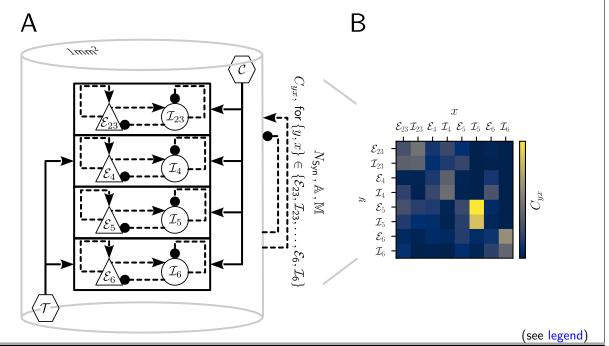
Detailed description of the cortical microcircuit model (Potjans et al., 2014)

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1 Model description

	Summary
Populations	8 cortical populations in 4 layers (L2/3, L4, L5, L6), driven by a thalamic population (\mathcal{T}) and cortico-cortical inputs (\mathcal{C})
Connectivity	random, independent, population specific
Neuron model	cortex: leaky integrate-and-fire (LIF); thalamus, cortico-cortical inputs: Poisson point process
Synapse model	exponential postsynaptic currents with static, normally distributed weights and delays
Predictions	population specific spiking activity



Populations								
Name	Elements	Size						
$x \in \{\mathcal{E}_{23}, \mathcal{E}_4, \mathcal{E}_5, \mathcal{E}_6, \mathcal{I}_{23}, \mathcal{I}_4, \mathcal{I}_5, \mathcal{I}_6\}$	LIF	N_x						
$\mathcal{P} = \bigcup_{x} x$	LIF	$N = \sum_x N_x$ (see re-						
		$\max \frac{1}{1}$						
\mathcal{T}	realizations of Poisson point process	$N_{\mathcal{T}}$						
$C = \bigcup_x C_x$	population specific currents	$N = \sum_{x} N_x$						

Table 1: Description of the network model (continued on next page).

Connectivity							
Source	Target	Pattern					
$x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$	$y \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$						
		$ullet$ random, fixed total number K_{yx} of connections $ullet$ (see remark 1)					
		$ullet$ synaptic weights J_{ij} ($orall i\in y, j\in x$)					
		$ullet$ spike-transmission delays d_{ij} $(orall i\in y, j\in x)$					
\mathcal{T}	$y \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$						
		$ullet$ random, fixed total number $K_{y\mathcal{T}}$ of connections 1					
		$ullet$ synaptic weights J_{ij} ($orall i\in y, j\in \mathcal{T}$)					
		$ullet$ spike-transmission delays d_{ij} $(orall i \in y, j \in \mathcal{T})$					
C_y	$y \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$						
		• one-to-one ²					

Connectivity patterns:

$$K_{yx} = \frac{\ln\left(1 - C_{yx}\right)}{\ln\left(1 - \left(N_x N_y\right)^{-1}\right)},$$

connections between a source population x of size N_x and a target population y of size N_y . C_{yx} denotes the connection probability. Sources and targets are randomly and independently drawn from x and y with replacement. Multiple connections between two neurons and self-connections are permitted (\mathbb{M}, \mathbb{A}) .

² one-to-one (δ) : Each neuron in the source population is connected to one corresponding neuron in the target population (bijection).

(see "Network sketch" above and Senk et al., 2022)

Table 1: Description of the network model (continued).

 $^{^{\}rm 1}$ random, fixed total number ($N_{\rm Syn})\!\!:$ This rule establishes a total number of

