OPERATIONS RESEARCH & OPTIMIZATION TECHNIQUES (SEMESTER - 4)

CS/B.Tech (CSE)/SEM-4/M(CS)-402/09



1.	Signature of Invigilator				a:	9			
2.	Reg. No. Signature of the Officer-in-Charge								
	Roll No. of the Candidate								

CS/B.Tech (CSE)/SEM-4/M(CS)-402/09 ENGINEERING & MANAGEMENT EXAMINATIONS, JUNE – 2009 OPERATIONS RESEARCH & OPTIMIZATION TECHNIQUES (SEMESTER - 4)

Time: 3 Hours [Full Marks: 70

INSTRUCTIONS TO THE CANDIDATES:

- 1. This Booklet is a Question-cum-Answer Booklet. The Booklet consists of **40 pages**. The questions of this concerned subject commence from Page No. 3.
- 2. a) In **Group A**, Questions are of Multiple Choice type. You have to write the correct choice in the box provided **against each question**.
 - b) For **Groups B** & **C** you have to answer the questions in the space provided marked 'Answer Sheet'. Questions of **Group B** are Short answer type. Questions of **Group C** are Long answer type. Write on both sides of the paper.
- 3. **Fill in your Roll No. in the box** provided as in your Admit Card before answering the questions.
- 4. Read the instructions given inside carefully before answering.
- 5. You should not forget to write the corresponding question numbers while answering.
- 6. Do not write your name or put any special mark in the booklet that may disclose your identity, which will render you liable to disqualification. Any candidate found copying will be subject to Disciplinary Action under the relevant rules.
- 7. Use of Mobile Phone and Programmable Calculator is totally prohibited in the examination hall.
- 8. You should return the booklet to the invigilator at the end of the examination and should not take any page of this booklet with you outside the examination hall, **which will lead to disqualification**.
- 9. Rough work, if necessary is to be done in this booklet only and cross it through.

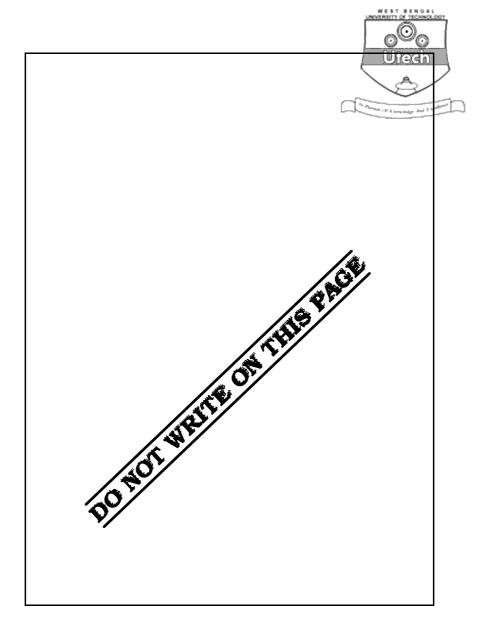
No additional sheets are to be used and no loose paper will be provided

FOR OFFICE USE / EVALUATION ONLY Marks Obtained Group - A Group - B Group - C Question Number Marks Obtained Signature

Head-Examiner/Co-Ordinator/Scrutineer

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engineering & management examinations; june 2009 OPERATIONS RESEARCH & OPTIMIZATION TECHNIQUES SEMESTER - 4

Time: 3 Hours [Full Marks: 70

Graph sheets are provided at the end of this booklet.

GROUP - A

(Multiple Choice Type Questions)

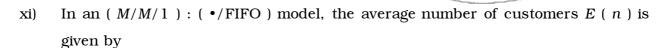
			(-JP- 3	,,	
l.	Choose the correct alternatives for any <i>ten</i> of the following :					
	i)		le solution for the constrain	at equations		
		will	consist of			
		a)	(2m + 1) variables	b)	(2m-1) variables	
		c)	2m variables	d)	$2m^2$ variables.	
	ii)	For	an LPP the dual of the dual prob	olem is	called the	
		a)	primal problem	b)	dual problem	
		c)	both (a) and (b)	d)	none of these	
	iii)	Wha	t is the number of basic non-va	riables	in the balanced TP with 4 r	ows and
		5 co	lumns ?			
		a)	4	b)	5	
		c)	12	d)	20.	
	iv)	The	full form of CPM is			
		a)	crash project management	b)	critical path management	
		c)	critical path method	d)	none of these.	



