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Assignment-1

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Download all python codes from

https://github.com/G.Soujanya/AssignmentT-1/tree/main/Assignment%201/CODES

and latex-tikz codes from

https://github.com/G.Soujanya/Assignment-1/tree/main/Assignment%201

1 QUESTION NO-2.13

Construct $\triangle ABC$ such that AB=2.5, BC=6, and AC=6.5. Find $\angle B$

2 SOLUTION

Let us assume, sideAB=c, sideBC=a, sideAC=bLet

$$\mathbf{A} = \begin{pmatrix} 0 \\ 2.5 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 6 \\ 0 \end{pmatrix} \tag{2.0.1}$$

Now.

$$\|\mathbf{A} - \mathbf{B}\|^2 = \|\mathbf{A}\|^2 = c^2 = (2.5)^2 = 6.25$$
 (2.0.2)

$$\|\mathbf{B} - \mathbf{C}\|^2 = \|\mathbf{C}\|^2 = a^2 = (6)^2 = 36$$
 (2.0.3)

$$\|\mathbf{A} - \mathbf{C}\|^2 = b^2 = (6.5)^2 = 42.25$$
 (2.0.4)

From $\triangle ABC$, we use the Law of cosine:

$$b^2 = a^2 + c^2 - 2accosB (2.0.5)$$

$$\cos B = \frac{a^2 + c^2 - b^2}{2ac} \tag{2.0.6}$$

$$\cos B = \frac{0}{32.5} \tag{2.0.7}$$

$$cosB = o (2.0.8)$$

$$B = 90^{\circ}$$
 (2.0.9)

As we consider $\triangle ABC$ in first quadrant we consider angle B

:.
$$angleB = 90$$
 (2.0.10)

Now, Vertices of given $\triangle ABC$ can be written as,

$$\mathbf{A} = \begin{pmatrix} 0 \\ 2.5 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{C} = \begin{pmatrix} 6 \\ 0 \end{pmatrix} \tag{2.0.11}$$

Now, $\triangle ABC$ can be plotted using vertices AB, BC and AC.

Plot of $\triangle ABC$:

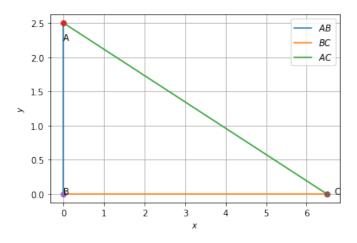


Fig. 2.1: △*ABC*