

Part - A: ① 255.375

$$255 \div 2 = 2(127) + 1$$

$$0.375 \times 2 = 0.75(0)$$

$$127 \div 2 = 2(63) + 1$$

$$0.75 \times 2 = 1.5(1)$$

$$0.5 \times 2 = 1(0)$$

$$(110)_2$$

$$63 \div 2 = 2(31) + 1$$

$$31 \div 2 = 2(15) + 1$$

$$15 \div 2 = 2(7) + 1$$

$$7 \div 2 = 2(3) + 1$$

$$3 \div 2 = 2(1) + 1$$

$$1 \div 2 = 0 + 1$$

$$(11111111)_2$$

Ans: $(11111111)_2 \cdot (110)_2 = (377)_8 \cdot (3)_8$

$$= (1515)_{16} \cdot (3)_{16}$$

$$\rightarrow \text{FF} \cdot (6)_{16}$$

② We go from top to down when writing fractional part

ex. 0.101 \Rightarrow we got $x \times 2 = 1$ at last digit
thus $x = 0.5$

$$2 \times 0.625 \rightarrow 1.25$$

$$\therefore \text{Fractional part} = 0.625$$

$$2 \times 0.25 = 0.5$$

$$2 \times 0.5 = 1$$

$$\therefore \text{Integral} = 53$$

③ $(100111)_2$

$$3 + 2^2(1+8)$$

Divisible by 3

$$1 \cdot 100 + 2^1 + 2^2 + 2^3 = 3 + 2^1 + 2^2 + 2^3$$

WORLDONE

$$32 \rightarrow 2^5 (2^4 + 2^4) \neq 10$$

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$$\textcircled{3} (100111)_2 = 2^0 + 2^1 + 2^2 + 2^5 = 32$$

$$2^n \Rightarrow n = \text{even} \quad 2^n \% 3 = 1$$

$$n = \text{odd} \quad 2^n \% 3 = 2$$

\therefore Adding up remainders $\Rightarrow 1 + 2 + 1 + 2 = 6 \Rightarrow 6$ Thus
 $=$ this no
 is divisible by

$$\textcircled{4} F = (A+B)(A'+C)(B+C')$$

$$(A \cdot A' + A \cdot C + A'B + BC)(B+C')$$

\downarrow

$A \cdot A' = 0$ (If $A=0$ then $A'=1$, both never 1 at same time)

$$(A \cdot C + A'B + BC)(B+C')$$

$$ABC + \cancel{ABC} + \cancel{A \cdot C \cdot C'} + A \cdot \underline{C \cdot C'} + A'B \cdot B + A'BC' + (B \cdot B)C + 0$$

$$B \cdot B = B \text{ (From truth table)}$$

$$ABC + A'B + A'BC' + B \cdot C$$

$$B[A' + A \cdot C] + B[C + A'C']$$

$$B[A' + A] \cdot (A' + C) + B[C + C'] \cdot (A' + C)$$

A or $\bar{A} = 1$ (one of the always true)

$$C + \bar{C} = 1$$

$$B(A' + C) + B(A' + C) \Rightarrow \boxed{B(A' + C)}$$

⑥

	A	B	C
m_0	0	0	0
m_1	0	0	1
m_2	0	1	0
m_3	0	1	1
m_4	1	0	0
m_5	1	0	1
m_6	1	1	0
m_7	1	1	1

$$F(A, B, C) = \sum m(1, 3, 5, 7)$$

$$= \bar{A}\bar{B}C + \bar{A}BC + A\bar{B}C + ABC$$

$$\Rightarrow \bar{A}C[B + \bar{B}] + AC[B + \bar{B}]$$

$$= C[A + \bar{A}] = \boxed{C}$$

④ $23 \Rightarrow (10111)_2$

~~Ques~~ For 1's complement: Invert 1 and 0

$$\begin{array}{l} 1000 \\ (1000)_2 \\ (11101000)_2 \end{array}$$

$$\text{Add } +1 \Rightarrow (11101001)_2$$

↳ Ans