		4			
v)	A ne	cessary and sufficient condition	for a l	pasic solution to a maximizing	problem
	to be	e optimal is that (for all j)		O O O	
	a)	$Z_j - C_j \ge 0$	b)	$Z_j - C_j \le 0$	
	c)	$Z_j - C_j = 0$	d)	$Z_j - C_j < 0 \text{ or } Z_j - C_j > 0.$	
vi)	The	basic feasible solutions of the sy	ystem (of equations	
		$x_1 + x_2 + x_3 = 8$			
		$3x_1 + 2x_2 = 18$			
	are				
	a)	(2,6,0),(6,0,2)	b)	(1,7,0),(7,1,0)	
	c)	no basic solution	d)	none of these.	
vii)	In a	n assignment problem, the min	imum	number of lines covering all z	eroes in
	the 1	reduced cost matrix of order n co	an be		
	a)	at most n	b)	n + 1	
	c)	n – 1	d)	at least n .	
viii)	Give	n a system of m simultaneous li	near eo	quations in n unknown variable	s
	(m -	< n), the number of basic variab	oles will	be	
	a)	m	b)	n	
	c)	n-m	d)	m-n.	
ix)	If th	ere are n workers and n jobs, th	ere wo	uld be	
	a)	n! solutions	b)	(n-1)! solutions	
	c)	$(n!)^n$ solutions	d)	n solutions.	



- x) The point of intersection of a pure strategy game is called
 - a) value of the game
- b) two-person
- c) mixed strategy game
- d) none of the



a) ρ^n

b) $\frac{\rho}{1-\rho}$

c) $\frac{\rho^2}{1-\rho}$

d) None of these.

xii) An assignment problem is a special type of

- a) transportation problem
- b) LPP
- c) inventory problem
- d) none of these.

xiii) In a fair game the value of the game is

a) 1

b) 0

c) unbounded

d) none of these.

xiv) The value of the game having the following pay-off matrix is

	B_{1}	B_2	B_3
A_{1}	10	2	3
A_2	7	6	8
A 3	0	3	1

a) 6

b) 10

c) 8

d) 2.

xv) An assignment problem can be solved by

- a) Hungarian Method
- b) VAM
- c) Matrix Minima Method
- d) Dominance Principle.



GROUP – B

(Short Answer Type Questions)

Answer any three of the following.



 $3 \times 5 = 15$

2. Show that the set given by

$$X = \left\{ \left(x_{1}, x_{2} \right) : 4x_{1}^{2} + 9x_{2}^{2} \le 36 \right\}$$

is a convex set.

3. Solve the following game problem:

	Player B	I	II	III	<i>IV</i>	
	Г і	3	2	4	0]	
DI A	II	3	4	2	4	
Player A	III	4	2	4	0	
	L _{IV}	0	4	0	8	l

4. Write the LPP in its standard form:

Max (
$$Z$$
) = $x_1 - 3x_2 + 5x_3$

subject to

$$x_1 + x_2 + x_3 \le 7$$

$$x_1 - x_2 + x_3 \ge 2$$

$$3x_1 - x_2 + 2x_3 = -5$$

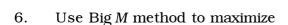
 x_1 , $x_2 \ge 0$ and x_3 is unrestricted.



5. Find any one of the basic feasible solutions of the following system of equations :

$$x_1 + 2x_2 + 3x_3 = 6$$

$$2x_1 - x_2 + 4x_3 = 4$$



$$Z = 3x_1 - x_2$$

subject to

$$2x_1 + x_2 \ge 2$$

$$x_1 + 3x_2 \le 3$$

$$x_2 \le 4$$

$$x_1, x_2 \ge 0.$$

GROUP - C

(Long Answer Type Questions)

Answer any three of the following.

