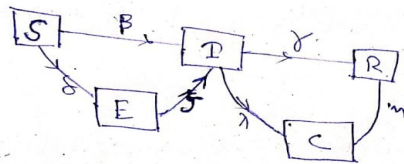


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A) Compartmental Schematic Diagram of the Model :



S = 'Susceptible'

I = 'Infected'

E = 'Exposed'

C = "CHRONICAL STAGE"

N = "TOTAL POPULATION"

R = "Recovered"

TRANSMISSION RATE

$S \rightarrow I$: β

$S \rightarrow E$: σ

$E \rightarrow I$: σ

$I \rightarrow C$: λ

$I \rightarrow R$: γ

$C \rightarrow R$: μ

So, the system has 5 variables and 6 parameters.

B) Table for Variables , Parameters name and Physical significance of Parameters

Variables	Parameters	Physical significance of parameters
Susceptible	Disease spreading rate (β) $S \rightarrow I$	From the sick and infected people the diseases get spread to the susceptible people who do not have any infection but can be infected if they remain in contact with an infected person. To stop the shift from susceptible to infected the process of lockdown is followed.

Exposed	Exposure rate (δ) $S \rightarrow E$	From the susceptible people to the exposed people the transition occurs when a person (susceptible) remains in contact with a infected person and is exposed to the disease . the process occur unconsciously as the infected people don't show symptoms immediately
Infected	Testing rate (τ) $E \rightarrow I$	The exposed people carry the disease but don't show any symptoms they can be found out only by testing and rapid testing can only solve this problem. Testing rate has an important role here and helps us to control the disease.
Chronical	Recovery rate (γ) $I \rightarrow R$	Depending on the availability of proper facilities like medicines and beds at hospitals and critical care units.the rate of recovery varies. N.b.: - people who passed away are also considered recovered as they can no longer be infected nor can they transfer their disease and so technically they can be considered recovered.
Recovered	Chronical rate(λ) $I \rightarrow C$	This parameter may depend upon various factors like surroundings or environment hygiene condition, climate, Age of infected people ,Condition of health, having any other disease before got infected (high blood pressure, asthma , high glucose level) or any genetical influence and also unavailability of proper medicine, space can make the infected person go through this chronical stage rather than got recovered.
	Chronical Recovery rate(m) $C \rightarrow R$	It is similar to the recovery rate but some extra care and medications are required here. Space availability is a constraint here.

C)

PYTHON CODE FOR DETERMINING THE MODEL OF INFECTION:

```
import EoN
```

```

import networkx as nx
from collections import defaultdict
import matplotlib.pyplot as plt
import random

N = 5000
G = nx.fast_gnp_random_graph(N, 6./(N-1))

#We have defined our network ( which is a random graph) with N number o
f nodes
#5 is the number that decides how densely the nodes are connected

#We show how node and edge attributes in the contact network 'G' can be
used
#to scale the transmission rates.

#Let us define H for the spotaneous transitions
H = nx.DiGraph()
H.add_node('S')
#
H.add_edge('I', 'R', rate = 0.5)
H.add_edge('I', 'C', rate = 0.5)
H.add_edge('C', 'R', rate = 0.25)
H.add_edge('E', 'I', rate = 0.65)
# The line above states that the I to 'R' transition occurs with rate
0.5
#
#Let us define J for the induced transitions
#
J = nx.DiGraph()
J.add_edge(('I', 'S'), ('I', 'I'), rate = 0.6)
J.add_edge(('E', 'S'), ('E', 'E'), rate = 0.35)
# The line above states that an 'I' individual will cause an 'S' indiv
idual
# to transition to 'I' with rate equal to 0.6

#Defining initial conditions
IC = defaultdict(lambda: 'S')
for node in range(10):
    IC[node] = 'I'
for node in range(40):
    IC[node] = 'E'
return_statuses = ('S', 'E', 'I', 'C', 'R')

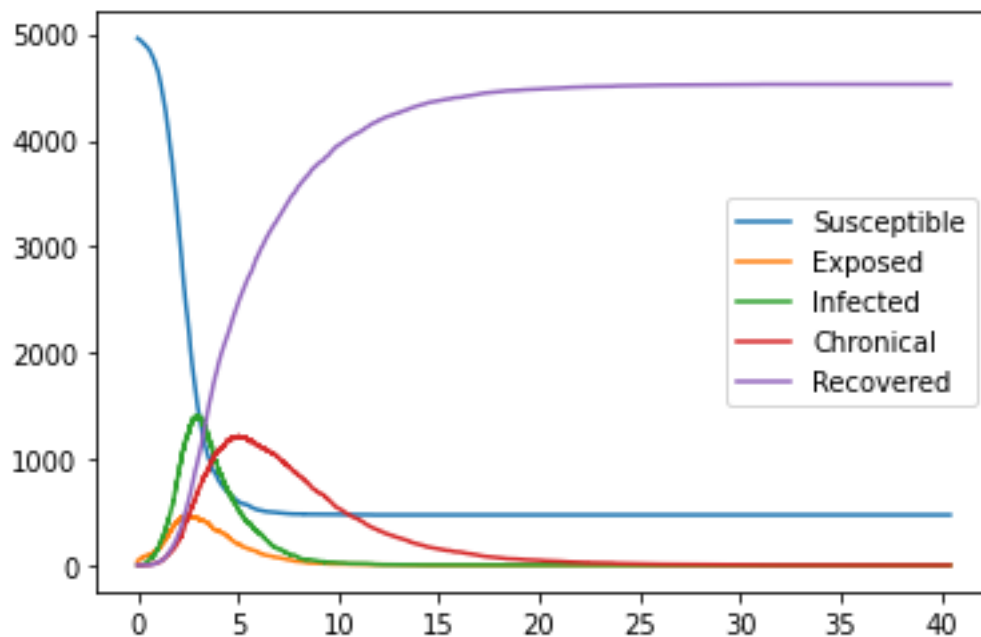
t, S, E, I, C, R = EoN.Gillespie_simple_contagion(G, H, J, IC, return_sta
tuses, tmax = float('Inf'))

plt.plot(t, S, label = 'Susceptible')
plt.plot(t, E, label = 'Exposed')
plt.plot(t, I, label = 'Infected')
plt.plot(t, C, label = 'Chronical')
plt.plot(t, R, label = 'Recovered')
plt.legend()

