



**Answer**

**Logical Design (CS 221) Mid-Term Exam**

**Execute the following conversions**

**( 3 marks )**

Decimal	Binary	Octal	Hexadecimal
<b>35</b>	100011	43	23
21	<b>10101</b>	25	15
18	10010	<b>22</b>	12
27	11011	33	<b>1B</b>

2 -

(5 marks)

- a) Convert each of the following BCD numbers to Decimal

$$10000111 = \underline{87}$$

$$1001010101110000 = \underline{9570}$$

- b) Add the following BCD numbers

$$1) 1001 + 0100 = 1101 + 0110 = 10011 = \underline{00010011} = 13$$

$$2) 01100111 + 01010011 = (67 + 53) 10111010 + 01100110 = 100100000 = \underline{000100100000} = 120$$

- c) convert the binary number 1101110110 to gray code.

$$= \underline{1011001101}$$

- d) convert the gray code number 10100101 to binary

$$= \underline{11000110}$$

- e) What is  $-18_{(10)}$  expressed as an 8-bit binary number in 2's complement notation ?

$$18 = 10010 = 00010010 = 11101110 (2's \text{ complement}) = \underline{11101110}$$

3 - Simplify the following Boolean expression using Boolean algebra :

$$[wx(y + \overline{xz}) + \overline{wx}]yz \quad (3 \text{ marks})$$

$$\begin{aligned} & [wx(y + \overline{x} + \overline{z}) + \overline{wx}]yz \\ &= [wxy + wx\overline{x} + wx\overline{z} + \overline{wx}]yz \\ &= [wxy + wx\overline{z} + \overline{wx}]yz \\ &= [wxxyz + wx\overline{z}yz + \overline{w}xyz] \\ &= [wxxyz + \overline{w}xyz] \\ &= yz(wx + \overline{w}) \\ &= yz \end{aligned}$$

- 4 - Express the Boolean function  $F = A' + BC'$  in sum of product using algebraic method and prove your answer by truth table method. (4 marks)

$$F = A' (B'C' + B'C + BC' + BC) + BC' (A' + A)$$

$$F = A' B' C' + A' B' C + A' B C' + A' B C + A' B C' + A B C'$$

0 0 0      0 0 1                      0 1 1              0 1 0              1 1 0

$$F(A,B,C) = \sum (m_0, m_1, m_2, m_3, m_6)$$

A	B	C	A'	C'	BC'	F = A'+BC'
0	0	0	1	1	0	<u>1</u> m <sub>0</sub>
0	0	1	1	0	0	<u>1</u> m <sub>1</sub>
0	1	0	1	1	1	<u>1</u> m <sub>2</sub>
0	1	1	1	0	0	<u>1</u> m <sub>3</sub>
1	0	0	0	1	0	0
1	0	1	0	0	0	0
1	1	0	0	1	1	<u>1</u> m <sub>6</sub>
1	1	1	0	0	0	0

Course Coordinator

Good Luck .... Prof. Khozium