 $3 \times 15 = 45$

15

7. Use the dual simplex method to solve the following L.P.P.:

Maximize
$$Z = -2x_1 - 2x_2 - 4x_3$$

subject to the constraints

$$2x_1 + 3x_2 + 5x_3 \ge 2$$

$$3x_1 + x_2 + 7x_3 \le 3$$

$$x_1 + 4x_2 + 6x_3 \le 5$$

$$x_1, x_2, x_3 \ge 0.$$



8. a) Solve the transportation problem by VAM method and checking optimality find optimum cost.

	D_{1}	D_2	D_3	Utech
<i>O</i> ₁	4	3	2	10
O_2	1	5	0	13
O_3	3	8	5	12
	8	5	4	

b) Find the assignment of Machines to the Jobs, that will maximize the profit.

1	62	78	50	101	82
2	71	84	61	73	59
3	87	92	111	71	81
4	48	64	87	77	80

6

3

2

ΑВ

9. A small maintenance project consists of the following jobs whose precedence relationship is given below:

	Estimated Duration (weeks)				
Activity	Optimistic	Most Likely	Pessimistic		
1-2	1	1	7		
1-3	1	4	7		
1-4	2	2	8		
2-5	1	1	1		
3-5	2	5	14		
4-6	2	5	8		
5-6	3	6	15		

- a) Draw the project network.
- b) Find the expected duration and variance of each activity.

c) Calculate the early and late occurrence for each event and the expected project length.

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- d) Calculate the variance and standard deviations of project length.
- e) What is the probability that the project will be complete
 - i) 4 weeks earlier than expected?
 - ii) not more than 4 weeks later than expected?

If the project due date is 19 weeks, what is the probability of meeting the due date?

[Given that
$$\phi$$
 (1.33) = 04082 and Φ (0.666) = 0.2514]

2 + 2 + 1

12

10. a) A medium project has twelve distinct activities which are to be further analyzed by using PERT. The following relevant information is also given in tabular form :

Activity	Duada assa an	Most optimistic	Most likely	Most pessimistic
Activity	Predecessor Activity	time (in days)	time (in days)	time (in days)
A	None	2	2	2
В	None	1	3	7
C	A	4	7	8
D	A	3	5	7
E	В	2	6	9
F	В	5	9	11
G	C, D	3	6	8
Н	E	2	6	9
I	C, D	3	5	8
J	G, H	1	3	4
K	F	4	8	11
L	J, K	2	5	7

- i) Present these activities on the PERT network.
- ii) Find the expected total float for each activity.
- iii) Determine the average critical path.
- iv) Within how many days is it expected to complete the project with 99% chance?
- b) Find graphically the non-negative values of the variables x and y which satisfy the constraints $3x + 5y \le 15$, $5x + 2y \le 10$ and which maximizes the linear form z = 6x + 3y.



- 11. a) Customers arrive at a one-window drive-in bank according to a Poisson distribution with mean 10 per hour. Service time per customer is exponential with mean 5 minutes. The space in front of the window, including that for the serviced car can accommodate a maximum of 3 cars. Other cars can wait outside this space.
 - i) What is the probability that an arriving customer can drive directly to the space in front of the window?
 - ii) What is the probability that an arriving customer will have to wait outside the indicated space ?
 - iii) How long is an arriving customer expected to wait before starting service?
 - iv) How many spaces should be provided in front of the window so that all the arriving customers can wait in front of the window at least 20% of the time? $4 \times 2\frac{1}{2} = 10$
 - b) Find the dual of the following LPP:

$$Minimize Z = 3x_1 + x_2$$

subject to
$$x_1 + x_2 \ge 1$$

$$2x_1 + 3x_2 \ge 2$$

$$x_1, x_2 \ge 0.$$
 5

12. a) Solve the travelling salesman problem with the following cost matrix [c_{ij}] 4 ∞ 4 where, c_{ij} is the cost of travelling from city i to city j:

	1	2	3	4
1	•	15	30	4
2	6	•	4	1
3	10	15	•	16
4	7	18	13	•



b) Solve the following Transportation Problem using the Vogel's Approximation Method:

	D_{1}	D_2	D_3
O 1	2	7	4
O 2	3	3	1
O 3	5	4	7
O 4	1	6	2

Also test the optimality of the solution obtained using Modified Distribution Method. 10

END