```

```
plt.savefig('SEICR.png')
```

#FOR TRYING OUT SIS MODEL, THE SAME CODE WOULD WORK IF YOU MODFIY ACCORDINGLY. THE ONLY CHANGE YOU NEED IS SET `tmax=20` INSTEAD OF `tmax = float('Inf')`. THIS DICTATES THE FINISHING TIME AND DOES NOT LOOK FOR AN AUTOMATIC SATURATION. THINK ABOUT WHY THIS IS NEEDED IN SIS.



Spontaneous Process

```
('I', 'R', rate = 0.5)
('I', 'C', rate = 0.5)
('C', 'R', rate = 0.25)
('E', 'I', rate = 0.65)
```

Induced Process

```
((('I', 'S'), ('I', 'I')), rate = 0.6)
((('E', 'S'), ('E', 'E')), rate = 0.35)
```

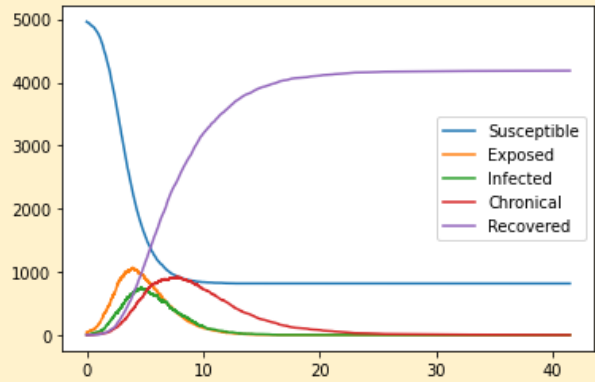
No. of Initially infected people = 10

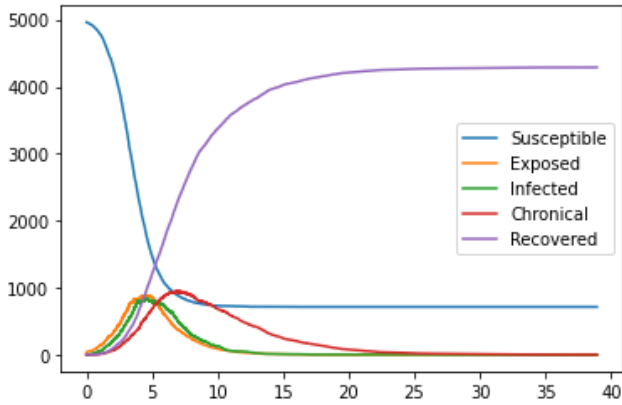
No. of Initially exposed people = 40

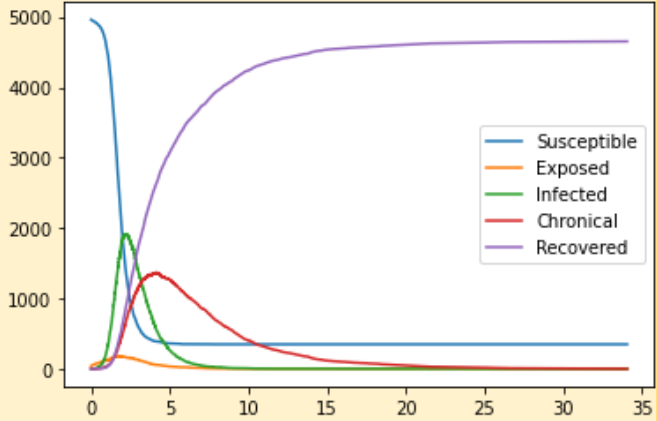
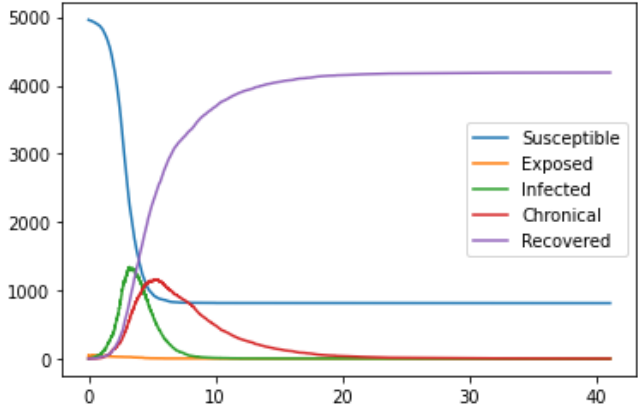
Total population, $N = 5000$

