



Name : .....

Roll No. : .....

Invigilator's Signature : .....

**CS/B.Tech(CE/OLD)/SEM-6/CE-604/2013**

**2013**

**STRUCTURAL ANALYSIS III**

Time Allotted : 3 Hours

Full Marks : 70

*The figures in the margin indicate full marks.*

*Candidates are required to give their answers in their own words  
as far as practicable.*

**GROUP – A**

**( Multiple Choice Type Questions )**

1. Choose the correct alternatives for any *ten* of the following :

$$10 \times 1 = 10$$

- i) The rotational stiffness of a beam when far end is hinged

a)  $\frac{3EI}{L}$

b)  $\frac{2EI}{L}$

c)  $\frac{4EI}{L}$

d) None of these.

- ii) If  $\xi = 6\%$  then the logarithmic decrement is

a) 0.377

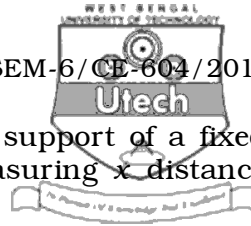
b) 0.378

c) 0.375

d) 0.376.



- iii) According to Muller Breslau principle for any reaction or stress component of a beam is obtained as a
- a) S.F. diagram for the beam
  - b) B. M. diagram for the beam
  - c) Deflection diagram for the beam
  - d) None of these.
- iv) In the horizontal load analysis the point of contra flexure lies at ..... point of the beam in the framed structure
- a) Middle
  - b) end
  - c) one third
  - d) none of these.
- v) A system is said to have under damped condition when
- a)  $c > c_{cr}$
  - b)  $c = c_{cr}$
  - c)  $c < c_{cr}$
  - d) all of these.
- vi) Flexibility and stiffness matrices for the system are
- a) equal
  - b) inverse
  - c) not related
  - d) direct.
- vii) The displacement function in case of truss element in finite element approach is
- a)  $a_1 + a_2 x$
  - b)  $a_1 x + a_2 x^2$
  - c)  $a_1 + a_2$
  - d) none of these.



viii) Influence line for B. M. at left hand support of a fixed beam is given by the equation, measuring  $x$  distance from left hand support

- a)  $\frac{x(l-x)^2}{l^2}$                       b)  $\frac{x(l+x)^2}{l^2}$
- c)  $\frac{x^2(l-x)^2}{l^2}$                       d) none of these.

ix) The degree of relative isolation is

- a) Transmissibility                      b) Resonance
- c) Damping                      d) Vibration.

x) The stage when forcing frequency equals natural frequency of the system is known as

- a) Resonance                      b) Steady state
- c) Transient response                      d) None of these.

xi) Direct stresses in columns are proportional to their distances from the C.G. of the frame is the assumption in

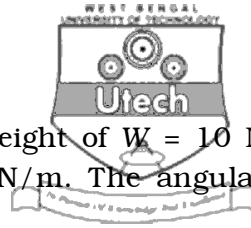
- a) Cantilever method                      b) Portal method
- c) Factor method                      d) None of these.

xii) The shape of the displacement associated with degrees of freedom is called

- a) Interpolation function
- b) Displacement function
- c) Shape function
- d) None of these.

xiii) Structural analysis technique which involves discretization and numerical approximation is called

- a) Finite difference method
- b) Finite element method
- c) Finite strip method
- d) All of these.



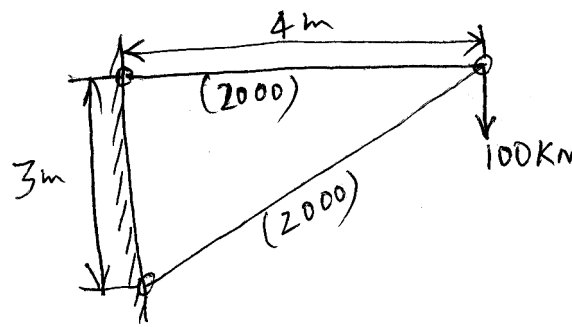
- xiv) A vibrating system consisting of a weight of  $W = 10 \text{ N}$  and a spring with stiffness  $k = 20 \text{ N/m}$ . The angular natural frequency of the system is
- a)  $4.43$                                       b)  $5.4$   
c)  $2.5$                                          d)  $3.25$ .
- xv) Numerical approach where the differential equations are converted to ordinary algebraic equations is
- a) Finite difference method  
b) Finite element method  
c) Newmark's method  
d) All of these.

### GROUP – B

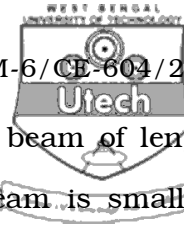
#### ( Short Answer Type Questions )

Answer any *three* of the following.                       $3 \times 5 = 15$

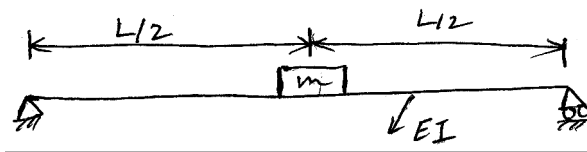
2. Develop the stiffness matrix for the pin jointed truss as shown in the Fig. The cross sectional area of each member is  $2000 \text{ mm}^2$ . The  $E = 200 \text{ KN/mm}^2$ .



