

Name :

Roll No. :

Invigilator's Signature :

CS/B.Tech (EE-N)/SEM-6/EC-611/2011

2011

DIGITAL SIGNAL PROCESSING

Time Allotted : 3 Hours

Full Marks : 70

The figures in the margin indicate full marks.

*Candidates are required to give their answers in their own words
as far as practicable*

GROUP – A

(Multiple Choice Type Questions)

1. Choose the correct alternatives for any *ten* of the following : $10 \times 1 = 10$

- i) The system described by $y(n) = x(n) + 2x(n-2) + 3x(n-3)$ is

- a) causal and stable
- b) causal and unstable
- c) noncausal and stable
- d) noncausal and unstable.

- ii) If $x(n) = \{ 2, 1, 3, 0, 1, 2, 4 \}$, then $x(-n+2)$ is given by

- a) $\{ 2, 1, 3, 0, 1, 2, 4 \}$
- b) $\{ 2, 1, 3, 0, 1, 2, 4 \}$
- c) $\{ 4, 2, 1, 0, 3, 1, 2 \}$
- d) $\{ 4, 2, 1, 0, 3, 1, 2 \}$.

- iii) If $x(n)$ and $h(n)$ are two finite length sequences, then their convolution has length
- a) 8 b) 10
c) 11 d) 9.
- iv) The overall impulse response of a cascade connection of two systems with impulse responses $h_1(n)$ and $h_2(n)$ is
- a) $h_1(n) + h_2(n)$ b) $h_1(n)h_2(n)$
c) $h_1(n) * h_2(n)$ d) $h_1(n) - h_2(n)$.
- v) A discrete-time LTI system is causal if
- a) impulse response $h(n) > 0, n > 0$
b) impulse response $h(n) < 0, n > 0$
c) impulse response $h(n) = 0, n > 0$
d) impulse response $h(n) = 0, n < 0$.
- vi) The ROC of an infinite causal sequence is the
- a) interior of a circle
b) exterior of a circle
c) entire z-plane except $z = 0$
d) entire z-plane except $z = \infty$.
- vii) The Z-transform of $u[n-1]$ is
- a) $1/(1 - Z^{-1})$ b) $Z/(1 - Z^{-1})$
c) $1/[Z(1 - Z^{-1})]$ d) $(1 + Z^{-1})$.

- viii) If $x(K)$ represents the 8 point DFT of $x(n) = \{1, 1, 1, 1, 1, 1, 0, 0\}$ then $x(0)$ is
- a) 3 b) 6
c) 1 d) 0.
- ix) The mapping from analog to digital domain in impulse invariant method is
- a) one to many b) many to one
c) one to one d) none of these.
- x) Overlap save method is used to find
- a) circular convolution b) linear convolution
c) DFT d) Z-transform.
- xi) Number of multiplications in FFT algorithm is
- a) $n \log(n)$ b) $(n/2) * \log(n)$
c) $(n/2) * \log(n/2)$ d) $n \log(n/2)$.
- xii) FIR filter is
- a) recursive and linear
b) non-recursive linear
c) recursive and non-linear
d) none of these.

GROUP – B

(Short Answer Type Questions)

Answer any *three* of the following. $3 \times 5 = 15$

2. The impulse response of an LTI system is $h(n) = \{1, 2, 1, -1\}$.

Determine the response of the system to the input signal

$$x(n) = \{1, 2, 3, 1\}.$$

3. If a discrete-time LTI system is BIBO stable, show that the

ROC of its system function $H(z)$ must contain the unit

circle, i.e., $|z|=1$.

4. Explain the relationship between S-plane and Z-plane.

5. a) Find the DTFT of the sequence $x(n) = \{1, -1, 1, -1\}$.

b) Find the IDTFT of $X(e^{j\omega}) = e^{-j\omega} \left(\frac{1}{2} + \frac{1}{2} \cos \omega \right)$. $2 + 3$

6. Determine the convolution of the two following sequences

using overlap add method :

$$x(n) = \{3, 2, 1, 2\} \quad h(n) = \{1, 2, 1, 1\}.$$

GROUP – C

(Long Answer Type Questions)

Answer any *three* of the following. $3 \times 15 = 45$

7. a) Justify whether the system is LTI or not.

$$y(n) = y(n-1) + \sum_{k=0}^2 x(n-k).$$

- b) Compute the circular convolution of the two sequences given below.

$$x(n) = \{2 \ -1 \ 0 \ 1 \ -2 \ 3 \ 0 \ 1\}.$$

$$h(n) = \{1 \ 2 \ -1 \ 1\}.$$

- c) Determine the linear convolution of the above sequences using over-lap save method.

8. a) What is ROC ? State its properties.

- b) Find the system function & impulse response of the system described by $y(n) = x(n) + 2x(n-1) - 4x(n-2) + x(n-3)$

- c) Find the Inverse Z-transform of

$$X(Z) = Z(Z^2 - 4Z + 5)/(Z-3)(Z-2)(Z-1)$$

- d) Prove that an LTI system is BIBO stable if the ROC system function includes the unit circle. $2 + 5 + 5 + 3$

9. a) Find the 8-point DFT using decimation in time FFT algorithm for a sequence $x(n) = \{1, 3, 5, 7, 2, 4, 6, 8\}$.
- b) What do you mean by zero padding ?
- c) Using linear convolution find $y(n) = x(n) * h(n)$ for the sequence $x(n) = \{1, 2, -1, -2, 0, 1, 3, -1\}$. Compare the result by solving the problem using
- overlap save method
 - overlap add method.

5 + 2 + 8

10. Following specifications are given for a filter function :

$$\alpha_{\text{pass}} = 4 \text{ dB}, \alpha_{\text{stop}} = 48 \text{ dB}, f_{\text{stop}} = 7 \text{ kHz}, f_{\text{pass}} = 2 \text{ kHz}, f_{\text{sampling}} = 20 \text{ kHz}$$

Determine an IIR filter using Butterworth approximation and impulse invariant method.

11. a) Design a digital Butterworth IIR filter for the given frequency response :

$$0.85 \leq |H(e^{j\omega})| \leq 1, \quad \text{for } 0 \leq \omega \leq 0.2\pi$$

$$|H(e^{j\omega})| \leq 0.02, \quad \text{for } 0.45\pi \leq \omega \leq \pi$$

Use impulse invariant method.

- b) Convert the analog filter with system function $G(s) = \frac{s + 0 \cdot 1}{(s + 0 \cdot 1)^2 + 16}$ into a digital filter using bilinear

transformation. The digital filter should have a resonant frequency of $\omega_r = \frac{\pi}{4}$ radian. 8 + 7

12. Write short notes on any *three* of the following : 3 × 5

- a) Causal and non-causal system
 - b) Circular convolution and linear convolution
 - c) DIT-FFT algorithm
 - d) Difference between DTFT and DFT
 - e) Bilinear transformation.
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