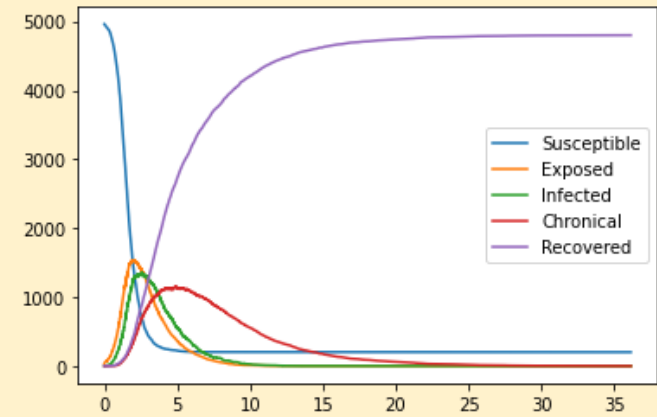
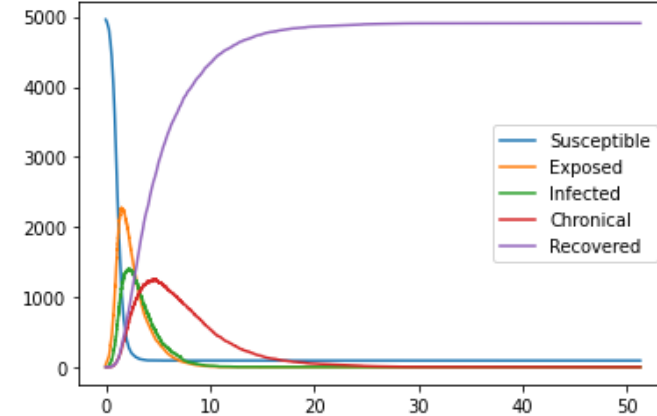
Average Degree = 6

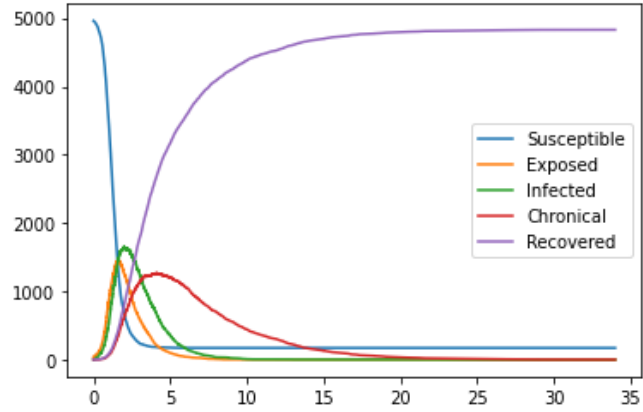
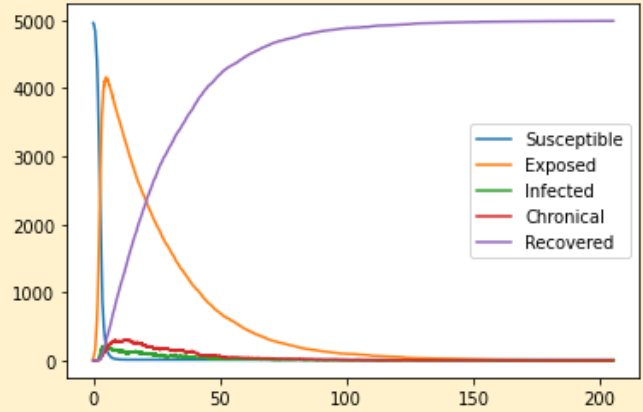
D)

SL No.	Parameters	Different Values of Parameters	Effect of the parameter on epidemic
1.	Disease spreading rate (β) S I	0.1	<p>Compared to the previous one (where $\beta = 0.6$) here saturated value of susceptible is more and for recovered it is low, as comparatively less people got sick overall so after end of epidemic more people remain susceptible and as then rest three variables become 0 so naturally no. of recovered people (total population - susceptible) go less.</p>  <p>As S I transition is low so the variable infected is taking more time to reach at peak however keeping S E and E I transition rate fixed denotes that S I direct transition rate is too low and is going on indirectly via E variable, introducing a delay so ultimately recovery would take much time and we can see in graph variable R is taking slightly more time (5 units time) to reach its saturated value. Similarly for susceptible also. And as all four variables are connected to I so its low peak value and low increasing rate results low peak value for chronical and recovered. So ultimately the delay is propagated resulting long-last duration.</p>

