

Q2) function ~~f(x)~~  $x = f(n)$

$x = 1;$

for  $i = 1:n$

for  $j = 1:n$

$x = x + 1;$

1) Find the runtime of the algorithm mathematically

Inner loop:

It executes  $n$  times for each phase in outer loop.

$\therefore n$  executions for inner loop

Outer loop:

It executes  $n$  times from  $i = 1$  to  $i = n$

$\therefore n$  executions for outer loop

$$\text{Total executions} = \sum_{i=1}^n \sum_{j=1}^n 1$$

$$= \sum_{i=1}^n n$$

$$= n \times n$$

$$= n^2$$

$\therefore$  The total runtime of the algorithm is  $O(n^2)$

3) Find polynomials that are upper and lower bounds on your curve. From this specify big-O, big-Omega, big-theta is

Big-O Notation (Upper bound)

$O(n^2)$  - function does not grow faster than quadratic

Big-Omega

$\Omega(n^2)$  - function does not grow slower than quadratic

Big Theta

$\Theta(n^2)$  - function grows asymptotically as  $n^2$

If I modified the function to be:

$x = f(n)$

$x = 1;$

$y = 1;$

for  $i = 1:n$

for  $j = 1:n$

$x = x + 1;$

$y = y + i + j;$

4) Will this increase how long it takes the algorithm to run?

$y = i + j$ , actual time taken by the modified function will be slightly longer due to it.

$\therefore O(n^2)$  is the time complexity.

5) Will it effect your results from first function?

It doesn't effect much in the time complexity.