Neurons								
Cortical neurons								
Туре	leaky integrate-and-fire (LIF)							
Description	dynamics of membrane potential $V_i(t)$ and spiking activity $s_i(t)$ of neuron $i \in x$ for $x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$:							
	$ullet$ emission of k th $(k=1,2,\ldots)$ spike of neuron i at time t_i^k if							
	$V_i\left(t_i^k ight) \geq heta$							
	with spike threshold $ heta$							
	reset and refractoriness:							
	$orall k, \; orall t \in \left[t_k^i, t_k^i + au_{ref} ight]: V_i(t) = V_{reset}$							
	with refractory period $ au_{ref}$ and reset potential V_{reset}							
	$ullet$ spike train $s_i(t) = \sum_k \delta(t-t_i^k)$							
	$ullet$ subthreshold dynamics of membrane potential $V_i(t)$:							
	$\forall k, \ \forall t \notin \left[t_i^k, t_i^k + \tau_{ref}\right):$							
	$\tau_{\rm m} \frac{\mathrm{d}V_i(t)}{\mathrm{d}t} = \left[E_{\rm L} - V_i(t) \right] + R_{\rm m} I_i(t) \tag{1}$							
	with membrane time constant $ au_{\rm m}$, membrane resistance $R_{\rm m}$, resting potential $E_{\rm L}$, and total synaptic input current $I_i(t)$							
	Thalamic neurons							
Туре	Poisson point process							
Description	spike trains $s_i(t)$ ($i\in\mathcal{T}$) modeled as independent realizations of Poisson point process with piece-wise constant rate							
	$ u_{\mathcal{T}}(t) = u_{\mathcal{T}} \cdot (\Theta(t - t_{start}) - \Theta(t - t_{stop}))$							
	Cortico-cortical inputs							
Туре	constant (direct) currents (DC)							
Description	population specific constant input current of magnitude							
	$I_{\mathcal{C}_x} = K_{\mathcal{C}_x} \cdot I_{\mathcal{C}} (\forall x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}),$							
	with cortico-cortical in-degree $K_{\mathcal{C}_x}$, and mean current							
	$I_{\mathcal{C}} = u_{\mathcal{C}} \cdot ar{I} \cdot au_{s}$							
	generated by a Poissonian spike train with rate $\nu_{\mathcal{C}}$, convolved with an exponential kernel with amplitude \bar{I} and time constant $\tau_{\rm s}$ (see remark 2)							

Table 2: Description of the network model (continued).

	Synapses
Туре	exponential postsynaptic currents with static weights and delays
Description	$ullet$ total synaptic input current $I_i(t)$ to neuron i $ig(orall i\in y\in\{\mathcal{E}_{23},\dots,\mathcal{I}_6\}ig)$ is governed
	by:
	$\left(\frac{d}{dt} + \frac{1}{\tau_{s}}\right) I_i(t) = f_i(t) \tag{2}$
	with superposition from all neurons $j \in x, \ \forall x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6, \mathcal{T}, \mathcal{C}\}$
	$f_i(t) = \sum_{x} \sum_{j} f_{ij}(t) = \sum_{x} \sum_{j} \hat{I}_{ij} s_j(t - d_{ij})$
	of weighted spike trains with static synaptic weigths \hat{I}_{ij} , synaptic time constant $ au_{\rm s}$, and spike transmission delays d_{ij}
	• solution of (2) for $f_{ij}(t) = \hat{I}_{ij}s_j(t)$ and $I_{ij}(t=0) = 0$:
	$PSC_{ij}(t) = \hat{I}_{ij} \exp(-t/ au_{s})\Theta(t)$
	with Heaviside function $\Theta(\cdot)$
	\sim (exponential decaying) posynaptic current triggered by a single presynaptic spike
	• solution of (1) for $I_i(t) = PSC_{ij}(t)$, $V_i(t=0) = 0$, and $E_L = 0$:
	$PSP_{ij}(t) = \hat{I}_{ij} R_m \frac{\tau_s}{\tau_s - \tau_m} \left(e^{-t/\tau_s} - e^{-t/\tau_m} \right) \Theta(t)$
	PSC amplitude (synaptic weight):
	$\hat{I}_{ij} = rac{J_{ij}}{J_{unit}(au_{m}, au_{s}, R_{m})}$
	parameterized by PSP amplitude $J_{ij} = max_t ig(PSP_{ij}(t)ig)$
	with unit PSP amplitude (PSP amplitude for $\hat{I}_{ij}=1$):
	$J_{\rm unit}(\tau_{\rm m},\tau_{\rm s},R_{\rm m}) = R_{\rm m} \frac{\tau_{\rm s}}{\tau_{\rm s}-\tau_{\rm m}} \left(\left[\frac{\tau_{\rm m}}{\tau_{\rm s}} \right]^{-\tau_{\rm m}/(\tau_{\rm m}-\tau_{\rm s})} - \left[\frac{\tau_{\rm m}}{\tau_{\rm s}} \right]^{-\tau_{\rm s}/(\tau_{\rm m}-\tau_{\rm s})} \right)$
	and time to PSP maximum:
	$t_{max} = \frac{\tau_{s} \tau_{m}}{\tau_{m} - \tau_{s}} \ln \left(\frac{\tau_{m}}{\tau_{s}} \right)$

Table 3: Description of the network model (continued).