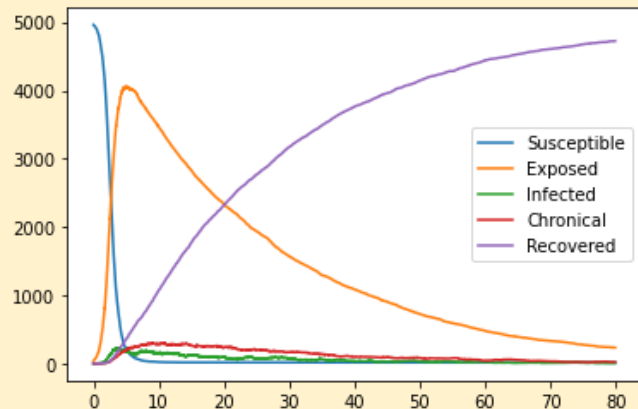
			?? why exposed got high whyyyy???
	0.25	<p>Now the rate for S I & S E is quite nearby values resulting almost same increasing rate and peak value for both I & E. Effect on other variables' values remain similar as discussed in previous.</p> 	
	0.9	<p>Compared to the previous one (where $\beta = 0.6$) here saturated value of susceptible is low and for recovered it is more, as comparatively more people got sick overall so after end of epidemic more people have gone through the process and got recovered and less remained susceptible.</p> <p>As S I transition is high so the variable infected reaches at peak too fast however keeping S E and E I transition rate fixed denotes that S I direct transition rate is too fast and is going on indirectly via E variable, introducing a delay but direct transition dominates here so ultimately recovery would take less time and we can see in graph variable R quickly reaches its saturated value. Similarly for susceptible also. And as all four variables are connected to I so</p>	

			<p>it's high peak value and high increasing rate results high peak value for chronical and recovered. So ultimately the endemic got slightly short-durated.</p>  <p>We can see here peak value of exposed significantly go down. But why????</p>
2.	<p>Exposure rate (δ)</p> <p>S E</p>	0.1	 <p>Saturated value of susceptible is comparatively more and that for recovered is low because overallly less people are sick and also peak value of infected is slightly low because of indirect transmission from S via E got low. But no delay is significantly seen in this case. Variable exposed almost got</p>

			nullified. Peak of chronical is slightly less as peak of infected got slightly lower.
	0.6		<p>Now the rate for S I & S E is quite nearby values resulting almost same increasing rate and peak value for both I & E. Saturated value of Susceptible go low and for recovered high. Peak and rate of chronical remains almost same.</p>
	0.9		<p>Saturated value of susceptible has gone too low and having fast decay also similarly for recovered it's too high denotes almost every person of the population have gone through the process testing and recovery and got recovered, very less no. of people remained susceptible. Peak and rate of Chronical remain almost same.</p>

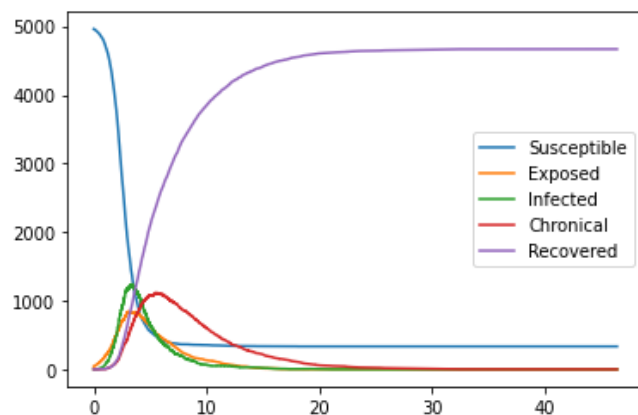
			<p>In this case if we increase test rate then the peak value of infected is going high and effects on other variables are almost same. (we can see in the following graph)</p> 
3.	Testing rate (τ) E I	0.04	<p>Too low testing rate denotes that the indirect transmission rate from S to E almost got nullified. And hence peak of infected is quite low and slowly the exposed are tested and moved to the box of infected but rate is too slow that exposed reached peak value too fast and over all sick people is too much then recovery rate is also slow and ultimately the epidemic is long-last for maximum duration out of all the other cases.</p>  <p>As chronical is connected directly to infected box it's</p>

rate and peak value also got lowered.
Here **enlarged view** is shown:

