	Utech
<i>Name</i> :	\$
Roll No.:	A Annual (V Same Life 2nd Explore)
Invigilator's Signature :	

# 2012 **MECHANICAL SCIENCES**

Time Allotted: 3 Hours Full Marks: 70

The figures in the margin indicate full marks. Candidates are required to give their answers in their own words as far as practicable.

## GROUP - A ( Multiple Choice Type Questions )

- 1. Choose the correct alternatives for the following:  $10 \times 1 = 10$ 
  - According to principle of transmissibility of forces, the i) effect of a force on a body is
    - maximum when it acts at the centre of gravity of a a)
    - b) minimum when it acts at the centre of gravity of a body
    - same at every point in its line of action c)
    - none of these.
  - Moment of inertia of a circular area whose diameter is dii) about an axis perpendicular to the area passing through its centre is given by
    - a)

c)

b)  $\frac{\pi d^4}{32}$ d)  $\frac{\pi d^4}{4}$ .

1202 (O) [ Turn over



- iii) If rain is falling in the opposite direction of the movement of a pedestrian, he has to hold his umbrella
  - a) more inclined when moving
  - b) less inclined when moving
  - c) more inclined when standing
  - d) none of these.
- iv) The ratio between tensile stress and tensile strain or compressive stress and compressive strain is termed as
  - a) Modulus of elasticity
  - b) Modulus of rigidity
  - c) Bulk modulus of elasticity
  - d) None of these.
- v) Temperature stress develop in a bar depends upon
  - a) Co-efficient of linear expansion
  - b) Change of temperature
  - c) Young's modulus
  - d) All of these..
- vi) Equation of motion of a particle is  $s = 2t^3 t^2 2$  where s is the displacement in metres and t is time in seconds. Acceleration of the particle after 1 second will be
  - a)  $8 \text{ m/sec}^2$
- b)  $9 \text{ m/sec}^2$
- c)  $10 \text{ m/sec}^2$
- d)  $5 \text{ m/sec}^2$ .
- vii) If the velocity of projection is u m/sec and the angle of projection is  $\alpha^{\circ}$ , the time of flight of the projectile is
  - a)  $\frac{u^2 \cos^2 \alpha}{2g}$
- b)  $\frac{2u\sin\alpha}{a}$
- c)  $\frac{2u\cos\alpha}{g}$
- d)  $\frac{u^2 \sin^2 \alpha}{2q}$

- viii) Frictional force encountered after commencement of motion is known as
  - a) sliding friction
- b) kinematic friction
- c) dynamic friction
- d) frictional resistance.
- ix) D' Alembert's Principle is used for
  - a) reducing the problem of kinetics to equivalent static problem
  - b) stability of floating bodies
  - c) solving kinematic problems
  - d) none of these.
- x) If two bodies, one light and the other heavy have equal kinetic energy, which one has a greater linear momentum?
  - a) The lighter body
  - b) The heavy body
  - c) Both have equal momentum
  - d) None of these.

#### **GROUP - B**

#### (Short Answer Type Questions)

Answer any three of the following.

 $3 \times 5 = 15$ 

2. A bar of length l cross-sectional area A is rigidly fixed at one end. Find the elongation of the bar due its self weight if density of the bar material is  $\rho$  kg/m<sup>3</sup>.

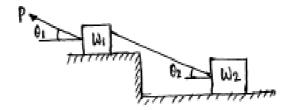
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- 3. a) What is FBD?
  - b) Draw the FBD of the given figure considering rough surface.

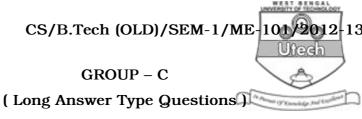


1 + 4

- 4. Prove that area moment of inertia of any area is minimum about its centroidal axis.
  - Again prove that for an axisymmetric area centroid lies on axis of symmetry. 2 + 3
- 5. A particle moves along a curvilinear path defined by  $y = ax^2$  where x and y are in metres. The velocity and acceleration of the particle at a point (5 m, 2.5 m) are respectively 5 m/sec and 2 m/sec<sup>2</sup>. Determine that total acceleration of the particle at the point.
- 6. A force  $P = P_x i + P_y j$  acts at a point of co-ordinates x and y.