	Synapses (continued)
Description	
	synaptic weights
	$\hat{I}_{ij} = \begin{cases} \max(0, z_{yx}), & j \in x \in \{\mathcal{E}_{23}, \mathcal{E}_4, \mathcal{E}_5, \mathcal{E}_6, \mathcal{T}\} \\ \min(0, z_{yx}), & j \in x \in \{\mathcal{I}_{23}, \mathcal{I}_4, \mathcal{I}_5, \mathcal{I}_6\} \\ \bar{I}_{yx}, & j \in x = \mathcal{C} \end{cases}$
	with $z_{yx} \sim \mathcal{N}\left\{ar{I}_{yx},\ \sigma_{s,yx}^2 ight\}$
	drawn from a normal distribution with mean $ar{I}_{yx}$, variance $\sigma^2_{s,yx}$
	note: clipping of synaptic weights leads to a deviation of the total number of synapses with non-zero weights from K_{yx} (see "Connectivity")
	distributed synaptic delays
	$d_{ij} = egin{cases} max(d_{min}, z_x), & j \in x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6, \mathcal{T}\} \ ar{d}_x, & j \in x = \mathcal{C} \end{cases}$
	with $z_x \sim \mathcal{N}\left\{ar{d}_x,\sigma_{d,x}^2 ight\}$
	drawn from a normal distribution with mean \bar{d}_x , variance $\sigma^2_{{\bf d},x}$, and minimal delay $d_{\min}>0$
	Initial conditions
Туре	random initial membrane potentials and homogeneous initial synaptic currents
Description	$ullet$ membrane potentials $V_i(t=0) \sim \mathcal{N}(ar{V}_{0,x},\sigma^2_{ extsf{v},x})$
	randomly and independently drawn from a normal distribution with mean $\bar{V}_{0,x}$ and variance $\sigma^2_{v,x}$ ($\forall i \in x \in \{\mathcal{E}_{23},\dots,\mathcal{I}_6\}$; see remark 3)

Table 4: Description of the network model (continued).

ullet synaptic currents: $I_i(t=0)=0\,\mathrm{pA}$ $(\forall i\in y\in\{\mathcal{E}_{23},\ldots,\mathcal{I}_6\})$