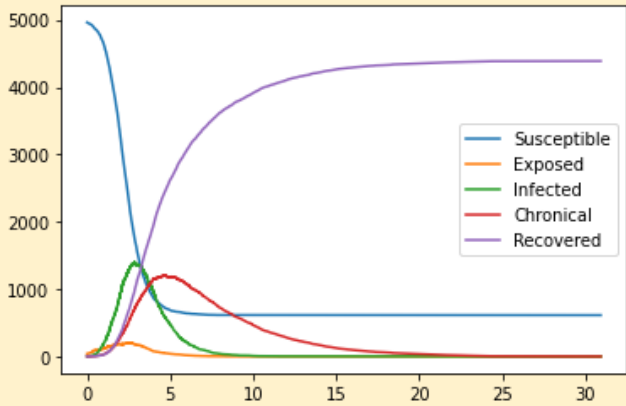
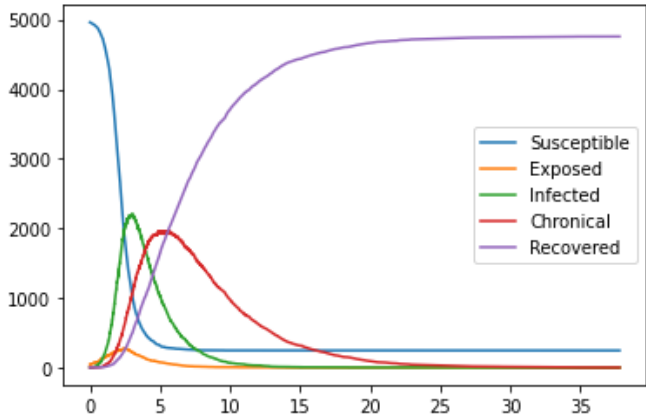


So, Ultimately we can conclude that it's the worst case in comparison to all possible changes.

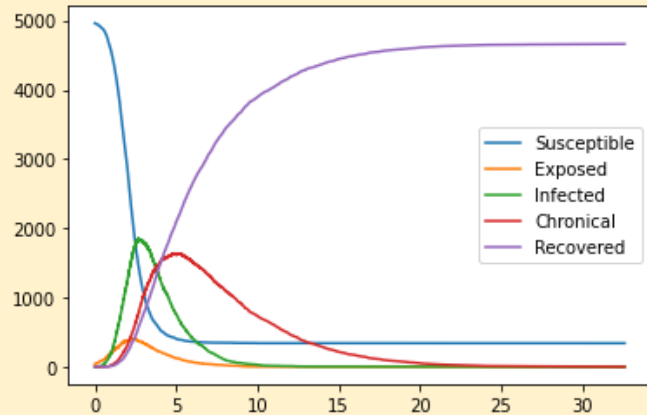
0.4



Moderate testing rate ensures decent values for all variables. The rate of increasing the value of infected is much than that of exposed. Saturated value of recovered and susceptible are also at moderate level. No significant change in peak value or rate of chronical.

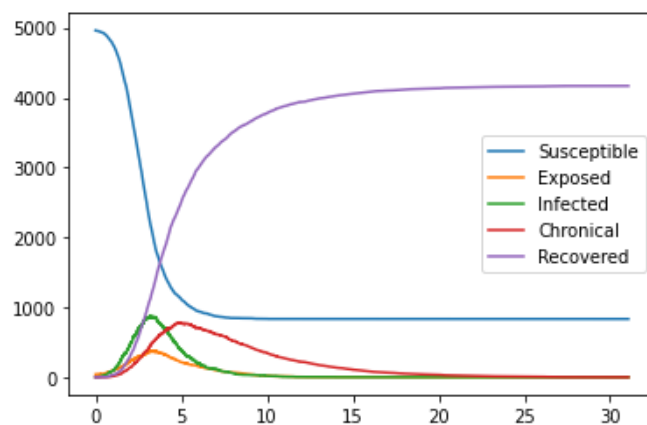
		0.95	 <p>High testing rate ensures that the variable exposed doesn't get the chance to reach to its peak value because before that testing is done and so the rate and peak of exposed almost got nullified.</p>
4.	Recovery rate (γ) I R	0.1	 <p>Low recovery rate denotes unavailability of medicine, well infrastructure ,space so that infected rate goes high and so the chronical rate and peak value. Although indirect transmission from I to R via C variable is taking place so it is introducing a slight delay but saturated value of recovered got slight high and for susceptible it's low. And ultimately the duration slightly increased (about 5 units time much)</p> <p>But why exposed got low????</p>

0.25

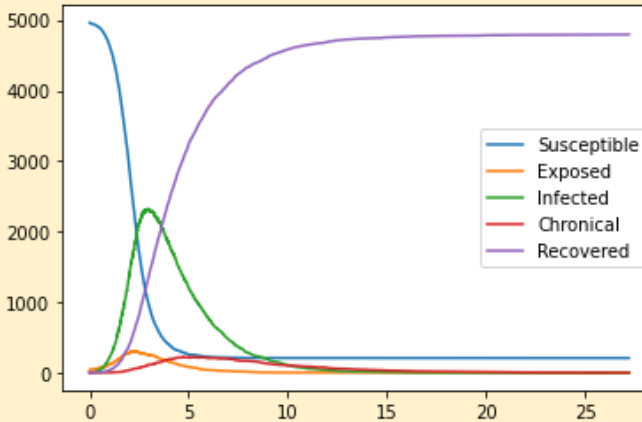
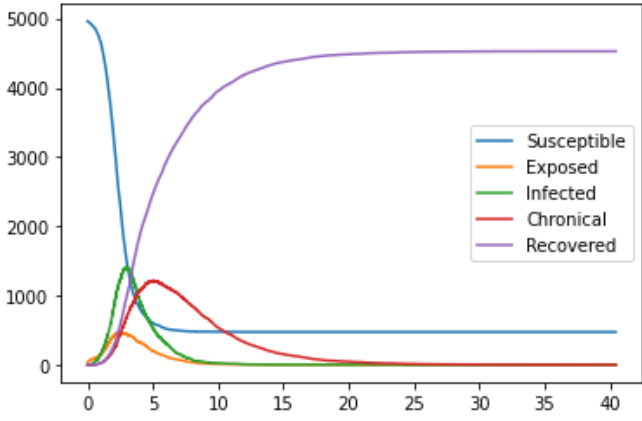


