

## □ LeetCode 1021 – Remove Outermost Parentheses

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### ◆ Problem Statement (Simple Words)

You are given a **valid parentheses string** `s`.

A **primitive parentheses string** is one that:

- Is non-empty
- Is valid
- Cannot be split into two valid parentheses strings

👉 For **each primitive**, remove its **outermost parentheses**

👉 Finally, **combine all results**

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### ◆ Example

#### Input

`s = "(()())()"`

#### Step 1: Split into primitives

`"(()())" "()"`

#### Step 2: Remove outermost parentheses

`"()()" "()"`

#### Output

`"()()"`

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### □ Key Idea (Using COUNT variable)

Instead of using a stack, we use a **counter**:

- count tracks **how deep** we are inside parentheses
- `'('` → increase count
- `')'` → decrease count

### 🔑 Important Rule

#### Character When to ADD to result

`(`            if count > 0

`)`            if count > 1

Why?

- The **outermost parentheses** always occur when:
  - '(' → count == 0
  - ')' → count == 1
- We **skip those**

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### Dry Run (Step-by-Step)

**Input**

s = "(()())()"

**Initialize**

count = 0

result = ""

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**Walk Through Each Character**

**Char Before count Action After count Add to result? Result**

|   |   |         |         |   |           |          |
|---|---|---------|---------|---|-----------|----------|
| ( | 0 | count++ | 1       | ✗ | outermost | ""       |
| ( | 1 | count++ | 2       | ✓ |           | "("      |
| ) | 2 | add     | count-- | 1 |           | "()"     |
| ( | 1 | count++ | 2       | ✓ |           | "()("    |
| ) | 2 | add     | count-- | 1 |           | "()()"   |
| ) | 1 | count-- | 0       | ✗ | outermost | "()()"   |
| ( | 0 | count++ | 1       | ✗ |           | "()()"   |
| ( | 1 | count++ | 2       | ✓ |           | "()()("  |
| ) | 2 | add     | count-- | 1 |           | "()()()" |
| ) | 1 | count-- | 0       | ✗ |           | "()()()" |

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 **Final Output**

"()()()"

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## □ Why This Works

- `count == 0` → 1 → entering a primitive → **skip '('**
  - `count == 1` → 0 → exiting a primitive → **skip ')'**
  - Everything inside → **keep it**
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## ✓ Code Implementations

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### Java Code

```
class Solution {  
    public String removeOuterParentheses(String s) {  
        StringBuilder result = new StringBuilder();  
        int count = 0;  
  
        for (char ch : s.toCharArray()) {  
            if (ch == '(') {  
                if (count > 0) {  
                    result.append(ch);  
                }  
                count++;  
            } else {  
                if (count > 1) {  
                    result.append(ch);  
                }  
                count--;  
            }  
        }  
        return result.toString();  
    }  
}
```

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### C++ Code

```
class Solution {
public:
    string removeOuterParentheses(string s) {
        string result = "";
        int count = 0;

        for (char ch : s) {
            if (ch == '(') {
                if (count > 0)
                    result += ch;
                count++;
            } else {
                if (count > 1)
                    result += ch;
                count--;
            }
        }
        return result;
    }
};
```

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### Python Code

```
class Solution:
    def removeOuterParentheses(self, s: str) -> str:
        result = []
        count = 0

        for ch in s:
            if ch == '(':
                if count > 0:
                    result.append(ch)
```

```
        count += 1
    else:
        if count > 1:
            result.append(ch)
        count -= 1

    return "".join(result)
```

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### Complexity Analysis

#### Metric Value

Time  **$O(n)$**

Space  **$O(n)$**  (output only)