,
   sqrt_aort_grad = tdc(time, sqrt(aort_grad))) %>%
  ## given time, sqrt_aort_grad added
```

id	tstart	tstop	death	sqrt_aort_grad	oper	sex
1	0.0000000	0.7504862	0	2.077925	SI	Male
1	0.7504862	1.8606248	0	1.909819	SI	Male
2	0.0000000	3.2322893	0	2.872840	SI	Male
2	3.2322893	3.8214459	0	2.535935	SI	Male
2	3.8214459	4.7061867	0	5.235966	SI	Male
2	4.7061867	5.3569110	0	4.049932	SI	Male
2	5.3569110	5.6207138	0	4.250990	SI	Male
2	5.6207138	6.6390331	0	4.405298	SI	Male
2	6.6390331	6.8962116	0	4.795410	SI	Male
2	6.8962116	7.8946465	0	4.006678	SI	Male
2	7.8946465	8.7633751	0	4.948445	SI	Male
2	8.7633751	9.4291267	0	7.366542	SI	Male
2	9.4291267	9.8154872	0	5.797056	SI	Male
2	9.8154872	10.7623612	0	6.578867	SI	Male
2	10.7623612	11.0586943	0	7.638576	SI	Male
2	11.0586943	12.0011893	0	7.368440	SI	Male
2	12.0011893	12.6317556	0	9.113807	SI	Male

b. for patient 3 create a stepped line plot

- square root aortic gradient
- vertical dashed line for patient's observed survival time



c. fit an extended Cox survival model

- square root aortic gradient as a time-varying covariate
- operation type and sex as a time-independent baseline covariate
- interpret the coefficient estimates
- how it is the different from model with only the baseline values?

Based on the model below, the aortic gradient level can significantly affect the subject's survival status (p << 0.001). On average, one unit increase on the sqrt of aortic gradient can increase the risk of event to 1.5 folds (95% CI 1.39 1.62).

After adjusted for the biomarker aortic gradient, the effect of operation type on survival becomes highly significant (in cox1 model, p < 0.01), and effect size of exp(operation) changes from 0.95 fold to 0.67; given patient's aort gradient level, the operation SI has stronger effects on survival improvement for certain patients.

Also the adjustment of biomarker flips the effect of gender, from increasing risk of event to decreasing risk of event, even though neither of model shows significant gender effect on patients' survival status.

Overall the model performance gets improved in model cox1 (AIC = 2284), of which AIC decreased, comparing to the baseline value model cox0 (AIC = 2400).

```
summary(cox0)
## Call:
## coxph(formula = survobj ~ oper + sex, data = aort1)
    n= 4183, number of events= 243
##
               coef exp(coef) se(coef)
                                          z Pr(>|z|)
## operSI -0.05155 0.94976 0.13087 -0.394
                                                0.694
## sexMale 0.02349 1.02377 0.12983 0.181
##
          exp(coef) exp(-coef) lower .95 upper .95
## operSI 0.9498 1.0529 0.7349 1.227
## sexMale 1.0238 0.9768 0.7938 1.320
## Concordance= 0.501 (se = 0.021 )
## Likelihood ratio test= 0.2 on 2 df,
                                         p = 0.9
## Wald test = 0.2 on 2 df,
                                        p=0.9
## Score (logrank) test = 0.2 on 2 df, p=0.9
summary(cox1)
## coxph(formula = survobj ~ oper + sex + sqrt_aort_grad, data = aort1)
```

```
## n= 4183, number of events= 243
##
                 coef exp(coef) se(coef) z Pr(>|z|)
-0.40736 0.66541 0.13574 -3.001 0.00269 **
##
## operSI
## sexMale
                 ## sqrt_aort_grad 0.40747 1.50301 0.03847 10.591 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
                   exp(coef) exp(-coef) lower .95 upper .95
                      0.6654
## operSI
                                  `1.5028 0.510
                                                     0.8682
## sexMale
                      0.8656
                                  1.1553
                                             0.669
                                                       1.1200
## sqrt_aort_grad 1.5030
                                  0.6653
                                             1.394
                                                       1.6207
## Concordance= 0.63 (se = 0.023)
## Likelihood ratio test= 117.4 on 3 df, p=<2e-16
## Wald test = 112.3 on 3 df, p=<2e-16
## Score (logrank) test = 115 on 3 df, p=<2e-16
```

```
rbind(glance0, glance1) %>%
  tibble() %>%
  rownames_to_column("model") %>%
  mutate(model = c("cox0", "cox1")) %>%
  dplyr::select(model, AIC, BIC, logLik) %>%
  knitr::kable("simple", align = "c")
```

model	AIC	BIC	logLik
cox0	2399.754	2406.741	-1197.877
cox1	2284.523	2295.002	-1139.261

d. comment on why it is not appropriate of the extended Cox model

The extended Cox model assumptions is only valid for exogenous time dependent covariates. However in this case, the aortic gradient level is a endogenous biomarker, the level of which cannot be predetermined or totally immune to measurement errors. Hence there is no way we will not know the future status of this variable, the feature of which we have no idea with. If we treat it as the exogenous variable, we would assume that the aortic gradient changes only at the measurement times and remain constant between two measurements, as step-function approximation, which is obvious highly impossible in the real world. Therefore, extended Cox model is not appropriate, or at least not the optimal method.

Question2. Two stage model

a. fit a mixed effects model

- · outcome: square root aortic gradient
- fixed effects: linear time, operation type, and sex
- random effects: intercept and linear slope for time
- interpret the coefficient estimates from this model