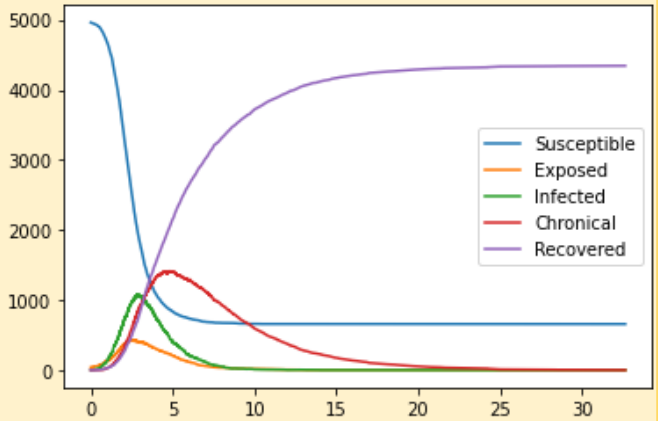
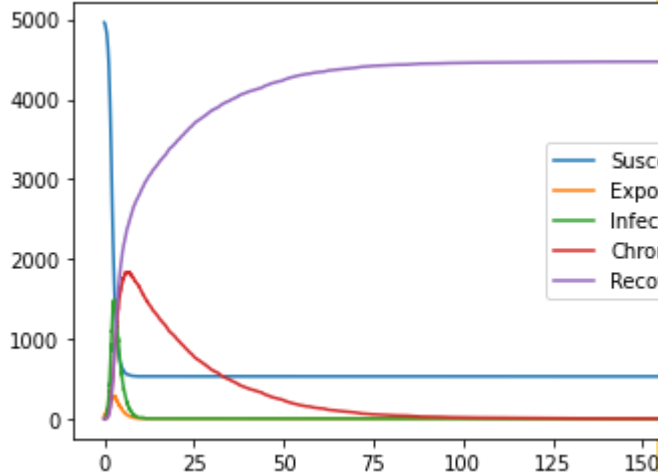
No significant change in Exposed rate and peak value. Comparatively high value for peak of infected and the rate also. And so the chronical (similar changes). And slight less rate of recovery results increased duration period. Saturated value of susceptible and recovered remain unchanged.

0.95

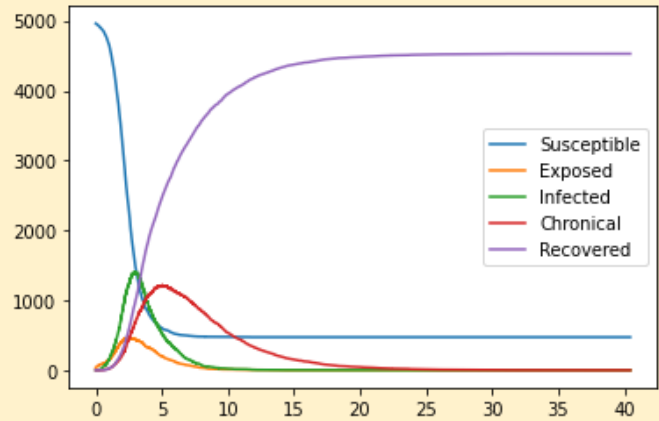


Well recovery rate means good infrastructure ,availability of space, medicine which dominates over S E and other transmissions of the spreading of the disease which indicates Variable **I** doesn't get much time to reach its peak value. Beforehand the spreading recovery is done.(people got 100% immune here : assumption)
So the infected peak value is quite low and so the chronical also and peak value of exposed

			<p>has no significant change. And for these ultimately less no. of people got sick and have gone through the rest process. Significantly high saturated value for susceptible and comparatively less value for recovered.</p> <p>Also we can notice slight decrease in epidemic time-duration.</p> <p>So, overall it represents well stable situation.</p>
5.	Chronical rate(λ) $I \rightarrow C$	0.15	 <p>fast saturation is seen, very short period for epidemic Peak of infected high exposed. Low chronical peak ,rate low so recovery going on fast because then c R transmission also got down...</p>
		0.5	<p>Moderate valued chronical transmission. High chronical peak lower peak compared to the 0.15 chronical rate graph.</p> 