2 Model parameters

				men		connect	ivity			
					Populati	ion sizes				
	x	\mathcal{E}_{23}	\mathcal{I}_{23}	\mathcal{E}_4	\mathcal{I}_4	\mathcal{E}_5	\mathcal{I}_5	\mathcal{E}_6	\mathcal{I}_6	\mathcal{T}
	N_x	20,683	5,834	21,915	5,479	4,850	1,065	14,395	2,948	902
Connection probabilities C_{yx}										
	x	\mathcal{E}_{23}	\mathcal{I}_{23}	\mathcal{E}_4	\mathcal{I}_4	\mathcal{E}_5	\mathcal{I}_5	\mathcal{E}_6	\mathcal{I}_6	\mathcal{T}
	$\frac{y}{\mathcal{E}_{23}}$	0.1009	0.1689	0.0437	0.0818	0.0323	0.0	0.0076	0.0	0.0
	\mathcal{I}_{23}	0.1346	0.1371	0.0316	0.0515	0.0755	0.0	0.0042	0.0	0.0
	\mathcal{E}_4	0.0077	0.0059	0.0497	0.1350	0.0067	0.0003	0.0453	0.0	0.0983
	\mathcal{I}_4	0.0691	0.0029	0.0794	0.1597	0.0033	0.0	0.1057	0.0	0.0619
	\mathcal{E}_5	0.1004	0.0622	0.0505	0.0057	0.0831	0.3726	0.0204	0.0	0.0
	\mathcal{I}_5	0.0548	0.0269	0.0257	0.0022	0.0600	0.3158	0.0086	0.0	0.0
	\mathcal{E}_6	0.0156	0.0066	0.0211	0.0166	0.0572	0.0197	0.0396	0.2252	0.0512
	\mathcal{I}_6	0.0364	0.0010	0.0034	0.0005	0.0277	0.0080	0.0658	0.1443	0.0196
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E_{L} T_{m} C_{m}	$-50\mathrm{mV}$ $-65\mathrm{mV}$ $10\mathrm{ms}$ $250\mathrm{pF}$	$=40\mathrm{M}\Omega$	spik rest mer mer	ke thresho ting poten mbrane ti mbrane ca	old ntial me consta apacitance	ant				
$ heta$ E_{L} $ au_{m}$ C_{m} R_{m} V_{reset}	$\begin{array}{c} -50\mathrm{mV} \\ -65\mathrm{mV} \\ 10\mathrm{ms} \\ 250\mathrm{pF} \\ \tau_\mathrm{m}/C_\mathrm{m} \end{array}$	$=40\mathrm{M}\Omega$	spik rest mei mei mei rese	ke thresho ting poten mbrane ti mbrane ca mbrane re	old ntial me consta apacitance esistance al	ant e				
EL m m m m m reset	$\begin{array}{c} -50{\rm mV} \\ -65{\rm mV} \\ 10{\rm ms} \\ 250{\rm pF} \\ \tau_{\rm m}/C_{\rm m} \\ -65{\rm mV} \\ 2{\rm ms} \\ 0.5{\rm ms} \end{array}$	$=40\mathrm{M}\Omega$	spik rest mei mei mei rese abs	we thresholding potential mbrane cambrane reset potential colute refractsynaptic	old me consta apacitance esistance al actory per	ant e riod ime const	cant			
\mathcal{G} E_{L} C_{m} R_{m} V_{reset} V_{res}	$\begin{array}{c} -50{\rm mV} \\ -65{\rm mV} \\ 10{\rm ms} \\ 250{\rm pF} \\ \tau_{\rm m}/C_{\rm m} \\ -65{\rm mV} \\ 2{\rm ms} \end{array}$	$=40\mathrm{M}\Omega$	spik rest mei mei mei rese abs	ke thresho ting poten mbrane ti mbrane ca mbrane re et potenti olute refra	old me consta apacitance esistance al actory per	ant e riod ime const	cant			
EL Tm Cm Rm Vreset Tref	$\begin{array}{c} -50{\rm mV} \\ -65{\rm mV} \\ 10{\rm ms} \\ 250{\rm pF} \\ \tau_{\rm m}/C_{\rm m} \\ -65{\rm mV} \\ 2{\rm ms} \\ 0.5{\rm ms} \end{array}$	$=40\mathrm{M}\Omega$	spik rest mer mer mer abs	we thresholding potential mbrane cambrane reset potential colute refractsynaptic	old me consta apacitance esistance al actory per current t mic neuro	ant e riod ime const	cant			
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$egin{array}{ll} eta & E_{L} & & & & & \\ \hline egin{array}{ll} \mathcal{F}_{m} & & & & & \\ \mathcal{F}_{m} & & & & & \\ \mathcal{F}_{reset} & & & & \\ \mathcal{F}_{reset} & & & & \\ \mathcal{F}_{reset} & & & & \\ \mathcal{F}_{start} & & & & \\ \Delta t_{\mathcal{T}} & & & & \\ \mathcal{F}_{stop} & & & & \\ \mathcal{F}_{stop} & & & & \\ \mathcal{F}_{c} & & & \\ \mathcal{F}_{c} & & & & \\ \mathcal{F}_{c} & & & \\ \mathcal$	$\begin{array}{c} -50\mathrm{mV} \\ -65\mathrm{mV} \\ 10\mathrm{ms} \\ 250\mathrm{pF} \\ \tau_\mathrm{m}/C_\mathrm{m} \\ -65\mathrm{mV} \\ 2\mathrm{ms} \\ 0.5\mathrm{ms} \\ 120\mathrm{s}^{-1} \\ 700\mathrm{ms} \\ 10\mathrm{ms} \\ t_\mathrm{start} + \Delta \\ 8\mathrm{s}^{-1} \end{array}$	$I = 40 \mathrm{M}\Omega$	spik rest mer mer mer rese abs pos rate star dur ms stop rate	mbrane time of the of cortice of cortice of cortice an amplituation and manufacture of the of the of cortice of cortice of cortice of an amplitude of the of cortice an amplitude of the of cortice of an amplitude of the of cortice of an amplitude of the of cortice of cortice of an amplitude of the of cortice of cortice of cortice of an amplitude of the of cortice of cortice of cortice of the of cortice of cortice of cortice of cortice of cortice of the of cortice of the office of the	me constance al actory per thalamic interpretal thalamic incorporation of DC and actory per thalamic interpretal thalamic interpretal thalamic incorporation of DC and actory per thalamic interpretal thalamic incorporation of DC and actory per thalamic incorporation of DC actory per tha	ant e riod ime const ons input input input l inputs C inputs				
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Table 5: Model parameters (continued on next page).