3. Derive 4th order derivatives in finite difference technique.



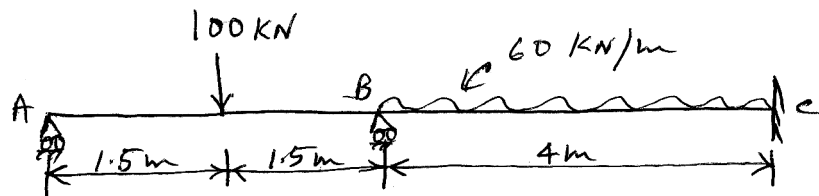
4. A mass  $m$  is attached to the midpoint of a beam of length  $L$  as shown in the Fig. the mass of the beam is small in comparison to  $m$ . Determine the spring constant and the frequency of the free vibration of the beam in the vertical direction. The beam has a uniform flexural rigidity  $EI$ .



5. Draw the influence line diagram for the reaction at  $B$ .



6. Write short notes on the following :
- System stiffness matrix
  - Shape functions
  - Critically damped system.
7. Develop the flexibility matrix for the continuous beam as shown in the Fig.





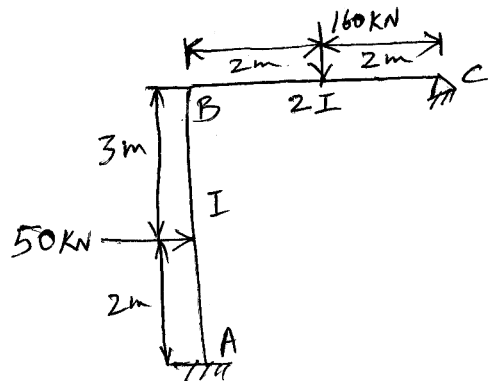
**GROUP – C**

**( Long Answer Type Questions )**

Answer any *three* of the following.

$3 \times 15 = 45$

8. Analyse the structure by matrix method as shown in the Fig.



9. The steel rigid frame supports a rotating machine which exerts a horizontal force at the girder level of  $50000 \sin 11t$  N. Assuming 4 percent critical damping, 5000 kg mass acting at beam level and columns mass less. Determine :

- (i) Steady state amplitude of vibration
- (ii) Transmissibility of the motion to the girder
- (iii) The max. Shearing force in the supporting columns
- (iv) Damped natural frequency
- (v) Logarithmic decrement
- (vi) Dynamic magnification factor
- (vii) Max. bending moment
- (viii) Max. shearing stress in the columns



(ix) Max. relative displacement

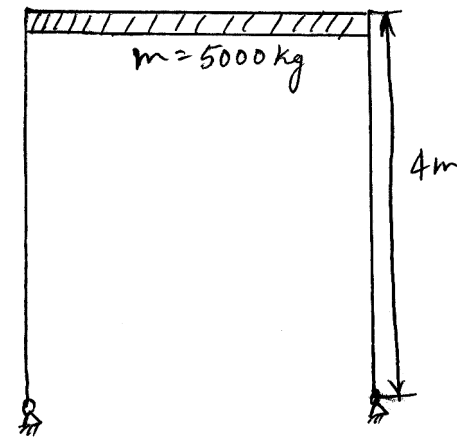
(x) Time interval between consecutive max. amplitudes.

Take length of the beam = 4m

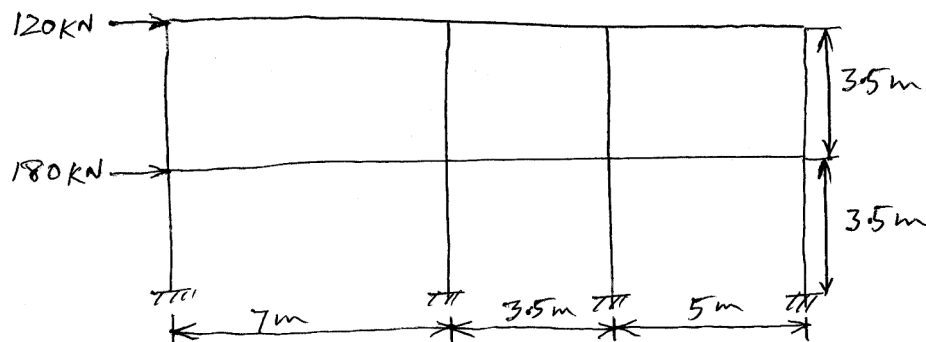
Length of the columns = 4 m

$$E = 2.1 \times 10^{11} \text{ N/m}^2$$

$$I \text{ for columns} = 1500 \times 10^{-7} \text{ m}^4$$



10. Analyse the frame as shown in the Fig. by portal or cantilever method. Assume const.  $EI$  for all beams and columns. Draw the relevant BMD and SFD.





11. A simply supported beam of span  $l$  carries *udl* of intensity  $w$  over the entire span. Determine the bending moments and the deflections at quarter span, mid span and three quarter span. Also determine the actual *BM* and the deflection at these points and calculate the percentage the percentage of error by finite difference method or relaxation technique. Take  $EI = \text{const.}$
12. Derive the stiffness matrix for a beam element using finite element method. Neglect the axial deformation.

=====