

# Advances Towards Practical Implementations of Isogeny Based Signatures

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# Overview

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## Introduction & Background

- Post-quantum Cryptography & Motivation

- Elliptic Curves & Isogenies

- Supersingular Isogeny Diffie-Hellman

- Isogeny-based Signatures

## Batching Field Element Inversions

- Batching Partial Inversions

- Implementing Batching in SIDH 2.0

- Performance of Inversion Batching

## Compressing Isogeny-based Signatures

- SIDH Public Key Compression

- Implementing in SIDH 2.0

- Advantage and Cost of Compressions

## Results

- Performance Measurements

# Public-key Cryptography

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There are five rudimentary concerns of information security:

- ▶ *Confidentiality*: information must be kept private from unauthorized individuals
- ▶ *Integrity*: information must not be altered by unauthorized individuals
- ▶ *Availability*: information must be available for authorized individuals
- ▶ *Authenticity*: information must have a verifiable source
- ▶ *Non-repudiation*: the source of information must be publicly verifiable

# Public-key Cryptography

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The goal of cryptography is to define mathematically precise means of ensuring these information security goals.

Cryptographic protocols can be either *private-key* or *public-key* systems.

Public-key systems require that every party takes ownership of both a public key ( $pk$ ), the value of which is known by everyone on the network, and a private key ( $sk$ ), known only to the owner.

# Quantum Cryptanalysis

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Efficient large-scale quantum computing → breaking most modern public-key cryptosystems.

This has lead to the development of the field known as post-quantum cryptography – the aim of which is to develop cryptosystems resistant to quantum cryptanalysis.

# Post-quantum Cryptography

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Common approaches to post-quantum cryptography include

- ▶ Lattice-based cryptography
- ▶ Hash-based cryptography
- ▶ Multivariate-based cryptography
- ▶ Code-based cryptography
- ▶ Isogeny-based cryptography

# Post-quantum Cryptography

|         | Key Gen       | Sign             | Verify           |
|---------|---------------|------------------|------------------|
| SIDH    | 84,499,270    | 4,950,023,141.65 | 3,466,703,991.09 |
| Sphincs | 17,535,886.94 | 653,013,784      | 27,732,049       |
| qTESLA  | 1,059,388     | 460,592          | 66,491           |
| Picnic  | 13,272        | 9,560,749        | 6,701,701        |
| RSA     | 12,800,000    | 1,113,600        | 32400            |
| ECDSA   | 1,470,000     | 128,928          | 140,869          |

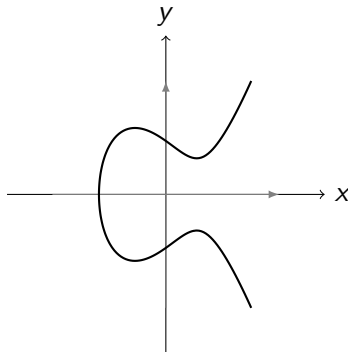
# Elliptic Curves as a Group

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Elliptic curves are a class of algebraic curves satisfying

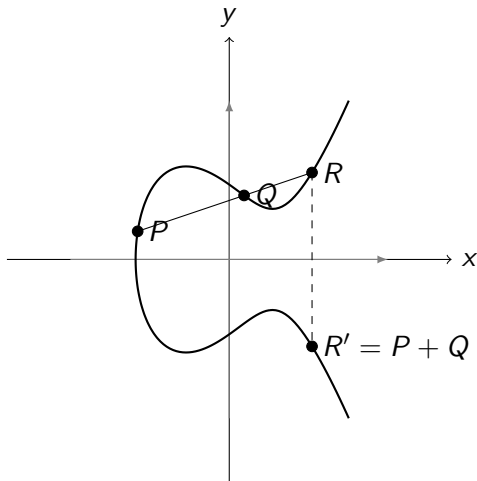
$$E : y^2 = x^3 + ax + b.$$

We can define a group  
composed of all the points  
 $P = (x, y)$  satisfying  $E$ .





# Elliptic Curves as a Group



# Isogenies

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Isogenies are maps that take a point on one elliptic curve to a point on another. For an isogeny  $\phi$  mapping from  $E_1$  to  $E_2$ , we can write

$$\phi : E_1 \rightarrow E_2$$

These maps have the following two properties

- ▶  $\phi(\mathcal{O}) = \mathcal{O}$
- ▶  $\phi(P^{-1}) = (\phi(P))^{-1}$

# Key Exchange Protocols

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Key exchange protocols are cryptographic schemes used to establish a shared secret between two party members

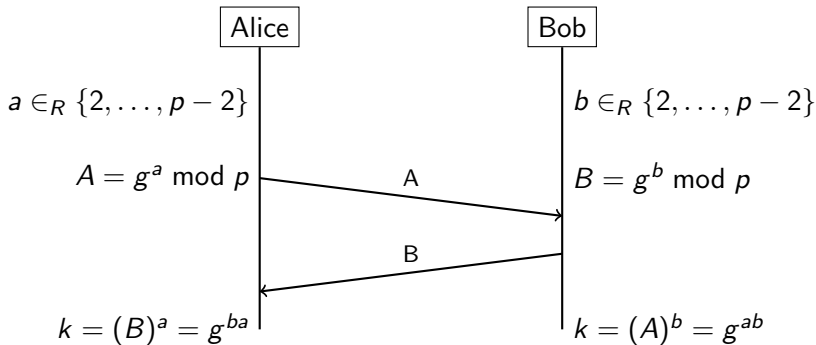
These can be defined by a tuple of algorithms

$$\Pi_{kex} = (\mathbf{KeyGen}, \mathbf{SecAgr}).$$

# Key Exchange Protocols

Public parameter:

$$g, p$$



# Supersingular Isogeny Diffie-Hellman

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# Interactive Identification Schemes

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Theorem (Mass–energy equivalence)

$$E = mc^2$$

# Signature Schemes

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Theorem (Mass–energy equivalence)

$$E = mc^2$$

# Fiat-Shamir Transform

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Theorem (Mass–energy equivalence)

$$E = mc^2$$



# Yoo Signatures

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Theorem (Mass–energy equivalence)

$$E = mc^2$$

# Table

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| Treatments  | Response 1 | Response 2 |
|-------------|------------|------------|
| Treatment 1 | 0.0003262  | 0.562      |
| Treatment 2 | 0.0015681  | 0.910      |
| Treatment 3 | 0.0009271  | 0.296      |

Table: Table caption

# Signature Schemes

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Theorem (Mass–energy equivalence)

$$E = mc^2$$

# Verbatim

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## Example (Theorem Slide Code)

```
\begin{frame}  
\frametitle{Theorem}  
\begin{theorem}[Mass--energy equivalence]  
$E = mc^2$  
\end{theorem}  
\end{frame}
```

# Figure

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Uncomment the code on this slide to include your own image from the same directory as the template .TeX file.

# Citation

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An example of the `\cite` command to cite within the presentation:

This statement requires citation [Smith, 2012].

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# Questions?



## References



John Smith (2012)

Title of the publication

*Journal Name* 12(3), 45 – 678