Synapse										
Name	Value		Description							
J	0.15 mV		(mean) weight (PSP amplitude) of excitatory synapses							
\bar{I}_{yx}		synaptic w	eights:							
	$J/J_{\rm unit} \approx 87$	7.81 pA	$x \in \{\mathcal{E}_{23}, a\}$	$\mathcal{E}_4, \mathcal{E}_5, \mathcal{E}_6, \mathcal{E}_6$	$\mathcal{T}, \mathcal{C}\}$					
	$-4J/J_{unit}$		$x \in \{\mathcal{I}_{23}, \mathcal{I}_{23}, \mathcal{I}$	$\mathcal{I}_4, \mathcal{I}_5, \mathcal{I}_6$, except fo	r:				
	$2J/J_{unit}$		$(x,y) = (\delta$	$\mathcal{E}_{23},\mathcal{E}_4)$						
$\sigma_{s,yx}$	$0.1 \cdot \bar{I}_{yx}$		standard c	leviation o	f weight di	stribution				
\bar{d}_x			mean spik	e transmis	sion delays	:				
	$1.5\mathrm{ms}$		$x \in \{\mathcal{E}_{23}, \mathcal{E}_4, \mathcal{E}_5, \mathcal{E}_6, \mathcal{T}, \mathcal{C}\}$							
	$0.75\mathrm{ms}$		$x \in \{\mathcal{I}_{23}, \mathcal{I}_4, \mathcal{I}_5, \mathcal{I}_6\}$							
$\sigma_{d,x}$	$0.5 \cdot \bar{d}_x$		standard deviation of spike transmission delays							
d_{min}	0.1 ms		minimal spike transmission delay							
				Initial o	conditions	1				
Po	opulation spec	ific mean	and stand	dard devia	ition of in	itial mem	brane-pot	ential dist	tributions	
population x \mathcal{E}_{23}		\mathcal{I}_{23}	\mathcal{E}_4	\mathcal{I}_4	\mathcal{E}_5	\mathcal{I}_5	\mathcal{E}_6	\mathcal{I}_6		
\bar{V}	$ar{V}_{0,x}$ (mV) -68.28		-63.16	-63.33	-63.45	-63.11	-61.66	-66.72	-61.45	
σ	$r_{v,x} \; (mV)$	5.36	4.57	4.74	4.94	4.94	4.55	5.46	4.48	

Table 6: Model parameters (continued).

A Single-neuron dynamics in normal form (subthreshold)

• linear, inhomogeneous dynamics of synaptic input currents and (subthreshold) membrane potential for neuron $i \in y \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$ (cf. eqs. (1) and (2)):

$$\dot{I}_i + \frac{1}{\tau_s} I_i = f_i(t)$$

$$\dot{V}_i + \frac{1}{\tau_m} \left[V_i - E_L \right] - \frac{R_m}{\tau_m} I_i = 0$$
(3)

with

$$f_i(t) = \sum_{x} \sum_{j \in x} \hat{I}_{ij} s_j(t - d_{ij}) \qquad (x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6, \mathcal{T}, \mathcal{C}\})$$

$$\tag{4}$$

ullet rescale membrane potential $v_i(t)=V_i(t)-E_{
m L}$ and total current $x_i(t)=rac{R_{
m m}}{ au_{
m m}}I_i(t)$:

$$\dot{x}_i + \frac{1}{\tau_s} x_i = \frac{R_m}{\tau_m} f_i(t)$$

$$\dot{v}_i + \frac{1}{\tau_m} v_i - x_i = 0$$
(5)

• normal form of neuron-i dynamics (5):

$$\frac{\mathsf{d}}{\mathsf{d}t}\boldsymbol{y}_i = \boldsymbol{A}\boldsymbol{y}_i + \boldsymbol{f}_i(t) \tag{6}$$

with D=2 dimensional state vector

$$\mathbf{y}_i(t) = \left(x_i(t), v_i(t)\right)^\mathsf{T},\tag{7}$$

with constant $(D\times D)$ matrix

$$\mathbf{A} = \begin{bmatrix} -1/\tau_{\mathsf{s}} & 0\\ 1 & -1/\tau_{\mathsf{m}} \end{bmatrix},\tag{8}$$

and inhomogeneity vector

$$\mathbf{f}_{i}(t) = \left(\frac{R_{\mathsf{m}}}{\tau_{\mathsf{m}}} f_{i}(t), 0\right)^{\mathsf{T}} \tag{9}$$

(see Sec. 3.2.2 in Rotter & Diesmann, 1999)

