## GrowthDynamics.R

## Administrator

Tue Feb 23 14:56:32 2016

```
# Modeling differential growth equations
# February 22, 2016
# NJG

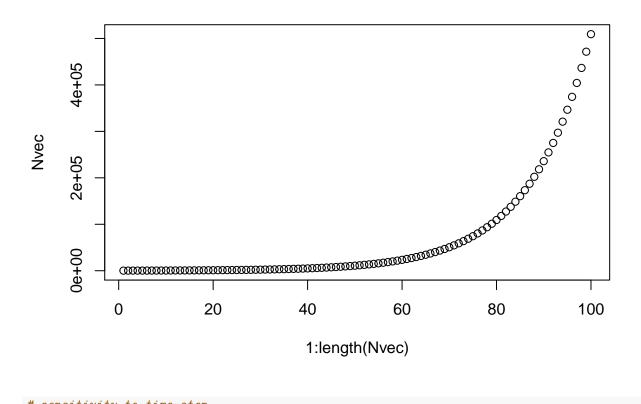
# basic equation for change plus current value
# illustrated with familiar exponential growth

rm(list=ls())
set.seed(100)
opar <- par(no.readonly=TRUE)

# basic growth model</pre>
```

```
Model1 <- function(N_0=250,Time=100,r=0.08){
   Nvec <- rep(0,Time)
   Nvec[1] <- N_0
   for (i in 2:Time) {
      Nvec[i] <- Nvec[i-1] + r*Nvec[i-1]
   }
   return(Nvec)

}
Nvec <- Model1()
plot(x=1:length(Nvec),y=Nvec)</pre>
```

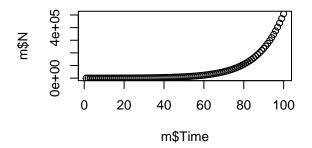


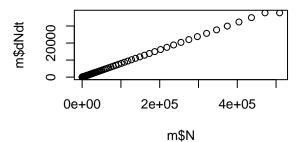
```
# sensitivity to time-step
r < -0.08
BigStep \leftarrow seq(1,50,by=1)
SmallStep <-seq(1,50,by=0.1)
BigVec <- rep(0,length(BigStep))</pre>
SmallVec <- rep(0,length(SmallStep))</pre>
BigVec[1] <- 250
SmallVec[1] \leftarrow 250
for (i in 2:length(BigVec)) BigVec[i] <- BigVec[i-1] + r*BigVec[i-1]</pre>
for (i in 2:length(SmallVec)) SmallVec[i] <- SmallVec[i-1] + r*SmallVec[i-1]*0.1
tail(BigVec)
## [1] 7388.993
                   7980.112 8618.521 9308.003 10052.643 10856.855
tail(SmallVec)
## [1] 11920.60 12015.96 12112.09 12208.99 12306.66 12405.11
250*exp(50*0.08)
```

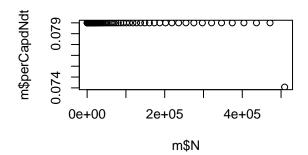
## [1] 13649.54

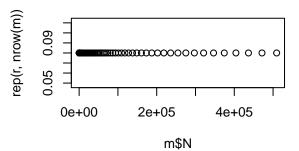
## # Calculating N, dNdt, (1/N)(dNdt)

```
Model2 <- function(N_0=250, Time=100, r=0.08){
  Nvec <- rep(0,Time)</pre>
  Nvec[1] \leftarrow N_0
  for (i in 2:Time) {
    Nvec[i] \leftarrow Nvec[i-1] + r*Nvec[i-1]
    dNvec <- diff(Nvec)</pre>
    dNvec <- c(dNvec,dNvec[length(dNvec)])</pre>
    perCapvec <- dNvec/Nvec</pre>
m <- cbind(1:Time,Nvec,dNvec,perCapvec)</pre>
colnames(m) <- c("Time","N","dNdt","perCapdNdt")</pre>
return(m)
}
m <- Model2()</pre>
                          # save output matrix
m <- as.data.frame(m)</pre>
                          # convert to data frame
par(mfrow=c(2,2))
plot(x=m$Time,y=m$N)
plot(x=m$N,y=m$dNdt)
plot(x=m$N,y=m$perCapdNdt)
plot(x=m$N,y=rep(r,nrow(m)))
```









par(opar)
# par(mfrow=c(2,2))