

Variance, Covariance and correlation

1. Continue with the wage exercise that we practiced in class. Complete the following:

(1) Calculate R-squared with the formula, and then calculate the correlation between wage and education to verify the relationship between R-squared and correlation. Interpret the meaning of R-squared.

(2) Use the formula for b_1 , prove that

$$b_1 = \hat{\rho} \frac{\hat{\sigma}_y}{\hat{\sigma}_x}$$

What does this equation mean? (eg. b_1 increases as ... increases, decreases as decreases)

(3) Test the null hypothesis that $\beta_1 = 0$. Is there any significant evidence that the education affects wage? (you can calculate manually with the formula, or use the regression function in Excel, both are fine).

(4) Test the null hypothesis that $\beta_1 \geq 0.8$. State your conclusion in detail.

(5) (bonus) Make a scatter plot for wage (vertical axis) and education (horizontal axis). Does it look like the graphs we used in class? What are the differences? Does this dataset fulfill the four conditions for running simple linear regression?