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| Invigilator's Signature : | |

PHYSICS-I

Time Allotted: 3 Hours Full Marks: 70

The figures in the margin indicate full marks.

Candidates are required to give their answers in their own words as far as practicable.

GROUP - A (Multiple Choice Type Questions)

1. Choose the correct alternatives for any *ten* of the following :

$$10 \times 1 = 10$$

- i) The deBroglie wavelength of a moving electron subjected to a potential V is
 - a) $\frac{1.26}{\sqrt{V}}$

b) $\frac{12.26}{\sqrt{V}}$

c) $\frac{122.6}{\sqrt{V}}$

d) $\frac{1226}{\sqrt{V}}$

(consider the appropriate units).

- ii) For Laser action to occur, the medium used must have at least
 - a) 2 energy levels
- b) 4 energy levels
- c) 3 energy levels
- d) one energy level.

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- The Miller indices of a plane holding the intercepts iii) $\frac{a}{2}$, b, 3c is
 - (361)a)

(611)b)

c) (631)

- (321). d)
- The intensity of principal maxima in the spectrum of iv) grating with N number of lines is proportional to
 - a)

b)

 N^2 c)

- d) $\frac{1}{N^2}$.
- To get a circular Lissajous figure, the phase difference v) (ϕ) and the amplitude (a and b) of two superimposing, mutually perpendicular SHMs respectively
 - $\phi = 0$, a = b
- b) $\phi = \frac{\pi}{2}$, a = b
- c) $\phi = \frac{\pi}{2}$, $a \neq b$
- d) $\phi = \frac{\pi}{4}$, $a \neq b$.
- *X*-ray is suitable for crystallography because vi)
 - *X*-ray is electromagnetic a)
 - X-ray is neutral b)
 - X-ray wavelength is in same order of interatomic c) spacing of Crystal
 - d) *X*-ray is hard penetrating.
- In Fraunhofer diffraction, the wave front is vii)
 - Cylindrical a)
- b) **Spherical**

c) **Plane**

Circular. d)

- viii) The refractive indices of *E*-ray and *O*-ray are respectively 1·65 and 1·45. Then, the thickness of the material required for a quarterwave plate for light of wavelength 500 nm is
 - a) 250 nm
- b) 125 nm
- c) 625 nm
- d) 740 nm.
- ix) If a spring of force constant *K* is cut into three equal parts, then the force constant of each part is
 - a) $\frac{K}{3}$

b) 3K

c) 1

- \mathbf{d}) K.
- x) Davisson-Germer experiment is related with
 - a) Interference
- b) Thermionic emission
- c) Phosphorescence
- d) Electron diffraction.
- xi) The velocity of a particle when its mass becomes twice its rest mass is
 - a) 0.5c

b) 0.72c

- c) 0.866c
- d) c

(where c is the speed of light in vacuum).

- xii) Which of the following pairs cannot be simultaneously measured?
 - a) p_x , p_y
- b) y, p_y

c) p_{x} , z

d) p_{x}, p_{z} .

xiii) The Compton shift $\Delta\lambda$ and Compton wavelength λ of a particle are equal if the angle of scattering is

a) 0°

b) 90°

c) 180°

d) 45°.

xiv) For holography system, the exposure time is of the order of

- a) 5 seconds and depends on the colour of the object
- b) nearly 2 seconds
- c) 1 second
- d) 50 seconds.

xv) The emissive power of a black body kept at an absolute temperature T is proportional to

a) T^4

b) T³

c) T^{-1}

d) *T*.

GROUP - B

(Short Answer Type Questions)

Answer any three of the following.

 $3 \times 5 = 15$

2. The displacement of any particle at any instant t is given by $x = 3 \cos \omega t + 4 \sin \omega t$. Show that the motion is simple harmonic. What is the amplitude of this oscillation ? Show that its kinetic energy oscillates with angular frequency 2ω .

