

Assignment 3

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Download all python codes from

<https://github.com/G.Soujanya/Assignment3/tree/main/CODES>

and latex-tikz codes from

<https://github.com/G.Soujanya/Assignment3/tree/main>

$$\Rightarrow \mathbf{r} = r \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \quad (2.0.4)$$

Here the direction vector is

$$\mathbf{d}_1 = \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \quad (2.0.5)$$

case(2) :Now let we find the line equation passing through the points

$$\mathbf{Q} = \begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} 4 \\ 3 \\ -1 \end{pmatrix} \quad (2.0.6)$$

Direction vector \mathbf{A} of the points \mathbf{Q} and \mathbf{R} is given by

$$\mathbf{A} = \mathbf{R} - \mathbf{Q} = \begin{pmatrix} 4 \\ 3 \\ -1 \end{pmatrix} - \begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix} \quad (2.0.7)$$

$$\text{Therefore } \mathbf{A} = \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix}$$

1 QUESTION No-2.45 (LINEAR FORMS)

show that the line joining the origin to the point $\begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix}$ is perpendicular to the line determined by the

points $\begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix}, \begin{pmatrix} 4 \\ 3 \\ -1 \end{pmatrix}$

2 SOLUTION

Let's take the given points

$$\mathbf{P} = \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix}, \mathbf{Q} = \begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix}, \mathbf{R} = \begin{pmatrix} 4 \\ 3 \\ -1 \end{pmatrix} \quad (2.0.1)$$

case(1):Now, we find the line equation passing through the origin to point $\begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix}$

Let origin point be $\mathbf{O} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix}$ and other point be

$$\mathbf{P} = \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix}$$

The vector form of the line passing through \mathbf{O} and \mathbf{P} , which is the line passing through the point \mathbf{O} and along direction vector \mathbf{A} is given by

$$\mathbf{r} = \mathbf{O} + k\mathbf{A} \quad (2.0.2)$$

$$\Rightarrow \mathbf{r} = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} + k \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \quad (2.0.3)$$

the equation of the line is

$$\mathbf{x} = \mathbf{Q} + \lambda\mathbf{A} \quad (2.0.8)$$

$$\mathbf{x} = \begin{pmatrix} 3 \\ 5 \\ -1 \end{pmatrix} + \lambda \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix} \quad (2.0.9)$$

Here, the direction vector is

$$\mathbf{d}_2 = \begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix} \quad (2.0.10)$$

Two lines are perpendicular each other when the dot product of their direction vectors is 0

Dot product of direction vectors \mathbf{d}_1 and \mathbf{d}_2

$$\mathbf{d}_1^T \mathbf{d}_2 = (2 \times 1) + (1 \times (-2)) + (1 \times 0) \quad (2.0.11)$$

$$= 2 + (-2) + 0 \quad (2.0.12)$$

$$= 2 - 2 \quad (2.0.13)$$

$$= 0 \quad (2.0.14)$$

$$\Rightarrow \boxed{\mathbf{d}_1^T \mathbf{d}_2 = 0} \quad (2.0.15)$$

as the dot product of direction vector of the lines is $0(\mathbf{d}_1^T \mathbf{d}_2)$, we can say that the lines are perpendicular to each other

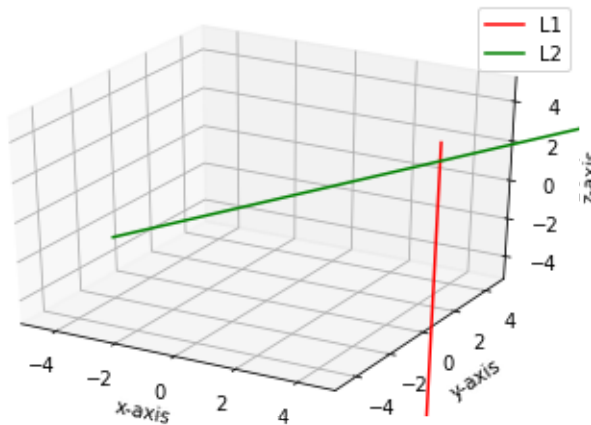


Fig. 2.1: lines perpendicular to each other