```
lme1 <- nlme::lme(sqrt_aort_grad ~</pre>
                   oper + sex + tstart,
                  random = (\sim 1 + tstart \mid id),
                 data = aort1)
summary(lme1)
## Linear mixed-effects model fit by REML
## Data: aort1
         AIC
                  BIC
##
                         logLik
    12225.41 12276.11 -6104.703
##
## Random effects:
## Formula: ~1 + tstart | id
## Structure: General positive-definite, Log-Cholesky parametrization
               StdDev
## (Intercept) 0.9339484 (Intr)
## tstart 0.1750445 -0.147
## Residual 0.8455028
## Fixed effects: sqrt_aort_grad ~ oper + sex + tstart
                  Value Std.Error
                                    DF t-value p-value
## (Intercept) 2.2863387 0.08294554 3682 27.56434 0.0000
## operSI 0.7374438 0.09190882 497 8.02365 0.0000
             0.0397345 0.09183342 497 0.43268 0.6654
## sexMale
## tstart
             0.3379494 0.01052127 3682 32.12060 0.0000
## Correlation:
         (Intr) operSI sexMal
##
## operSI -0.600
## sexMale -0.579 0.042
## tstart -0.165 0.001 -0.002
## Standardized Within-Group Residuals:
##
                      01
                                 Med
## -3.152709486 -0.592187596 0.006059147 0.601982291 4.206817111
##
## Number of Observations: 4183
## Number of Groups: 500
```

As seen in model lme1, time has a very highly significant effect on the level of aortic gradient level (p << 0.001); on average, the patients will suffer an increase the subject's sqrt aortic gradient level 0.33 unit yearly. Operation type SI also has a significant effect on this biomarker, which can increase sqrt aortic gradient 0.737 unit on sqrt level compare to RR. There is some variability for each patient baseline aortic gradient level, showing as $sd_{intercept} = 0.934$, and the random linear time effects $sd_{intercept} = 0.175$. The random intercept and random slope are not strongly related with each other (Corr = -0.15). We can see that the variability for within individual is still pretty high time to time.

b. the mixed effects model as subject-specific predictions

- the contributions from the random intercept and random slope
- use as a time-varying covariate in a Cox survival model
- Cox model includes operation type and sex as time independent baseline covariates
- interpret the coefficient estimates from this model

```
## why this is subject specific?
## this is marginal, right?
## The uncertainty in our estimates
## from the first stage are not carried
## through to the second stage
aort1$sqrt_aort_pred <- c(predict(lme1))
head(aort1) %>% knitr::kable("simple", align = "c")
```

id	tstart	tstop	death	sqrt_aort_grad	oper	sex	survobj	sqrt_aort_pred
1	0.0000000	0.7504862	0	2.077925	SI	Male	(0.0000000,0.7504862+]	2.217513
1	0.7504862	1.8606248	0	1.909819	SI	Male	(0.7504862,1.8606248+]	2.475283
2	0.0000000	3.2322893	0	2.872840	SI	Male	(0.0000000,3.2322893+]	2.219919
2	3.2322893	3.8214459	0	2.535935	SI	Male	(3.2322893,3.8214459+]	3.692635
2	3.8214459	4.7061867	0	5.235966	SI	Male	(3.8214459,4.7061867+]	3.961070
2	4.7061867	5.3569110	0	4.049932	SI	Male	(4.7061867,5.3569110+]	4.364181

```
cox2 <- coxph(survobj ~
              oper + sex + sqrt_aort_pred,
            data = aort1,
            x = TRUE
tidy2 <- tidy(cox2) %>%
 tibble() %>%
 mutate(model = "two-stage")
glance2 <- glance(cox2)</pre>
summary(cox2)
## Call:
## coxph(formula = survobj ~ oper + sex + sqrt aort pred, data = aort1,
##
##
   n= 4183, number of events= 243
##
##
##
                   coef exp(coef) se(coef)
                                             z Pr(>|z|)
          ## operSI
## sexMale
## sqrt_aort_pred 0.35229 1.42232 0.04475 7.872 3.5e-15 ***
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##
               exp(coef) exp(-coef) lower .95 upper .95
          0.6934 1.4422 0.5296 0.9078
## operSI
## sexMale
                  0.8948
                            1.1176
                                   0.6919
                                              1.1573
## sqrt_aort_pred 1.4223
                            0.7031
                                   1.3029
                                              1.5527
##
## Concordance= 0.597 (se = 0.02)
## Likelihood ratio test= 63.46 on 3 df,
## Wald test
                   = 62.09 on 3 df,
                                       p = 2e - 13
## Score (logrank) test = 63.01 on 3 df,
```

As shown in model cox2, the aortic gradient level can significantly affect the subject's survival status (p << 0.001). On average, one unit increase on the sqrt of aortic gradient can increase the risk of event to 1.422 folds (95% CI 1.30 1.55).

After adjusted for the biomarker aortic gradient, the effect of operation type on survival becomes highly significant (p << 0.01); given patient's aort gradient level, the operation SI has significant benefit effects (p < 0.001) to lower the risk to 0.69 fold (95% CI: 0.530, 0.908) than RR . Also the gender still has no significant gender effect on patients' survival status. Overall the

model performance does not get obviously improved in model cox2 (AIC = 2338.5), of which AIC decreased, comparing to the baseline value model cox1 (AIC = 2284.5).