2 + 1 + 2



- 3. a) What is diffraction of light?
 - b) Draw the intensity distribution pattern of diffraction grating.
 - c) Two slits in Young's double slit experiment are 1.3 mm apart from each other and the screen is placed 1.6 m away from the slits. Calculate the distance of the 4th bright fringe. The wavelength of the light used is 6000 Å. 1 + 1 + 3
- 4. a) State Bragg's law.
 - b) Cs metal (atomic weight 130) has a cubic unit cell of lattice constant 0.6 nm. If the density of Cs is 2 gm/cc, determine whether the unit cell is SC, BCC or FCC. 1+4
- 5. a) Explain Brewster's law.
 - b) Show that when light is incident on a transparent substance at the polarizing angle, the reflected and the refracted rays are perpendicular to each other. 2 + 3
- 6. a) Deduce Stefan's law from Planck's radiation law.
 - b) What is population inversion? Why is it needed for lasing action? 3+1+1

GROUP - C

(Long Answer Type Questions)

Answer any *three* of the following. $3 \times 15 = 45$

- 7. a) State Heisenberg's uncertainty principle.
- 2
- b) Using this principle, prove that a free electron cannot exist in an atomic nucleus.
- c) Write down the uncertainty relation for energy and time.
- d) Find the wavelength spread of a 1 nano-second pulse from a ruby LASER with a wavelength of 630 nm.

| e) | Show that the group velocity | ty of | the wave packet |
|------------|--------------------------------|--------|---------------------|
| | representing a particle is equ | ıal to | the velocity of the |
| | particle itself. | | 2 |

- f) Calculate the de Broglie wavelength of a baseball of mass 1 kg moving at a speed of 10 m/sec. Discuss the reason why its wave nature connot be observed.
- 8. a) State Malus law. A beam of polarized light makes an angle of 60° with the axis of the polaroid sheet. How much intensity of light is transmitted through the sheet? 2+4
 - b) What is a retardation plate? How can you distinguish between circularly polarized light and unpolarized light with the help of a quarter wave plate and a Nicol prism? 2+4
 - c) The critical angle of glass with respect to air is 41°.
 Find the refractive index of the medium and the angle of refraction of the light incident on the glass plate at the polarizing angle.
- 9. a) What are the differences between LASER and normal visible light?
 - b) Derive the relation between Einstein's A and B coefficients.
 - c) Calculate the ratio of stimulated to the spontaneous emission at a temperature 300 K for sodium D-line ($\lambda = 5890 \ \text{Å}$).

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- d) With the help of a neat diagram, briefly describe the construction of a Ruby LASER.
- e) Why is optical pumping not generally employed in case of a gas LASER?
- 10. a) Distinguish between interference and diffraction. Is energy conserved in interference phenomenon ? Explain. 3 + (1 + 2)
 - b) In a Newton's ring arrangement, the diameter of the 5th dark ring is 0.3 cm and the diameter of 25th dark ring is 0.8 cm. If the radius of curvature of the planoconvex lens is 100 cm, find the wavelength of the light used.
 - c) What are the conditions to get sustained interference pattern?
 - d) Show that the intensity of the 1st secondary maxima formed by a single slit Fraunhofer diffraction process is nearly 4.5% of the principal maxima.
- 11. a) Show that the fractional change in the natural frequency of a damped simple harmonic oscillator is $\frac{1}{8Q^2}$, where Q is the quality factor of the oscillator. 3
 - b) The displacement of a simple harmonic oscillator is given by $x = a \sin (\omega t + \theta)$. If the oscillations started at time t = 0 from a position x_0 with velocity $\dot{x} = v_0$, show that $\tan \theta = \frac{\omega x_0}{v_0}$ and $a = \left(x_0^2 + \frac{v_0^2}{\omega^2}\right)^{1/2}$.

- c) A particle of mass 2 kg is subjected to an elastic force per unit displacement 0.03 Nm⁻¹ and frictional force per unit velocity 0.005 Nm⁻¹s. If if is displaced through 2 cm and then released, find whether the resulting motion is oscillatory or not.
- d) The forced harmonic oscillators have displacement amplitude at frequencies $\omega_1=400~sec^{-1}$ and $\omega_2=600~sec^{-1}$.
 - Find the resonant frequency at which the displacement amplitude is maximum.
- e) Differentiate between amplitude resonance and velocity resonance for a forced harmonic oscillator. 2
- 12. a) In the continuous *X*-ray spectra, λ_{min} values are obtained for higher potential. Explain.
 - b) What do you mean by the terms "atoms per unit cell","cordination number" and "atomic packing factor"?
 - c) Show that the packing fraction of FCC is greater than BCC.
 - d) The density of BCC iron is 7.9 gm/cc and its atomic weight is 56. Calculate the length of the side of the cubic unit cell and nearest neighbouring distance.
 - e) The spacing of planes in a crystal is 1.2 Å and the angle for the 1st order Bragg's reflection is 30° . Determine the energy of the *X*-rays beam in eV.

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