  Derive an expression for the perpendicular distance d from the line of action of P to the origin O of the system of co-ordinates.

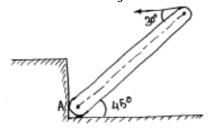
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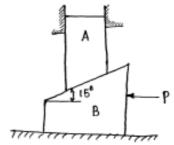
Answer any three of the following.

 $3 \times 15 = 45$ 

7. a) A joint of length 4 m and weighing 300 N is raised by pulling a rope as shown. Determine the tension in the rope and reaction at *A* of joint.



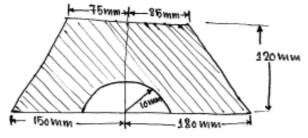
b) A block weighing 2000 N is to be raised by forcing the wedge under it. Determine the required force P to lift the block A. Assume the weight of block-B as 1000N and the angle of friction of all connected system to be  $10^{\circ}$ .



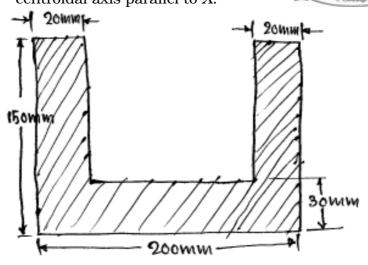
7 + 8

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8. a) Find the centroid of the shaded area as shown below.

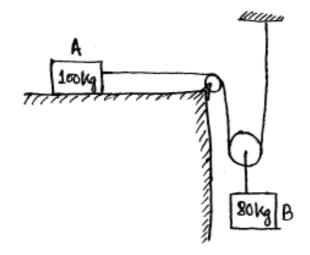


b) Find the moment of inertia of shaded area about the centroidal axis parallel to X.

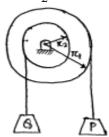


8 + 7

9. a) Two blocks of mass 100 kg and 80 kg are connected by a light inextensible string as shown in figure. Using the D' Alembert's principle find the acceleration of the blocks and tension in the string. Asseme co-efficient of friction  $\mu = 0.3$ .



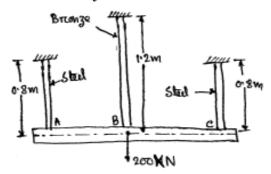
b) Two weights P and Q are hung and initially at rest as shown in figure. Find the velocity of the falling weight P when it covers a vertical distance of 3 metres. Given P = Q = 10N,  $r_2 = 100$  mm and  $r_1 = 50$  mm. 8 + 7



- 10. a) Find the volumetric strain for a triaxial stress system.
  - b) A rigid bar ABC weighing 180 kN is supported by three rods placed symmetrically as shown in figure. Assuming the bar to remain horizontal, determine the stress in each rod after a temperature rise of 25°C. The lower ends of the rods are assumed to be at the same level before the bar is attached and the change in temperature.

Given : Area of steel rod = 800 mm<sup>2</sup>; Area of bronze rod = 1400 mm<sup>2</sup>;  $E_{st} = 2 \times 10^5 \text{ N/mm}^2$ ;  $E_{br} = 0.8 \times 10^5 \text{ N/mm}^2$ ;  $\alpha_{st} = 12 \times 10^{-6} / ^{\circ}\text{C}$ ;  $\alpha_{br} = 20 \times 10^{-6} / ^{\circ}\text{C}$ 

What will be the stress in each rod if the weight of the bar is 120 kN only?



- 11. a) Explain the principle of transmissibility and parallelogram law.
  - b) A bus is starting to move with an acceleration of  $0.5 \text{ m/sec}^2$ . A man standing 21 m behind the bus runs at constant speed of 5 m/sec. Find the time at which the man will overtake the bus.
  - c) During a free kick, a football player kicks a football of 250 g mass, which is at rest and it leaves his foot with a velocity of 25 m/sec at an angle of 25° with respect to the ground level. Determine the force exerted by the player if the duration of the strike is 1/60th of a second.

5 + 5 + 5