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Q) We define $f(x, y)$ as no. of different corresponding bits in the binary representation of x and y .
for example $f(2, 3) = 2$.

Given an array of n integers need to return all pairs possible for i, j , where corresponding bits are not same & have sum.

- Test cases:

$$I/p = [2, 3]$$

O/p = 2 (Explanation)

$$\begin{array}{r} 0 \ 1 \ 0 \\ 0 \ 1 \ 1 \\ \hline 1 \quad + \quad 1 \\ = 2 \ O/p \end{array}$$

Same for $[1, 2, 5] = 8 \leftarrow \text{Sol'n}$

Solution → ~~Naive Solution: pairs * bits to compare~~
for every possible pair in the array check
or compare the bits as the bits are different
increase the count, complexity will be high
possibly $O(n^2)$

② Better solution →

Count no. of 0's & 1's for each position
of bits & then compare them.

Pseudo code:

Sum of different bits (A, n):

$$\text{total} \doteq 0$$

for bit 0 to 31:

Count 1 $\leftarrow 0$

for $i = 0$ to $n-1$;
 $\{ A[i] \text{ And } (1 \ll \text{bit}) \} \neq 0$;

Count 1 = Count 1 + 1

Count 0 = $n - \text{Count 1}$

Total = Total $(\text{Count 1} \times \text{Count 0})$

return $2 \times \text{Total}$;

Explanation:

- Every no. is represented in binary, we process each bit position from 0 to 3.
- for a fixed bit we count how many array elements have the bit set, (Count 1)
- Remaining elements already have bit unset
 $\text{Count 0} = (n - \text{Count 1})$
- Every pair having one '1' & one '0'
Contributivity 1 to the answer.
- So Contribution of one bit = $(\text{Count 1} \times \text{Count 0})$
we sum this for all bits
- Since problem consider ordered pairs means $(i, j) \neq (j, i)$. No we multiply answer by 2