

K nearest neighbour algorithm:-

rating = 4.2, audience = 4.5

Index	rating	audience (in millions)	Genre
1	4.5	5	Action
2	3.8	2	Comedy
3	4.9	6	Action
4	2.9	1	Drama
5	3.2	3	Comedy
6	4.0	4	Drama
7	2.9	1.5	Comedy
8	3.7	2.5	Action

For k=3

$$\sqrt{(4.2-5)^2 + (4.5-5)^2} = 0.943$$

~~$$\sqrt{(4.2-3.8)^2 + (4.5-2)^2}$$~~

$$\sqrt{(4.2-3.8)^2 + (4.5-2)^2} = 2.5962.532$$

$$\sqrt{(4.2-4.9)^2 + (4.5-6)^2} = 1.655$$

$$\sqrt{(4.2-2.5)^2 + (4.5-1)^2} = 3.891$$

$$\sqrt{(4.2 - 3.2)^2 + (4.5 - 3)^2} = 1.803$$

$$\sqrt{(4.2 - 4)^2 + (4.5 - 4)^2} = 0.539$$

$$\sqrt{(4.2 - 2.9)^2 + (4.5 - 1.5)^2} = \cancel{3.17} \quad 3.269$$

$$\sqrt{(4.2 - 3.7)^2 + (4.5 - 2.5)^2} = 2.062$$

For $k=3$

\Rightarrow Movie ID = 6, 1, 3

Genre = Comedy, Action, Action

\therefore Genre for the new rating
and audience at $k=3$ is Action

K means algorithm:-

Customer ID	Annual Income (in \$1000s)	Spending Score (1-100)
1	19	39
2	16	81
3	17	6
4	18	77
5	19	40
6	20	76
7	21	6
8.	22	94
9	23	3
10	24	72

$$k_1 = 19, 39 \quad k_2 = 16, 81$$

$$\text{for } ③ = \sqrt{(17-19)^2 + (39-6)^2} = 33.06$$

$$\sqrt{(17-16)^2 + (6-81)^2} = 75.0$$

$$k_1 = \frac{15+17}{2}, \frac{39+6}{2} = 16, 22.5$$

$$k_1 = 16, 22.5 \quad k_2 = 16, 81$$

$$\begin{aligned} ④ &= \sqrt{(18-16)^2 + (22.5-77-22.5)^2} = 54.54 \\ &\sqrt{(18-16)^2 + (77-81)^2} = 4.47 \end{aligned}$$