```
rbind(glance1, glance2) %>%
  tibble() %>%
  rownames_to_column("model") %>%
  mutate(model = c("cox1", "cox2")) %>%
  dplyr::select(model, AIC, BIC, logLik) %>%
  knitr::kable("simple", align = "c")
```

model	AIC	BIC	logLik
cox1	2284.523	2295.002	-1139.261
cox2	2338.493	2348.972	-1166.247

c. bootstrap

- compute the standard errors for Cox component of the two-stage model
- the differences from the standard errors estimated in the model2?
- reasons of differences between two methods for inference?

Overall the two-stage model results is pretty closed to the boostrap results. For two-stage model, the estimates are obtained by fitting the corresponding mixed model using the observed responses up to given time from all subjects still at risk. It will not take the error terms from the first mixed model to the survival model. Hence by using the assumed real endogenous biomarker level, the method will underestimate the standard error for the coefficient. Hence, there will be a bias for the implementation that remove all the measurement errors then predicted by empirical Bayesian; also the partial likelihood asymptotic feature will no hold anymore. Therefor the bootstrapping results should be more reliable and less biased, and larger standard errors (difference below 0.0010) and confidence interval on the endogenous time-dependent variable.

```
set.seed(55555)
#' get_coef() to extract the coef from one bootstrap
#' @param data the dataset for bootstrap
#' @param indices a placeholder for the map function
#' @return the coefs from the model fitting
#' @examples
#' get_coef(aort1, 1)
get_coef <- function(data, indices) {</pre>
  data1 <- data %>%
    ## put all the same id in one group
    group_by(id) %>%
    ## put the data frame in the tibble
    nest() %>%
    ## just make sure nested
    as.data.frame()
  ## resample 500 id for data2
  index <- sample(1:nrow(data1),</pre>
                  size = nrow(data1),
                  replace =TRUE)
  ## get the new dataset
  data2 <- data1[index, ] %>%
    ## remove the old id
    select(-id) %>%
    ## build up the new id
    rownames_to_column("id") %>%
    unnest()
  ## longitudinal model for two stage
  lmm <- lme(sqrt aort grad ~</pre>
               oper + sex + tstart,
             random = (~ 1 + tstart | id),
             data = data2)
  data2$sqrt_aort_pred <- c(predict(lmm))</pre>
  ## survival model for two stage
  fit1 <- coxph(survobj ~</pre>
                  oper + sex + sqrt_aort_pred,
               data = data2)
  ## the coef from two stage as tibble
  return(coef(fit1))
```

term	estimate	boot.estimate	std.error	boot.std.error
operSI	-0.3661550	-0.3559587	0.1374833	0.1329524
sexMale	-0.1111559	-0.1120138	0.1312380	0.1219880
sqrt_aort_pred	0.3522863	0.3399614	0.0447545	0.0449749

d. comparision

- the two-stage model and the time-varying covariate model
- comment on any differences
- why these differences may exist

Overall these two models are pretty similar to each other. Comparatively, the two-stage model has smaller estimate value and larger standard error; the two stage model can reduce bias compared to the Cox extended model. However, the overall performance of two-stage model is superior than the extended model; this might due to the individual biomarker level varies in a large range within subjects (possible larger than the between-subject variations). This information of error residual variability in the mixed model is not passed into the Cox proportional hazard model, which might cause the ill performance of two-stage model. More flexible functions like polynomial or spline can improve the performance for the two-stage model.

The Cox extended model uses step function approximation for the time dependent covariate, assuming measured without error. This may introduce bias to the estimates and standard error. These difference demonstrate the attenuation in the regression coefficients of the cox analysis due to the measurement error.

```
rbind(tidy1, tidy2) %>%
  dplyr::select(model, everything()) %>%
  arrange(term) %>%
  knitr::kable("simple", align = "c")
```

model	term	estimate	std.error	statistic	p.value
cox-ex	operSI	-0.4073591	0.1357360	-3.0011132	0.0026899
two-stage	operSI	-0.3661550	0.1374833	-2.6632697	0.0077385
cox-ex	sexMale	-0.1443701	0.1314674	-1.0981437	0.2721417
two-stage	sexMale	-0.1111559	0.1312380	-0.8469797	0.3970064
cox-ex	sqrt_aort_grad	0.4074694	0.0384742	10.5907213	0.0000000
two-stage	sqrt_aort_pred	0.3522863	0.0447545	7.8715308	0.0000000