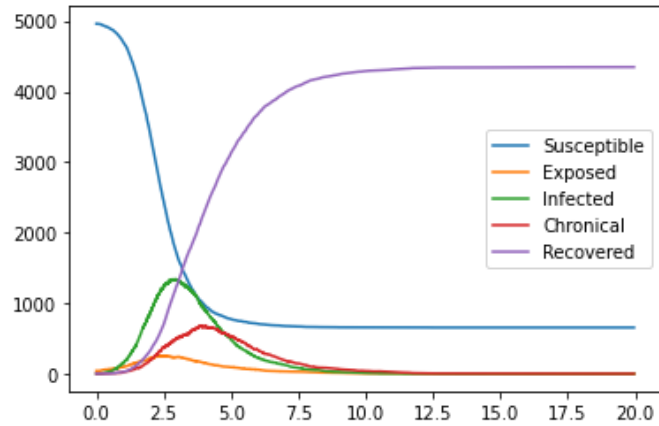
		0.8	 <p>High rate taking time to reach to saturated value... because denotes slow recovery. More people remain susceptible No change in exposed...low infected</p>
6.	Chronical Recovery rate(m) C R	0.05	 <p>Too much fast decay in susceptible too much fast growing in infected chronical too much late decay . Too much time consuming to reach to saturated value (almost 5 times)exposed peak value Very low, rate unchanged</p>

0.25



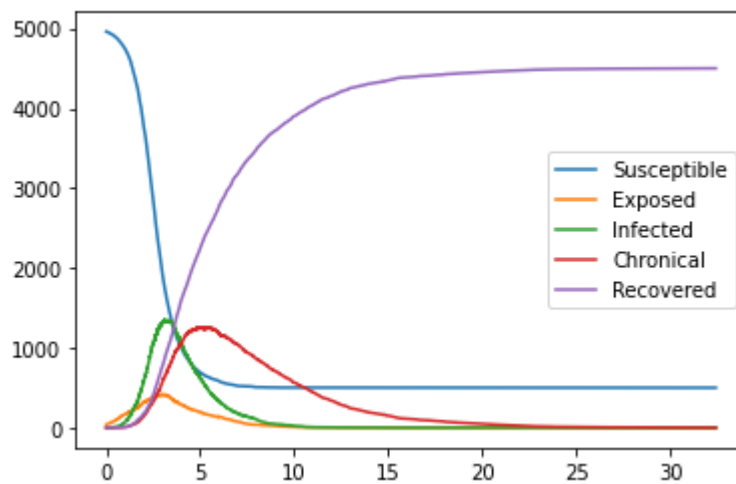
Exposed...no change
Moderate in terms of chronicle
stage and the no. of exposed
increases manifolds

0.8



Chronical low value
Susceptible slight more,
recovered slight less, recovery
rate very fast, infected peak ,
rate unchanged
Exposed unchanged

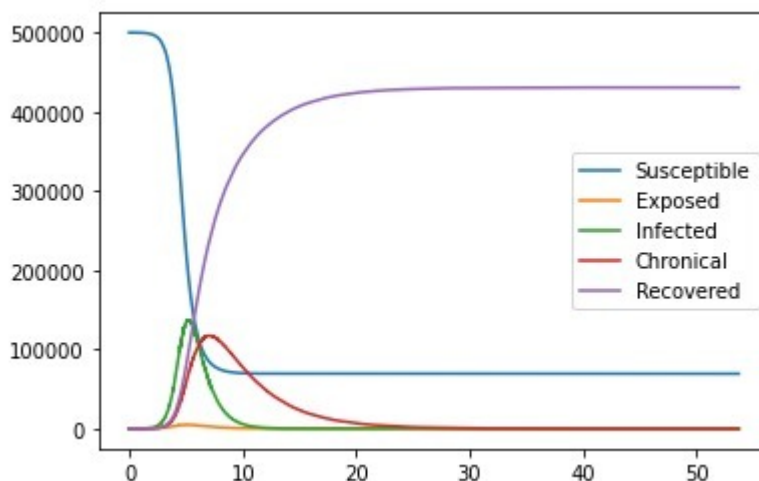
E.) While studying about the model of an epidemic . We come across some interesting facts. Firstly for experimentation we take a control experiment with no. of nodes =5000, degrees per node(avg)=6 and the initial no. of infection = 10 and initial no. of exposed people =40. In the results we see the



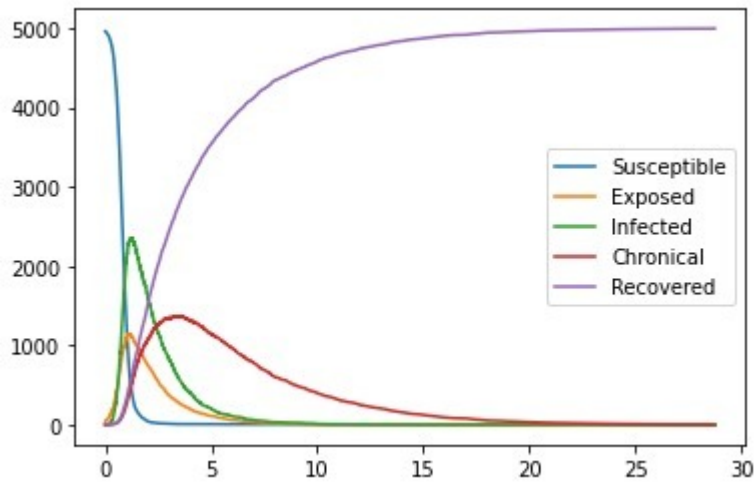
graph,

Now to study the various aspects of the graph we first take the nodes.

