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Orientation of 3 ordered points

Orientation of an ordered triplet of points in the plane can be

- counterclockwise
- clockwise
- colinear

The following diagram shows different possible orientations of ([a](#), [b](#), [c](#))



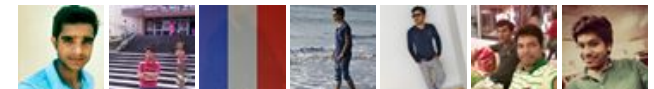
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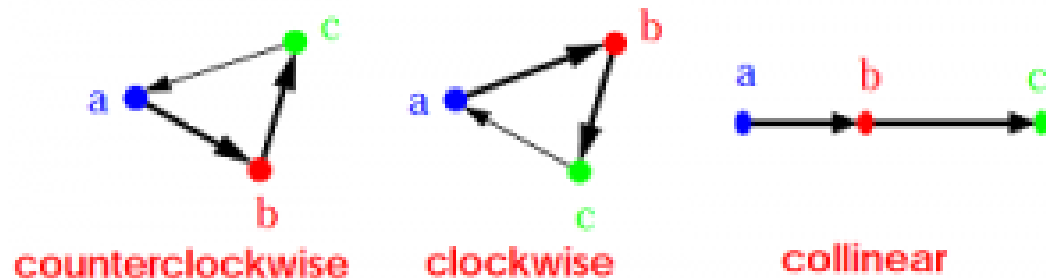


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If orientation of (p_1, p_2, p_3) is collinear, then orientation of (p_3, p_2, p_1) is also collinear.

If orientation of (p_1, p_2, p_3) is clockwise, then orientation of (p_3, p_2, p_1) is counterclockwise and vice versa is also true.

Given three points p_1 , p_2 and p_3 , find orientation of (p_1, p_2, p_3) .

Example:

Input: $p_1 = \{0, 0\}$, $p_2 = \{4, 4\}$, $p_3 = \{1, 2\}$

Output: CounterClockWise

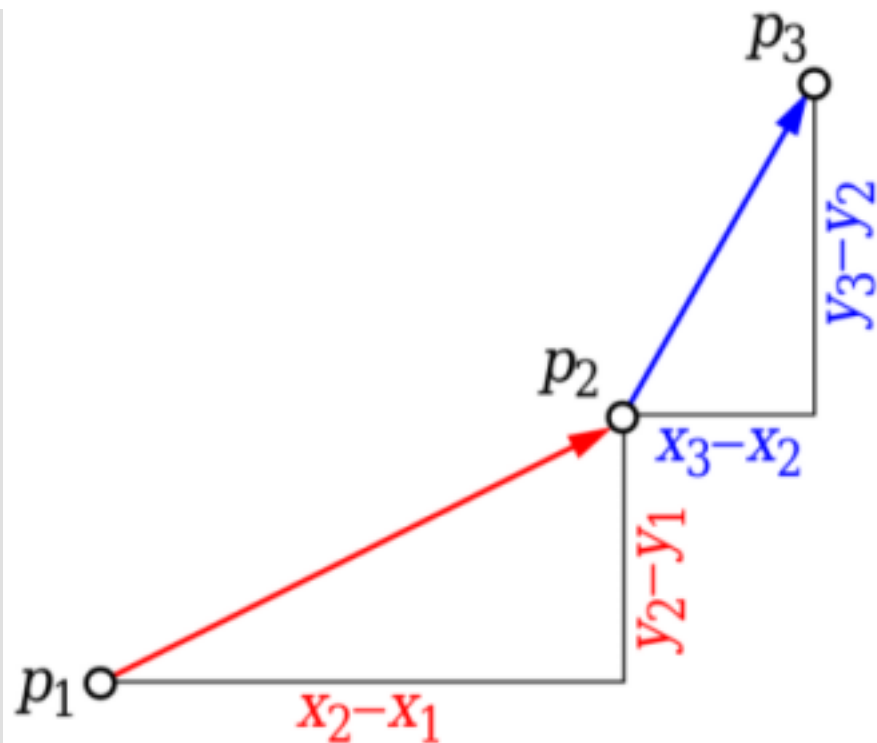
Input: $p_1 = \{0, 0\}$, $p_2 = \{4, 4\}$, $p_3 = \{1, 1\}$

Output: Colinear

How to compute Orientation?