$$k_2 = \frac{16+18}{2}, \frac{81+77}{2}$$

$$k_2 = 17, 79$$

$$k_1 = 16, 22.5, k_2 = 17, 79$$

$$\text{for } ③ = \sqrt{(19-16)^2 + (40-22.5)^2} = 17.76$$

$$\sqrt{(19-17)^2 + (40-79)^2} = 39.09$$

$$k_1 = \frac{16+19}{2}, \frac{40+22.5}{2}$$

$$k_1 = 17.5, 31.25$$

$$\text{for } ④ = \sqrt{(20-17.5)^2 + (76-31.25)^2} = 44.82$$

$$\sqrt{(20-17)^2 + (76-79)^2} = 4.24$$

$$k_2 = \frac{20+17}{2}, \frac{76+79}{2}$$

$$k_2 = 18.5, 77.5$$

$$k_1 = 17.5, 31.25, k_2 = 18.5, 77.5$$

$$\text{for } ⑤ = \sqrt{(21-17.5)^2 + (6-31.25)^2} = 29.49$$

$$\sqrt{(18.5)^2 + (21-18.5)^2 + (6-77.5)^2} = 71.54$$

$$k_1 = \frac{21+17.5}{2}, \frac{6+31.25}{2}$$

$$k_1 = 19.25, 18.63$$

$$k_1 = 19.29, 18.63 \quad k_2 = 18.9, 77.9$$

$$\text{for } ⑧ = \sqrt{(22-19.29)^2 + (94-18.63)^2} = 79.42$$

$$\sqrt{(22-18.9)^2 + (94-77.9)^2} = 16.87$$

$$k_2 = \frac{22+18.5}{2}, \frac{94+77.9}{2}$$

$$k_2 = 20.25, 85.75$$

$$k_1 = 19.29, 18.63 \quad k_2 = 20.25, 85.75$$

$$\text{for } ⑨ = \sqrt{(23-19.29)^2 + (3-18.63)^2} = 16.07$$

$$\sqrt{(23-20.25)^2 + (3-85.75)^2} = 82.80$$

$$k_1 = \frac{23+19.29}{2}, \frac{3+18.63}{2}$$

$$k_1 = 21.13, 10.82$$

$$k_1 = 21.13, 10.82 \quad k_2 = 20.25, 85.75$$

$$\text{for } ⑩ = \sqrt{(24-21.13)^2 + (72-10.82)^2} = 61.25$$

$$\sqrt{(24-20.25)^2 + (72-85.75)^2} = 14.25$$

$$k_1 = \{1, 3, 4, 9, 7, 9\}$$

$$k_2 = \{2, 6, 8, 10\}$$

Decision Trees:-

Dataset:-

<u>PersonID</u>	<u>Age</u>	<u>Income</u>	<u>Student</u>	<u>Bought Car</u>
1	<30	High	No	No
2	<30	High	No	No
3	31-40	High	No	Yes
4	>40	Medium	No	Yes
5	>40	Low	Yes	No
6	>40	Low	Yes	Yes
7	31-40	Low	Yes	Yes
8	<30	Medium	No	No
9	<30	Low	Yes	Yes
10	>40	Medium	Yes	Yes
11	<30	Medium	Yes	Yes
12	31-40	Medium	No	Yes
13	31-40	High	Yes	Yes
14	>40	Medium	No	Yes

$$P_f = \frac{9}{14}$$

Bought Car:-

$$P_f = \frac{9}{14}$$

$$P_{\bar{f}} = \frac{5}{14}$$

$$\text{Entropy} = -\left(\frac{9}{14}\right) \log_2\left(\frac{9}{14}\right) - \left(\frac{5}{14}\right) \log_2\left(\frac{5}{14}\right)$$

$$= 0.940$$

Dye :-

~~R = 375~~ ~~R = 275~~

$$C_{30} = -\frac{2}{5} * \log_2\left(\frac{2}{5}\right) - \frac{3}{5} \log_2\left(\frac{3}{5}\right).$$

≈ 0.971

$$31-40 = -\frac{0}{4} \log_2\left(\frac{0}{4}\right) - \frac{4}{4} \log_2\left(\frac{4}{4}\right)$$

$$>40 = -\frac{3}{5} \log_2\left(\frac{3}{5}\right) - \frac{2}{5} \log_2\left(\frac{2}{5}\right)$$

≈ 0.971

Weighted Entropy :-

$$\frac{5}{14}(0.971) + \frac{4}{14}(0) + \frac{5}{14}(0.971) = 0.693$$

$$IG \text{ for Dye} = 0.94 - 0.693 = 0.247$$

Income :-

High :-

$$-\frac{2}{5} \log_2\left(\frac{2}{5}\right) - \frac{3}{5} \log_2\left(\frac{3}{5}\right) = 0.971$$

Medium :-

$$-\frac{1}{5} \log_2\left(\frac{1}{5}\right) - \frac{4}{5} \log_2\left(\frac{4}{5}\right) = 0.722$$

$$Low = -\frac{2}{4} \log_2\left(\frac{2}{4}\right) - \frac{2}{4} \log_2\left(\frac{2}{4}\right) = 1$$

Weighted Entropy :-

$$\frac{S(0.971)}{14} + \frac{S(0.722)}{14} + \frac{4(1)}{14} = 0.836$$

IG for Income :-

$$0.940 - 0.836 = 0.10$$

Student :-

Yes :-

$$\frac{-2}{8} \log_2 \left(\frac{2}{8} \right) - \frac{6}{8} \log_2 \left(\frac{6}{8} \right) = 0.811$$

No :-

$$\frac{-3}{6} \log_2 \left(\frac{3}{6} \right) - \frac{3}{6} \log_2 \left(\frac{3}{6} \right) = 1$$

$$\frac{8}{14}(0.811) + \frac{6}{14}(1) = 0.892$$

$$0.940 - 0.892 = 0.048$$

Highest IG for age for Dge

Age :-

Age < 30 :

No: 2

Yes: 3

impure ; next attribute

Age 31-40:

No = 0

Yes = 4

consists of only
one class

Age > 40:

No: 3

Yes: 2

impure; next attribute

Age < 30 & Income = High

Boys No: 2

Yes: 3

< 30

Age ~~< 30~~ & Income = Medium

Yes: 2

∴ Pure

Age ~~> 40~~ < 30 & Income = Low

Yes: 1

Pure

$Dye > 40 \wedge Income = Medium$

Yes: 2 \therefore Pure

$Dye > 40 \wedge Income = Low$

Yes = 2
No = 3 \therefore Not Pure

