

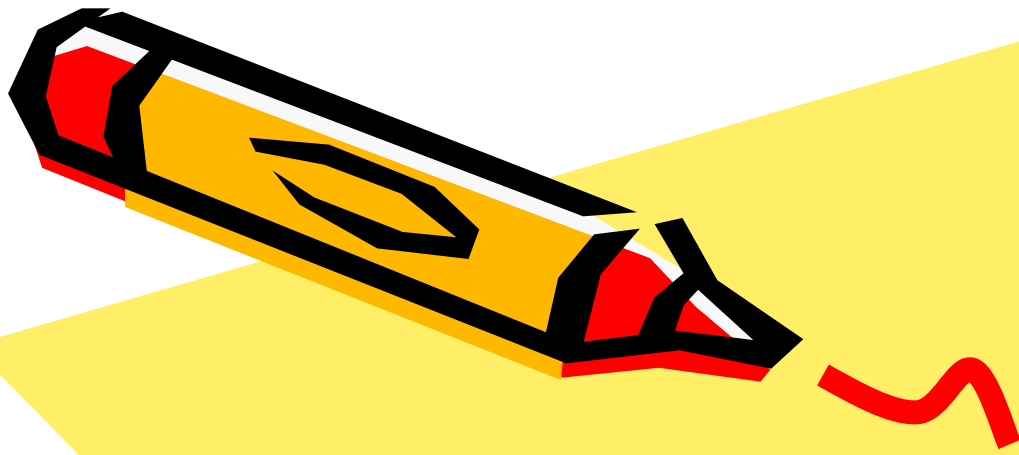


Logical Design

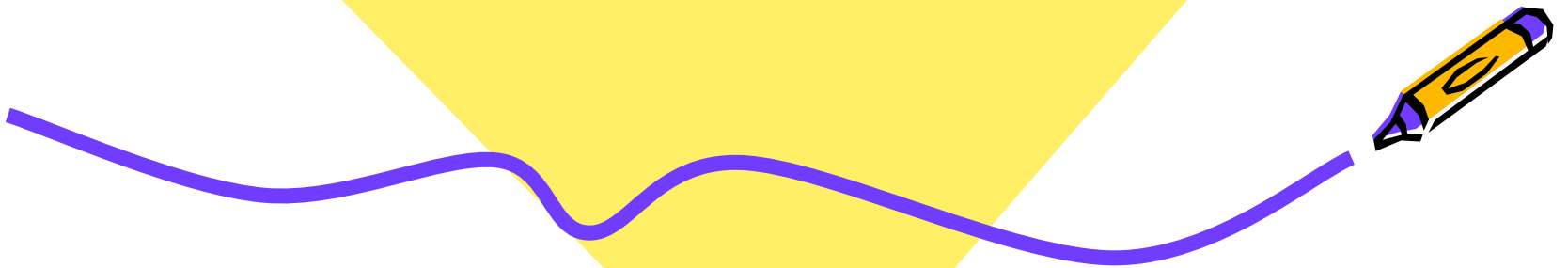
CS 221

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Karnaugh Maps





Karnaugh Maps



- Boolean expressions may be simplified by using algebraic operations
- But there is not set method to predict the steps to take
- That means not amenable to automated techniques
- Karnaugh Maps to the rescue
- Generates simplified expressions that are in SOP or POS form
- Produce two-level implementation with a minimum number of gates and a minimum number of inputs to the gates
- Sometimes two or more expressions that satisfy the simplification criteria





Two-Variable Map



X	Y	Minterms	
0	0	$x'y'$	m0
0	1	$x'y$	m1
1	0	xy'	m2
1	1	xy	m3

		0	1
x \ y	0	$x'y'$ ^{m0} 0	$x'y$ ^{m1} 1
	1	xy' ^{m2} 2	xy ^{m3} 3





$$F(x,y) = xy + x'y$$

$x \backslash y$		0	1
0			1
1			1

$$F(x,y) = y$$





Three Variables Map



$x \backslash yz$				
	00	01	11	10
0	$x'y'z'$ m0 0	$x'y'z$ m1 1	$x'yz$ m3 3	$x'yz'$ m2 2
1	$xy'z'$ m4 4	$xy'z$ m5 5	xyz m7 7	xyz' m6 6





Simplify the following Boolean function

$$F(x,y,z) = \Sigma(3,4,6,7)$$

x \ yz	yz			
	00	01	11	10
0			1	
1	1		1	1

$$F(x,y,z) = xz' + yz$$





$$F(x,y,z) = A'C + A'B + AB'C + BC$$

Express it in sum of minterms

Find the minimal sum of products expression

x \ yz	yz			
	00	01	11	10
0		1	1	1
1		1	1	

$$F(x,y,z) = \Sigma(1,2,3,5,7)$$

$$F(x,y,z) = C + A'B$$





Four Variables Map



$wx \backslash yz$		00	01	11	10
00	$w'x'y'z'$ m0 0	$w'x'y'z$ m1 1	$w'x'yz$ m3 3	$w'x'yz'$ m2 2	
01	$w'xy'z'$ m4 4	$w'xy'z$ m5 5	$w'xyz$ m7 7	$w'xyz'$ m6 6	
11	$wxy'z'$ m12 12	$wxy'z$ m13 13	$wxyz$ m15 15	$wxyz'$ m14 14	
10	$wx'y'z'$ m8 8	$wx'y'z$ m9 9	$wx'yz$ m11 11	$wx'yz'$ m10 10	





Simplify the following Boolean function

$$F(w,x,y,z) = \Sigma(0,1,2,4,5,6,8,9,12,13,14)$$

yz wx		yz			
		00	01	11	10
00	1	1		1	
01	1	1		1	
11	1	1		1	
10	1	1			

$$F(w,x,y,z) = y' + w'z' + xz'$$





Simplify the following Boolean function

$$F(w,x,y,z) = \Sigma(0,2,3,5,7,8,9,10,11,13,15)$$

wx \ yz		yz			
		00	01	11	10
00	1			1	1
01			1	1	
11			1	1	
10	1	1		1	1

$$F(w,x,y,z) = wx' + yz + xz + x'z'$$





Don't Care Conditions

Simplify the following Boolean function

$$F(w,x,y,z) = \Sigma(1,3,7,11,15)$$

Which has the don't care conditions $d(w,x,y,z) = \Sigma(0,2,5,8)$



wx \ yz				
	00	01	11	10
00	x	1	1	x
01		x	1	
11			1	
10	x		1	

$$F(w,x,y,z) = w'x' + yz$$







Thank you