The idea is to use slope.

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Slope of line segment (p1, p2): $\sigma = (y_2 - y_1)/(x_2 - x_1)$

Slope of line segment (p2, p3): $\tau = (y_3 - y_2)/(x_3 - x_2)$

If $\sigma < \tau$, the orientation is counterclockwise (left turn)

If $\sigma = \tau$, the orientation is collinear

If $\sigma > \tau$, the orientation is clockwise (right turn)

Using above values of σ and τ , we can conclude that,
the orientation depends on sign of below expression:

$$(y_2 - y_1)(x_3 - x_2) - (y_3 - y_2)(x_2 - x_1)$$

Above expression is negative when $\sigma < \tau$, i.e., counterclockwise

Above expression is 0 when $\sigma = \tau$, i.e., collinear

Above expression is positive when $\sigma > \tau$, i.e., clockwise

Below is C++ implementation of above idea.

```
// A C++ program to find orientation of three points
#include <iostream>
using namespace std;

struct Point
{
    int x, y;
};

// To find orientation of ordered triplet (p1, p2, p3).
// The function returns following values
// 0 --> p, q and r are colinear
// 1 --> Clockwise
// 2 --> Counterclockwise
int orientation(Point p1, Point p2, Point p3)
{
    // See 10th slides from following link for derivation
    // of the formula
    int val = (p2.y - p1.y) * (p3.x - p2.x) -
              (p2.x - p1.x) * (p3.y - p2.y);

    if (val == 0) return 0; // colinear

    return (val > 0)? 1: 2; // clock or counterclock wise
}

// Driver program to test above functions
```

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```

int main()
{
    Point p1 = {0, 0}, p2 = {4, 4}, p3 = {1, 2};
    int o = orientation(p1, p2, p3);
    if (o==0)          cout << "Linear";
    else if (o == 1)   cout << "Clockwise";
    else               cout << "CounterClockwise";
    return 0;
}

```

Output:

CounterClockwise

The concept of orientation is used in below articles:

[Find Simple Closed Path for a given set of points](#)

[How to check if two given line segments intersect?](#)

[Convex Hull | Set 1 \(Jarvis's Algorithm or Wrapping\)](#)

[Convex Hull | Set 2 \(Graham Scan\)](#)

Source:

<http://www.dcs.gla.ac.uk/~pat/52233/slides/Geometry1x1.pdf>

This article is contributed by **Rajeev Agrawal**. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above

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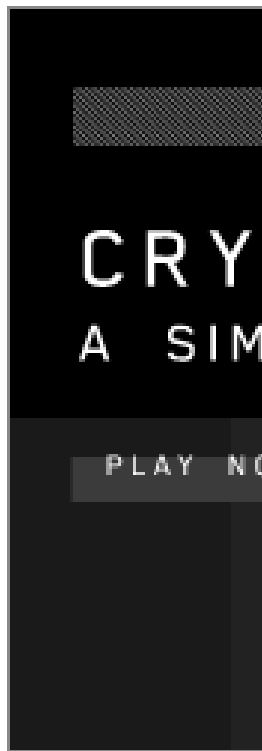
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Yt R · 11 days ago

Time complexity: $O(1)$

Auxiliary space: $O(1)$

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Siva Krishna • 11 days ago

$(y_2 - y_1)(x_3 - x_2) - (y_3 - y_2)(x_1 - x_1)$

It should be

$(y_2 - y_1)(x_3 - x_2) - (y_3 - y_2)(x_2 - x_1)$

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GeeksforGeeks Mod → Siva Krishna • 11 days ago

Thanks for pointing this out. We have updated the post.

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