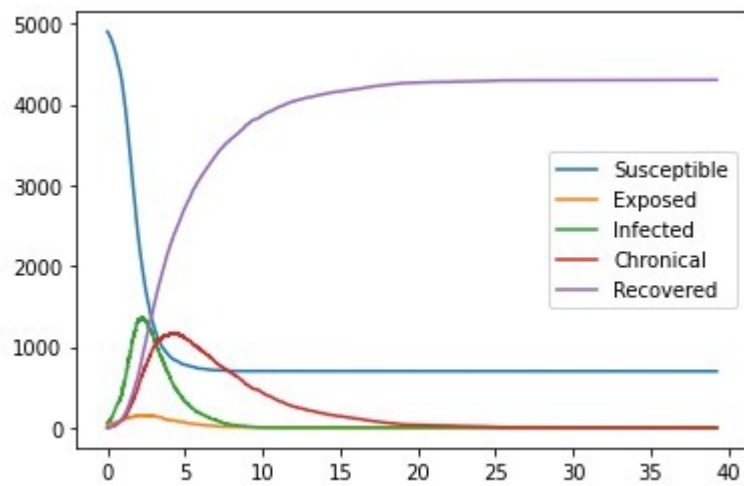
We increase the no. of nodes to 500000 and keeping all other parameters constant we get the following graph



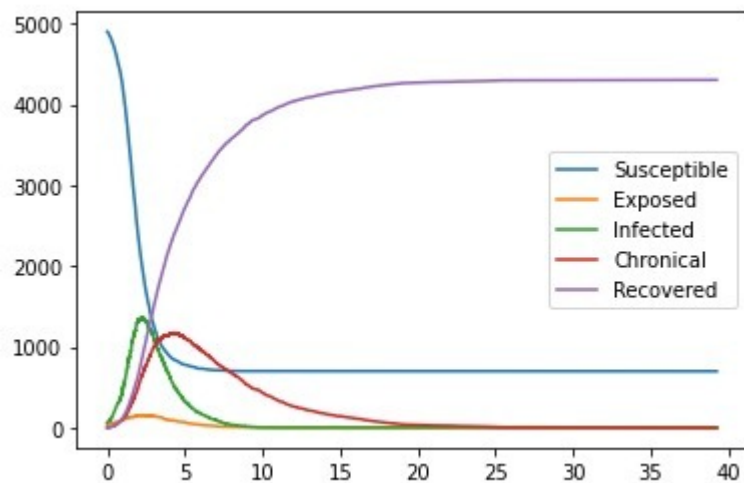
After this we increase the degrees from 6 to 15 and keeping the rest of the parameters at the control level we get the following graph



Again keeping the rest of the parameters at the control value we change the no. of initial infection to 100 from 10 and we get the following graph.



Again keeping all other parameters at the control level we change the value of the initial exposed to 200 from 40.



According to the graphs we received as the results we see that in the first case we can observe that the rate of change of slope of the graph with no. of nodes 500000 is much higher when compared with the control experiment.

When we look at the second graph and compare it with the control we see the infection is much higher and the peak is touched very fast. So we can say that in a well connected society where the people are more connected to each other an epidemic reaches the fast and creates the maximum damage and gets flattened the fastest due to herd immunity.

When we look at the third graph and compare it with the control experiment we see that the graph shifts toward the left hand side if we increase the no. of initial infections the graph shifts towards the left (the infection graph only)

Again we see if we increase the no. of initial exposed and compare it with the control we get the fourth curve which shows us that the exposed graph shifts towards the left. And vice versa now,

When we study more about the epidemic from the graphs we see that the more the no. of people and more the connected they are the higher is the slope resulting the disease will spread faster in that area. So those areas with a higher population density and a higher percentage of interconnected communities we see that there will be a greater spread of the disease and in those areas there will be a very less reaction time in those areas and may lead to the shortage of medicines and health care facilities in the locality leading to a higher no. of deaths and higher economic imbalance in the area .

When it comes to the future of the disease we see the curve is flattened faster in a well connected locality and as a result herd immunity is developed faster in these areas and there also remains a very less scope of viral genome getting mutated to a new variant and probably more dangerous but in all the other cases the virus sits in the society for an ample amount of time and has more chances of forming a variant and again returning back to the society .

We must also take into view the factors we neglected while forming the above graphs such as a lockdown or use of masks, or drinking of filtered water and avoidance of raw food . also we neglected the probable use of vaccinations against the microbial genome and also the health care of the area where the epidemic had spread. From the above graphs we can see the above features about the bacteria/ virus and the outcome of the epidemic and the future of the epidemic.

The End