- see App. B for an efficient, exact integration scheme of (6)
- back-transform to physical quantities:

$$\begin{split} V_i(t) &= v_i(t) + E_{\mathsf{L}} \\ I_i(t) &= \frac{\tau_{\mathsf{m}}}{R_{\mathsf{m}}} x_i(t) \end{split} \tag{10}$$

B Exact integration of single-neuron dynamics (subthreshold)

• exact integration of (6) for spikes arriving at the target neuron i on a time grid $\mathcal{T}_{\Delta} = \{t_k = k\Delta | k \in \mathbb{N}, \Delta \in \mathbb{R}^+\}$, i.e., for spike trains $s_j(t) = \sum_l \delta(t - t_j^l)$ with $t_j^l \in \mathcal{T}_{\Delta}$ (Rotter & Diesmann, 1999):

$$y_i(t_{k+1}) = Py_i(t_k) + f_i(t_{k+1})$$
 (11)

with $(D \times D)$ propagator matrix (matrix exponential)

$$P = e^{A\Delta} \tag{12}$$

with components

$$\mathbf{P} = \begin{bmatrix} e^{-\Delta/\tau_{s}} & 0\\ \frac{e^{-\Delta/\tau_{m}} - e^{-\Delta/\tau_{s}}}{1/\tau_{s} - 1/\tau_{m}} & e^{-\Delta/\tau_{m}} \end{bmatrix}$$
(13)

(see Sec. 3.2.2 in Rotter & Diesmann, 1999)

C Remarks

1. The implementation contains, besides the original full-scale model of Potjans et al. (2014), a downscaled version, which can run on a desktop computer. This is controlled by the parameters N_scaling and K_scaling in the network parameters file. The first parameter scales the number of neurons, whereas the second parameter scales the number of synapses per neuron or in-degree. The scaling happens on both, inter-population and external connectivity.

Downscaling the in-degree $K_{\mathcal{C}_x}$ changes the mean and variance of the synaptic input currents. In order to avoid this, one can choose the new synaptic weights J^* in such a way that together with a compensation current these effects are compensated. For the full-scale model we have

$$\mu = \tau_{\rm s} K J r \,,$$

$$\sigma^2 = \tau_{\rm s} K J^2 r \,,$$

where K is the in-degree, J the synaptic weight and r the firing rate. For the downscaled model we have

$$\mu^* = \tau_{\rm s} K^* J^* r + \mu_0 ,$$

$$(\sigma^*)^2 = \tau_{\rm s} K^* (J^*)^2 r .$$

Here, $K^* = fK$ with some factor 0 < f < 1, and μ_0 is a compensation current. Comparing the equations of the variance we find $J^* = J/\sqrt{f}$. Inserting this in the equation of the mean and solving for the compensation current μ_0 we find

$$\mu_0 = \tau_{\rm s} \left(1 - \sqrt{f} \right) KJr \,.$$

There are other ways to downscale the model, for more details see (van Albada et al., 2015).

2. In the original model of Potjans et al. (2014), the cortico-cortical inputs are modeled as independent realizations $s_i(t)$ ($i \in \mathcal{C}_x$ for $x \in \{\mathcal{E}_{23}, \dots, \mathcal{I}_6\}$) of a Poisson point process with constant rate $\nu_{\mathcal{C}_x} = K_{\mathcal{C}_x}\nu_{\mathcal{C}}$, filtered by an exponential kernel PSC(t) with time constant τ_s and amplitude $\bar{I}_{\mathcal{C}}$. Here, $K_{\mathcal{C}_x}$ denotes the cortico-cortical in-degree and $\nu_{\mathcal{C}}$ a constant rate. DC inputs are computationally less expensive, exactly reproducible, and lead to similar network activity statistics. When replacing Poissonian input spikes s(t) by DC inputs, the current implementation preserves the mean input current

$$I_{\mathcal{C}} = (\langle s \rangle * \mathsf{PSC})(t) = \bar{I}_{\mathcal{C}} \nu_{\mathcal{C}} \tau_{\mathsf{s}} \,.$$

3. The original model of Potjans et al. (2014) uses population *unspecific* normal distributions of initial membrane potentials. By default, the current implementation uses population *specific* initial membrane potential distributions instead to speed up convergence to the stationary state. In the reference implementation, the type of initial conditions can be set by the parameter V0_type ("optimized" [default] or "original"). In (Senk et al., 2025), the population specific initial conditions are referred to as *amended* initial conditions.

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