	Utech
Name :	
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Inviailator's Signature :	

ELECTROMAGNETIC FIELD THEORY

Time Allotted: 3 Hours Full Marks: 70

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

GROUP - A

(Multiple Choice Type Questions)

1.	Choose	the	correct	alternatives	for	any	ten	of	the	
	following :							$10 \times 1 = 10$		

- Unit of Dipole moment i)
 - Coulomb/m² a)
- b) Newton-m
- Coulomb-m c)
- Newton/m. d)
- Given $A = 2i + \alpha j + 2k$ and $B = \alpha i + j + k$. If A and B are ii) normal to each other, α is
 - a) 1

b) -2/3

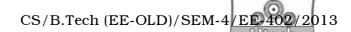
c) - 1

- d) 0.
- iii) Which statement is correct?
 - a) $A \times B + B \times A = 1$ b) $i \times j = k$
 - c) $i \cdot j = k$
- d) A . B . C = B . C . A.

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- iv) If a vector field P is solenoidal, which of this is true 3
 - a) $\oint_L P \cdot dI = 0$
 - b) $\oint_L P.dS = 0$
 - c) $\nabla \cdot P = 0$
 - d) $\nabla \times P \neq 0$.
- v) If a point is denoted by (3, 4, -2) in Cartesian Coordinate system, then which one of these is incorrect in spherical coordinate system?
 - a) $r = \sqrt{29}$
- b) $\theta = \tan^{-1}\left(\sqrt{5}/2\right)$
- c) $\Phi = \tan^{-1}(4/3)$
- d) z = -2.
- vi) Which one of the following is zero?
 - a) grad div A
 - b) div gradient ∇
 - c) div curl A
 - d) $\operatorname{curl} \operatorname{curl} A$.
- vii) The magnetic field at any point on the axis of a current carrying circular coil will be
 - a) perpendicular to the axis
 - b) parallel to the axis
 - c) at an angle 45° to the axis
 - d) zero.



- viii) A plane wave in a homogeneous medium has $E = 50 \sin \left(10^8 t + 2z\right) j \text{ V/m}$. What is the direction of wave propagation?
 - a) y direction
 - b) z direction
 - c) -z direction
 - d) -y direction.
- ix) Skin depth is proportional to
 - a) frequency
 - b) permeability
 - c) $1/\sqrt{\sigma}$
 - d) $\sqrt{\sigma}$.
- x) Which statement does not say that electrostatic field is conservative?
 - a) if the curl of E is identically zero
 - b) the potential difference between two points is zero
 - c) it is gradient of a scalar potential
 - d) the work done in a closed path inside the field is zero.



- xi) Which of the following is incorrect?
 - a) Continuity equation : $\nabla \cdot J = -\partial \rho / \partial t$
 - b) Faraday's Law : $\nabla \times E = \partial B / \partial t$
 - c) Ampere's circuital law : $\nabla \times H = J + \partial D / \partial t$
 - d) Poisson's equation : $\nabla^2 \nabla = 0$.
- xii) The characteristic impedance of a transmission line is
 - a) directly proportional to its length
 - b) inversely proportional to its length
 - c) independent of its length
 - d) directly proportional to square root of its length.

GROUP - B

(Short Answer Type Questions)

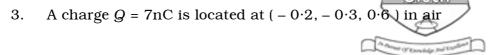
Answer any *three* of the following.

 $3 \times 5 = 15$

- 2. Given points A (x=2, y=3, z=1) & B ($\rho=4$, $\phi=-50^\circ$, z=2). Find the distance from
 - a) A to origin
 - b) *B* to origin and
 - c) A to B.

$$1\frac{1}{2} + 1\frac{1}{2} + 2$$

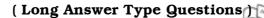




- a) Find the magnitude of the electrical field intensity at a point 1 mtr from the charge,
- b) Find \overline{E} at (0.4, 0.6, -1.2). 2 + 3
- 4. Define vector & scalar field with proper examples. Show a point P in 3 different co-ordinate systems with standard notations. What is equipotential surface ? 2+2+1
- 5. Find the nature of the Field by determining its Divergence & Curl. $B=\left(150/r^2\right)\stackrel{\wedge}{a}_r+10\stackrel{\wedge}{a}_\phi$ (cylindrical co-ordinate system). $2\frac{1}{2}+2\frac{1}{2}$
- 6. Using Gauss's theorem find the charge density (D) outside a uniformly charged sphere (where $r>\alpha$).

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Answer any three of the following.



 $3 \times 15 = 45$

- 7. The electric field associated with a EM wave propagating through a lossless medium of relative permittivity (ε_r) 78 and $\mu_r = 1$ at a frequency of 300 MHz is represented as $E_y = 10 \cos \left(6\pi \times 10^8 \, t \beta x\right)^{6}$. Determine
 - i) The phase constant
 - ii) Wave velocity
 - iii) Intrinsic impedance
 - iv) Wavelength and
 - v) Corresponding magnetic field *H*.

 5×3

8. State and define Biot-Savart Law. An infinitely long conductor is bent into an L shape. If 15 Amp current flows find H at (0, 0, 2) and (0, -2, 0). 5 + 10

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- 9. State and define Ampere's Circuital law. Starting from Maxwell's equation Curl $E=-\partial B/\partial t$ and Curl $H=J+\partial D/\partial t$ respectively, show that Div B=0 and Div $D=\rho$. 5+10
- 10. State Gauss's law. What is Gaussian surface ? Derive an expression for electric field ($\it E$) due to sheet of charge.

5 + 2 + 8

- 11. Write short notes on any *three* of the following: 3×5
 - a) Waves in transmission lines
 - b) Polarisation in dielectrics
 - c) Helmholtz's theorem
 - d) Law of conservations of charges.

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